



- 2. The drift velocity of electrons for a conductor connected in an electrical circuit is V_d. The conductor in now replaced by another conductor with same material and same length but double the area of cross section. The applied voltage remains same. The new drift velocity of electrons will be
- (1) V_d (2) $\frac{V_d}{4}$ (3) 2 V_d (4) $\frac{V_d}{2}$ Sol. (1) $V = IR = I\left(\frac{\rho l}{A}\right)$ $A \rightarrow 2A$ $I \rightarrow 2I$ $I = AneV_d$ $V_d \propto \frac{I}{A}$
- **3.** The initial speed of a projectile fired from ground is *u*. At the highest point during its motion, the speed of projectile is $\frac{\sqrt{3}}{2}u$. The time of flight of the projectile is :

(1) $\frac{2u}{g}$ (2) $\frac{u}{2g}$ (3) $\frac{\sqrt{3}u}{g}$ (4) $\frac{u}{g}$ Sol. (4) At highest point $u\cos\theta = \frac{\sqrt{3}u}{2}$ $\theta = 30^{\circ}$ $T = \frac{2u\sin\theta}{g} = \frac{u}{g}$

Give yourself an extra edge



4. The correct relation between
$$\gamma = \frac{c_p}{c_p}$$
 and temperature *T* is :
(1) $\gamma \alpha T^0$ (2) $\gamma \alpha T$ (3) $\gamma \alpha \frac{1}{\sqrt{T}}$ (4) $\gamma \alpha \frac{1}{T}$
Sol. (1)
 $\gamma = \frac{C_p}{C_v}$, Independent on T
5. The effect of increase in temperature on the number of electrons in conduction band (n_e) and resistance of a semiconductor will be as:
(1) Both n_e and resistance increase (2) Both n_e and resistance decrease
(3) n_e decreases, resistance increase (4) n_e increases, resistance decreases
(3) n_e decreases, resistance increases (4) n_e increases, resistance decreases
Sol. (4)
In semi conductors,
 T^{\uparrow}, n_v in Conduction Band increases
 $T^{\uparrow}, R^{\downarrow}$
6. The amplitude of 15sin(1000 πt) is modulated by 10sin($4\pi t$) signal. The amplitude modulated signal contains frequency (ies) of
A. 500 Hz B. 2 Hz C. 250 Hz D. 498 Hz E. 502 Hz
Choose the correct answer from the options given below:
(1) A Only (2) B Only (3) A and B Only (4) A, D and E Only
Sol. (4)
 $f_c = \frac{1000\pi}{2\pi} = 500$ Hz
 $f_m = \frac{4\pi}{2\pi} = 2$ Hz
Upper side Band, USB = $f_c + f_n$
USB = 502HZ
Lower side Band, $\frac{LSB}{LSB} = \frac{f_c}{-f_m}$
LSB = 502Hz

7. Two polaroide A and B are placed in such a way that the pass-axis of polaroids are perpendicular to each other. Now, another polaroid *C* is placed between *A* and *B* bisecting angle between them. If intensity of unpolarized light is I_0 then intensity of transmitted light after passing through polaroid B will be:

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(1) $\frac{I_0}{4}$ (2) $\frac{I_0}{2}$ (3) Zero (4) $\frac{I_0}{8}$ Sol. (4) After A, $I = \frac{I_0}{2}$ After C, $I = \frac{I_0}{2} \cos^2 45^\circ = \frac{I_0}{4}$ After B, $I = \frac{I_0}{4} \cos^2 45^\circ = \frac{I_0}{8}$

Give yourself an extra edge



8. As shown in figure, a 70 kg garden roller is pushed with a force of $\vec{F} = 200$ N at an angle of 30° with horizontal. The normal reaction on the roller is (Given g = 10 m s⁻²)



9. If 1000 droplets of water of surface tension 0.07 N/m, having same radius 1 mm each, combine to from a single drop. In the process the released surface energy is-

$$(Take \pi = \frac{22}{7})$$
(1) 8.8 × 10⁻⁵ J
(2) 7.92 × 10⁻⁴ J
(3) 7.92 × 10⁻⁶ J
(4) 9.68 × 10⁻⁴ J
Sol.
(2)
$$V_1 = V_2$$

$$1000 \times \frac{4}{3} \pi r^3 = \frac{4}{3} \pi R^3$$

$$R = 10r$$

$$E = U_1 - U_2$$

$$= 1000 (T \times 4\pi r^2) - T \times 4\pi R^2$$

Give yourself an extra edge





- $E = 4\pi T \left(1000 \times r^2 100r^2 \right)$ $E = 4 \times \frac{22}{7} \times 0.07 \times 900 \times 10^{-6}$ $E = 7.92 \times 10^{-4} \text{ J}$
- **10.** The pressure of a gas changes linearly with volume from *A* to *B* as shown in figure. If no heat is supplied to or extracted from the gas then change in the internal energy of the gas will be



Given below are two statements: One is labelled as Assertion A and the other is labelled as Reason R Assertion A: The beam of electrons show wave nature and exhibit interference and diffraction. Reason R: Davisson Germer Experimentally verified the wave nature of electrons.In the light of the above statements, choose the most appropriate answer from the options given

In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) Both A and R are correct and R is the correct explanation of A
- (2) A is not correct but R is correct
- (3) A is correct but R is not correct
- (4) Both A and R are correct but R is Not the correct explanation of A
- Sol. (1)

Theoritical

- **12.** A free neutron decays into a proton but a free proton does not decay into neutron. This is because (1) proton is a charged particle
 - (2) neutron is an uncharged particle
 - (3) neutron is a composite particle made of a proton and an electron
 - (4) neutron has larger rest mass than proton
- Sol. (4)

Rest mass of neutron is greater than proton.

Give yourself an extra edge



13. Spherical insulating ball and a spherical metallic ball of same size and mass are dropped from the same height. Choose the correct statement out of the following Assume negligible air friction}

(1) Insulating ball will reach the earth's surface earlier than the metal ball

(2) Metal ball will reach the earth's surface earlier than the insulating ball

(3) Both will reach the earth's surface simultaneously.

(4) Time taken by them to reach the earth's surface will be independent of the properties of their materials

Sol. (1)

In Conductor, A portion of the Gravitational Potential Energy goes into generating eddy current.

14. If R, X_L, and X_C represent resistance, inductive reactance and capacitive reactance. Then which of the following is dimensionless :

(1)
$$\frac{R}{X_L X_C}$$
 (2) $\frac{R}{\sqrt{X_L X_C}}$ (3) $R \frac{X_L}{X_C}$ (4) $R X_L X_C$

Sol. (2)

 $R, X_{\scriptscriptstyle L}, X_{\scriptscriptstyle C}$ have same unit i.e. ohm

$$\frac{R}{\sqrt{x_L x_c}} \rightarrow \frac{ohm}{\sqrt{ohm^2}} \rightarrow Dimensionless$$

15. 100 balls each of mass m moving with speed v simultaneously strike a wall normally and reflected back with same speed, in time t sec. The total force exerted by the balls on the wall is

Sol. (4) (1) $\frac{100mv}{t}$ (2) 200mvt (3) $\frac{mv}{100t}$ [200mv t (3) $\frac{mv}{t}$

Change in momentum,

$$|\overrightarrow{\Delta p}| = 2mV$$

Average force,

$$F_{avg} = N \frac{\left| \overline{\Delta \rho} \right|}{t}$$
$$F_{avg} = 100 \left(\frac{2mV}{t} \right)$$
$$F_{avg} = \frac{200mV}{t}$$



16. If a source of electromagnetic radiation having power 15 kW produces 10^{16} photons per second, the radiation belongs to a part of spectrum is. (Take Planck constant $h = 6 \times 10^{-34}$ Js)

(1) Micro waves (2) Ultraviolet rays

(3) Gamma rays

(4) Radio waves

Sol. (3)

$$P = \frac{N}{t} \left(\frac{hc}{\lambda}\right)$$

$$15 \times 10^{3} = 10^{16} \times \frac{6 \times 10^{-34} \times 3 \times 10^{8}}{\lambda}$$

$$\lambda = 1.2 \times 10^{-13} \text{ m}$$

$$\lambda = 0.0012 \text{ A}^{0}$$

Corresponds to Gamma rays

17. Which of the following correctly represents the variation of electric potential (V) of a charged spherical conductor of radius (R) with radial distance (r) from the center?



Give yourself an extra edge



A bar magnet with a magnetic moment 5.0Am² is placed in parallel position relative to a magnetic field of 0.4 T. The amount of required work done in turning the magnet from parallel to antiparallel position relative to the field direction is ______.
 (1) 1 L ______ (2) 4 L ______ (2) 2 L ______ (4) zero

(1) 1) (2) 4) (3) 2) (4) zero
Sol. (2)

$$W = MB(\cos\theta_1 - \cos\theta_2)$$

 $W = MB(\cos0^\circ - \cos180^\circ)$
 $W = 2MB$
 $W = 2 \times 5 \times 0.4$
 $W = 4$ J

19. At a certain depth "d " below surface of earth, value of acceleration due to gravity becomes four times that of its value at a height 3R above earth surface. Where *R* is Radius of earth (Take R = 6400 km). The depth d is equal to

(1) 4800 km (2) 2560 km (3) 640 km (4) 5260 km Given $g\left(1-\frac{d}{R}\right) = 4\frac{g}{\left(1+\frac{h}{R}\right)^2}$ $1-\frac{d}{R} = \frac{4}{(1+3)^2} = \frac{1}{4}$ $\frac{d}{R} = \frac{3}{4}$ $d = \frac{3R}{4} = \frac{3}{4} \times 6400$ d = 4800km

20. A rod with circular cross-section area 2 cm² and length 40 cm is wound uniformly with 400 turns of an insulated wire. If a current of 0.4 A flows in the wire windings, the total magnetic flux produced inside windings is $4\pi \times 10^{-6}$ Wb. The relative permeability of the rod is (Given : Permeability of vacuum $\mu_0 = 4\pi \times 10^{-7}$ NA⁻²)

$(1)\frac{5}{16}$	(2) 12.5	(3) 125	$(4)\frac{32}{5}$
(1)			

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NTA Ans. (3)

Magnetic field in the Solenoid,

B = \mu_0 \mu_r nI
Magnetic flux, \phi = N(BA)

\phi = N(\mu_0 \mu_r n IA)

4\pi \times 10^{-6} = 400 \left( 4\pi \times 10^{-7} \mu_r \times \frac{400}{0.4} \times 0.4 \times 2 \times 10^{-4} \right)

\frac{1}{40} = \mu_r \times 8 \times 10^{-2}

\mu_r = \frac{100}{320} = \frac{5}{16}
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Give yourself an extra edge

Sol.



SECTION - B

In a medium the speed of light wave decreases to 0.2 times to its speed in free space The ratio of 21. relative permittivity to the refractive index of the medium is x: 1. The value of x is (Given speed of light in free space = 3×10^8 m s⁻¹ and for the given medium $\mu_r = 1$)

Sol. (5)

$$V = \frac{c}{n}$$

 $n \rightarrow$ refractive index

$$n = \frac{c}{0.2c} = 5$$
$$n = \sqrt{\mu_r \varepsilon_r}$$
$$\varepsilon_r = n^2 = 25$$
$$\frac{\varepsilon_r}{n} = \frac{25}{5} = \frac{5}{1}$$

A solid sphere of mass 1 kg rolls without slipping on a plane surface. Its kinetic energy is 7×10^{-3} J. 22. The speed of the centre of mass of the sphere is cms⁻¹

Sol. (10)

On Rolling,

On Rolling,

$$KE = \frac{1}{2}MV^2 + \frac{1}{2}I\omega^2$$

 $KE = \frac{1}{2}MV^2 + \frac{1}{2}(\frac{2}{5}MR^2)(\frac{v}{R})^2$
 $KE = \frac{7}{10}MV^2 = 7 \times 10^{-3}$
 $V^2 = 10^{-2}$
 $V = 10^{-1} \text{m/s}$
 $V = 10 \text{cm/s}$

- A lift of mass M = 500 kg is descending with speed of 2 ms⁻¹. Its supporting cable begins to slip thus 23. allowing it to fall with a constant acceleration of 2 ms^{-2} . The kinetic energy of the lift at the end of fall through to a distance of 6 m will be _____ kJ.
- Sol. (7)

Acceleration is constant,

 $v^{2} = u^{2} + 2as$ $v^2 = 2^2 + 2(2)(6)$ $v^2 = 28$ $\frac{1}{2}Mv^2 = \frac{1}{2} \times 500 \times 28$ KE = 7kJ

Give yourself an extra edge



24. In the figure given below, a block of mass M = 490 g placed on a frictionless table is connected with two springs having same spring constant (K = 2 N m⁻¹). If the block is horizontally displaced through 'X' m then the number of complete oscillations it will make in 14π seconds will be _____.



Sol. (20)

$$T = 2\pi \sqrt{\frac{m}{k_{eq}}}$$
$$T = 2\pi \sqrt{\frac{m}{2k}}$$
$$T = 2\pi \sqrt{\frac{0.49}{2 \times 2}}$$
$$T = 2\pi \times \frac{0.7}{2} = 0.7\pi$$
in 14\pi sec, $\frac{14\pi}{0.7\pi} = 20$

25. An inductor of 0.5mH, a capacitor of 20μ F and resistance of 20Ω are connected in series with a 220 V ac source. If the current is in phase with the emf, the amplitude of current of the circuit is \sqrt{x} A. The value of *x* is-

READY

Sol. (242)

Current is in phase with EMF. Hence, Circuit is at Resonance.

$$I_{rms} = \frac{V_{rms}}{R} = \frac{220}{20}$$
$$I_{rms} = 11A$$
$$I_0 = \sqrt{2} I_{rms} = \sqrt{242}A$$

26. The speed of a swimmer is 4 km h^{-1} in still water. If the swimmer makes his strokes normal to the flow of river of width 1 km, he reaches a point 750 m down the stream on the opposite bank. The speed of the river water is _____ kmh^{-1}.

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Sol. (3)

$$T = \frac{D}{V} = \frac{1}{4}hr$$
Drift = uT

$$\frac{750}{1000} \text{kM} = u \times \frac{1}{4}hr$$

$$u = 3\text{km/hr}$$

$$T = \frac{D}{V} = \frac{1}{4}hr$$

$$U = \frac{1}{4}hr$$

Give yourself an extra edge



27. For hydrogen atom, λ_1 and λ_2 are the wavelengths corresponding to the transitions 1 and 2 respectively as shown in figure. The ratio of λ_1 and λ_2 is $\frac{x}{32}$. The value of x is



28. Two identical cells, when connected either in parallel or in series gives same current in an external resistance 5Ω. The internal resistance of each cell will be Ω.
 Sol. (5)



$$r_{eq} = \frac{r}{2}, r_{eq} = 2r$$

$$E_{eq} = \frac{r}{2} \left(\frac{E}{r} + \frac{E}{r}\right) = E, E_{eq} = 2E$$

$$I_{1} = \frac{E}{5 + \frac{r}{2}}, I_{2} = \frac{2E}{2r + 5}$$

$$I_{1} = I_{2}$$

$$2r + 5 = 2\left(5 + \frac{r}{2}\right)$$

$$r = 5\Omega$$

Give yourself an extra edge



29. Expression for an electric field is given by $\vec{E} = 4000x^2 \hat{i} \frac{V}{m}$. The electric flux through the cube of side 20 cm when placed in electric field (as shown in the figure) is _____ V cm



Sol. (640)



 $\vec{E} \perp \vec{A}, \phi_{Top} = \phi_{Bottom} = \phi_{Front} = \phi_{Back} = 0$ for *OCDG*, $x = 0, E = 0, \phi = 0$ for *ABEF*, x = 0.2m $E = 4000 \times (0.2)^2$ E = 160V / m $\phi = E(a^2) = 160V / m \times (0.2)^2 m^2$ $\phi = 6.4V - m$ $\phi = 640V - cm$

30. A thin rod having a length of 1 m and area of cross-section 3×10^{-6} m² is suspended vertically from one end. The rod is cooled from 210°C to 160°C. After cooling, a mass *M* is attached at the lower end of the rod such that the length of rod again becomes 1 m. Young's modulus and coefficient of linear expansion of the rod are 2×10^{11} N m⁻² and 2×10^{-5} K⁻¹, respectively. The value of M is _____ kg. (Take g = 10 m s⁻²)

Sol. (60)

$$Y = \frac{FL}{A\Delta L}$$

$$F = YA\left(\frac{\Delta L}{L}\right)$$

$$F = YA(\alpha\Delta T)$$

$$Mg = YA(\alpha\Delta T)$$

$$M \times 10 = 2 \times 10^{11} \times 3 \times 10^{-6} \times 2 \times 10^{-5} \times 50$$

$$M = 60 \text{kg}$$



Sol.

32.

SECTION - A





Give yourself an extra edge

(2)

NH2

CH2

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(4)

CH2NH2





Sol. 1



33. An organic compound 'A' with emperical formula C_6H_60 gives sooty flame on burning. Its reaction with bromine solution in low polarity solvent results in high yield of B.B is



34. When Cu^{2+} ion is treated with KI, a white precipitate, X appears in solution. The solution is titrated with sodium thiosulphate, the compound Y is formed. X and Y respectively are

(1)
$$X = CuI_2$$
 $Y = Na_2 S_4O_6$
(2) $X = CuI_2$ $Y = Na_2 S_2O_3$
(3) $X = Cu_2I_2$ $Y = Na_2 S_4O_5$

(4)
$$X = Cu_2I_2$$
 $Y = Na_2 S_4O_5$
(4) $X = Cu_2I_2$ $Y = Na_2 S_4O_5$

4

Sol.

'M' Electrolysis & liquation is method of purification where as hydraulic washing, leading, froth flotation are method of can conbration.







Give yourself an extra edge



37. The methods NOT involved in concentration of ore are
A. Liquation B. Leaching C. Electrolysis D. Hydraulic washing
E. Froth floatation
Choose the correct answer from the options given below :
(1) C, D and E only (2) B, D and C only (3) A and C only (4) B, D and E only

Sol. 3

Methods involved in concentration of one are

- (i) Hydraulic Washing
- (ii) Froth Flotation
- (iii) Magnetic Separation
- (iv) Leaching
- **38.** A protein 'X' with molecular weight of 70,000u, on hydrolysis gives amino acids. One of these amino acid is



Sol. 3

 $Na = 4f^4 5d^0 6s^2$ $Na^{+2} = 4f^4 5d^0 6s^0$

40. Match List I with List II

List I	List II
A. XeF ₄	I. See-saw
B. SF ₄	II. Square planar
C. NH ₄ ⁺	III. Bent T-shaped
D. BrF ₃	IV. Tetrahedral

Choose the correct answer from the options given below : (1) A-IV, B-III, C-II, D-I (3) A-II, B-I, C-III, D-IV (4) A-II, B-I, C-IV, D-III





Sol. 4

XeF ₄	Sq. planar
SF ₄	see saw
NH_4^+	Tetrahedral
BrF₃	Bent 'T' shaped

41. Identify X, Y and Z in the following reaction. (Equation not balanced)

$$ClO + NO_2 \rightarrow \underline{X} \xrightarrow{H_2O} \underline{Y} + \underline{Z}$$

- (1) $X = CIONO_2$, Y = HOCI, $Z = HNO_3$ (2) $X = CIONO_2$, Y = HOCI, $Z = NO_2$ (3) $X = CINO_2$, Y = HCI, $Z = HNO_3$
- (4) $X = CINO_3, Y = Cl_2, Z = NO_2$

Sol. 1

$$ClO+NO_2 \longrightarrow ClO.NO_2 \longrightarrow HOCl+HNO_3$$

- **42.** The correct increasing order of the ionic radii is (1) $S^{2-} < Cl^- < Ca^{2+} < K^+$ (2) $K^+ < S^{2-} < Ca^{2+} < Cl^-$
 - (3) $Ca^{2+} < K^+ < Cl^- < S^{2-}$ (4) $Cl^- < Ca^{2+} < K^+ < S^{2-}$

Sol. 3

For isoelectronic species size $\propto \frac{1}{2}$

 $Ca^{+2} < K^+ < Cl^- < S^{-2}$: size Z : 20 19 17 18

43. Cobalt chloride when dissolved in water forms pink colored complex \underline{X} which has octahedral geometry. This solution on treating with conc HCl forms deep blue complex, \underline{Y} which has a \underline{Z} geometry. X, Y and Z, respectively, are

(1) $X = [Co(H_2O)_6]^{2+}, Y = [CoCl_4]^{2-}, Z = Tetrahedral$ $(2) <math>X = [Co(H_2O)_6]^{2+}, Y = [CoCl_6]^{3-}, Z = Octahedral$ $(3) <math>X = [Co(H_2O)_4Cl_2]^+, Y = [CoCl_4]^{2-}, Z = Tetrahedral$ $(4) <math>X = [Co(H_2O)_6]^{3+}, Y = [CoCl_6]^{3-}, Z = Octahedral$

Sol. 1

$$\operatorname{CoCl}_{2} + \operatorname{H}_{2}O \longrightarrow [\operatorname{Co}(\operatorname{H}_{2}O)_{6}]^{2+} \xrightarrow[\operatorname{Conc. HCl}]{\operatorname{CoCl}_{4}} [\operatorname{CoCl}_{4}]^{2-}$$

_{Pink} Blue Tetrahderal

44. H_2O_2 acts as a reducing agent in

(1)
$$2\text{NaOCl} + \text{H}_2\text{O}_2 \rightarrow 2\text{NaCl} + \text{H}_2\text{O} + \text{O}_2$$

(3)
$$2Fe^{2+} + 2H^+ + H_2O_2 \rightarrow 2Fe^{3+} + 2H_2O$$

(2) $Na_2 S + 4H_2O_2 \rightarrow Na_2SO_4 + 4H_2O$ (4) $Mn^{2+} + 2H_2O_2 \rightarrow MnO_2 + 2H_2O$

READY?

$$e^{3+} + 2H_20$$
 (4) $Mn^{2+} + 2H_2O_2$

Sol. 1

$$2NaOCl + H_2O_2 \longrightarrow 2NaCl + H_2O + O_2$$

 H_2O_2 acts as reducing agent.





45. Adding surfactants in non polar solvent, the micelles structure will look like



Sol. 1

Non polar end will be towards non polar solvent

46. The correct order of melting points of dichlorobenzenes is



Sol.



47. The correct order of basicity of oxides of vanadium is

ol.	4	
	$(3) V_2 O_3 > V_2 O_5 > V_2 O_4$	$(4) V_2 O_3 > V_2 O_4 > V_2 O_5$
	(1) $V_2O_5 > V_2O_4 > V_2O_3$	(2) $V_2 O_4 > V_2 O_3 > V_2 O_5$

Sol.

Leaser is charge on canter atom more will be the basicity.

Give yourself an extra edge





48. Which of the following artificial sweeteners has the highest sweetness value in comparison to cane sugar ?

(1) Sucralose (2) Aspartame (3) Alitame (4) Saccharin

Sol. 3

Alitame has 2000 has times more sweetner as compare to cane sugar.

49. Which one of the following statements is correct for electrolysis of brine solution?
(1) Cl₂ is formed at cathode
(2) O₂ is formed at cathode
(3) H₂ is formed at anode
(4) OH⁻ is formed at cathode

Sol. 4

Brine solⁿ gives H_2/OH^- at cathode & Cl_2 at anode.

50. Which transition in the hydrogen spectrum would have the same wavelength as the Balmer type transition from n = 4 to n = 2 of He⁺spectrum

E READY?

(1) n = 2 to n = 1 (2) n = 1 to n = 2 (3) n = 3 to n = 4 (4) n = 1 to n = 3

Sol. 1

$$\lambda_{\rm H} = \lambda_{{\rm He}^+}$$

$$R_{\rm H} \times (1)^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right) = R_{\rm H} \times (2)^2 \left(\frac{1}{(2)^2} - \frac{1}{(4)^2} + \frac{1}{(4)^2}\right)^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right) = \left(\frac{4}{4}\right) - \left(\frac{4}{16}\right)^2$$

$$\frac{1}{n_1^2} - \frac{1}{n_2^2} = \frac{1}{1} - \frac{1}{4}$$

$$n_1 = 1 : n_2 = 2 \text{ for H-atom}$$

SECTION B

- **51.** The oxidation state of phosphorus in hypophosphoric acid is +
- **Sol.** Hypophosphoric acid is $H_4P_2O_6$ oxidation state of P is +4.

52. The enthalpy change for the conversion of $\frac{1}{2}$ Cl₂(g) to Cl⁻(aq) is (-) kJmol⁻¹ (Nearest integer)

Given : $\Delta_{dis} H^{\Theta}_{Cl_{2(g)}} = 240 \text{ kJ mol}^{-1}, \Delta_{eg} H^{\Theta}_{Cl_{(g)}} = -350 \text{ kJ mol}^{-1}, \Delta_{hyd} H^{\Theta}_{Cl_{(g)}} = -380 \text{ kJ mol}^{-1}$

Sol. 610

Give yourself an extra edge



The logarithm of equilibrium constant for the reaction $Pd^{2+} + 4Cl^- \rightleftharpoons PdCl_4^{2-}$ is (Nearest integer) 53.

Given : $\frac{2.303 \text{RT}}{\text{F}} = 0.06 \text{ V}$ $Pd^{2+}_{(aq)} + 2e^{-} \rightleftharpoons Pd(s) E^{\ominus} = 0.83 V$ $PdCl_4^{2-}(aq) + 2e^- \rightleftharpoons Pd(s) + 4Cl^-(aq) E^{\theta} = 0.65 V$

Sol. 6

JUI4²⁻ (aq.) $\Delta G^{\circ} = -RT \ell nK$ $-nFE^{\circ}_{cell} = -RT \times 2.303 (log_{10}K)$ Net reaction $\rightarrow Pd^{2+}$ (aq.) + 4Cl⁻ (aq.) $\rightleftharpoons PdCl_{4^{2-}}$ (aq.) $E^{\circ}_{cell} = E^{\circ}_{cathod} - E^{\circ}_{anode}$ $E^{\circ}_{cell} = 0.83 - 0.65$ From equation (1) Also n = 2 $\log K = 6$

On complete combustion, 0.492 g of an organic compound gave 0.792 g of CO_2 . 54. The % of carbon in the organic compound is (Nearest integer)

Sol. 44

44 gm of CO₂ contains 12 g carbon. 0.792 gm of CO₂ contains $\frac{0.792 \times 12}{44}$ g of carbon % of carbon = $\frac{0.216}{0.492} \times 100$ = 43.9% = 44%

55. Zinc reacts with hydrochloric acid to give hydrogen and zinc chloride. The volume of hydrogen gas produced at STP from the reaction of 11.5 g of zinc with excess HCl is L (Nearest integer) (Given : Molar mass of Zn is 65.4 g mol⁻¹ and Molar volume of H_2 at STP = 22.7 L) 4

 $Zn + 2HCl \longrightarrow ZnCl_2 + H_2$ No. of moles of $Zn = \frac{11.5}{65.3}$ = No. of moles of H₂ No. of H₂ liberated = 0.176×22.7 Lt. = 3.99 L = 4 Lt.





56. $A \rightarrow B$

> The rate constants of the above reaction at 200 K and 300 K are 0.03 min⁻¹ and 0.05 min⁻¹ respectively. The activation energy for the reaction is I (Nearest integer) (Given : $\ln 10 = 2.3$ $R = 8.3 \ J \ K^{-1} \ mol^{-1}$ $\log 5 = 0.70$

- $\log 3 = 0.48$
 - $\log 2 = 0.30$)

Sol. 2520

In
$$\left(\frac{K_2}{K_1}\right) = \frac{Ea}{R} \left[\frac{1}{T_1} - \frac{1}{T_2}\right]$$

Log $\left(\frac{0.05}{0.03}\right) = \frac{Ea}{2.3 \times 8.3} \left[\frac{1}{200} - \frac{1}{300}\right]$
 $\left[0.70 - 0.48\right] = \frac{Ea}{2.3 \times 8.3} \left[\frac{300 - 200}{300 \times 200}\right]$
 $0.22 = \frac{Ea}{2.3 \times 8.3} \left[\frac{1}{600}\right]$
Ea = 0.22 × 2.3 × 8.3 × 600
= 2519.88 J
 ≈ 2520

For reaction: $SO_2(g) + \frac{1}{2}O_2(g) \rightleftharpoons SO_3(g)$ 57. $K_p = 2 \times 10^{12}$ at 27°C and 1 atm pressure. The K_c for the same reaction is $\times 10^{13}$. (Nearest integer) (Given R = 0.082 L atm $K^{-1} \text{ mol}^{-1}$) Sol.

 $K_{C} = 1 \times 10^{13}$ $SO_2(g) + \frac{1}{2}O_2 \rightleftharpoons SO_3(g)$ $\Delta n = \frac{-1}{2}$

 $K_P = 2 \times 10^{12}$ $K_P = K_C (RT) \Delta^{ng}$ P = 1 atm $2 \times 10^{12} = K_C (0.082 \times 300)^{-1/2}$ $T = 27^{\circ}C$ $K_C = 1 \times 10^{13}$

58. The total pressure of a mixture of non-reacting gases X(0.6 g) and Y(0.45 g) in a vessel is 740 mm of Hg. The partial pressure of the gas X is mm of Hg. (Nearest Integer)

(Given : molar mass X = 20 and Y = 45 g mol⁻¹)

Sol. 555

Number of moles of gas $X = \frac{0.6}{20} = 0.03$

Number of moles of gas $Y = \frac{0.45}{45} = 0.01$

Total number of moles = 0.03 + 0.01 = 0.04 mole Partial pressure of gas X = Mole fraction \times Total pressure 0.03

$$=\frac{0.05}{0.04} \times 740 = 555$$







59. How many of the transformations given below would result in aromatic amines ?

(2) In Gabriel phthalimide synthesis chloro-benzene is poor substrok for $\rm S_{N_2}$, Hence reaction will not observed.



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60. At 27°C, a solution containing 2.5 g of solute in 250.0 mL of solution exerts an osmotic pressure of 400 Pa. The molar mass of the solute is $gmol^{-1}$ (Nearest integer) (Given : $R = 0.083 L_{bar} K^{-1} mol^{-1}$)

Sol. 62250

 $\pi = CRT$ $\frac{400Pa}{10^5} = \frac{\frac{2.5g}{M_{\circ}}}{250/1000} \times 0.083 \frac{L - bar}{Kmol} \times 300 K$ $M_{\circ} = 62250$





SECTION - A

61. If the maximum distance of normal to the ellipse $\frac{x^2}{4} + \frac{y^2}{b^2} = 1, b < 2$, from the origin is 1, then the eccentricity of the ellipse is :

(1) $\frac{1}{2}$ (2) $\frac{\sqrt{3}}{4}$ (3) $\frac{\sqrt{3}}{2}$ (4) $\frac{1}{\sqrt{2}}$

Sol.

Normal to the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ at point (a cos θ , b sin θ) is $\frac{ax}{\cos\theta} - \frac{by}{\sin\theta} = a^2 - b^2$

Its distance from origin is

$$d = \frac{|a^2 - b^2|}{\sqrt{a^2 \sec^2 \theta + b^2 \csc^2 \theta}}$$

$$d = \frac{|a^2 - b^2|}{\sqrt{a^2 + b^2 + 2ab + (a \tan \theta - b \cot \theta)^2}}$$

$$d \frac{|(a - b)(a + b)|}{\sqrt{a^2 + b^2 + 2ab + (a \tan \theta - b \tan \theta)^2}}$$

$$d_{max} = \frac{|(a - b)(a + b)|}{a + b} = |a - b|$$

$$\therefore d_{max} = 1$$

$$|2 - b| = 1$$

$$2 - b = 1 [\because b < 2]$$

$$\boxed{b=1}$$
Eccentricity = $\sqrt{1 - \frac{b^2}{a^2}} = \sqrt{1 - \frac{1}{4}} = \frac{\sqrt{3}}{2}$

$$\Rightarrow \boxed{e = \frac{\sqrt{3}}{2}}$$

62. Let a differentiable function f satisfy $f(x) + \int_{3}^{x} \frac{f(t)}{t} dt = \sqrt{x+1}, x \ge 3$. Then 12f(8) is equal to : (1) 34 (2) 1 (3) 17 (4) 19

Sol.

$$f(x) + \int_{3}^{x} \frac{f(t)}{t} dt = \sqrt{x+1}, \ x \ge 3$$

Differentiate both side w.r.t. x

$$f^{1}(x) + \frac{f(x)}{x} = \frac{1}{2\sqrt{x+1}}$$

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Above eqn. is linear differential equation

I.f.
$$= e^{\int_{x}^{1} dx} = e^{\ln x} = x$$

Solution is
 $f(x) \cdot x = \int \frac{x}{2\sqrt{x+1}} dx + C$
 $f(x) \cdot x = \frac{1}{2} \int \left(\frac{x+1}{\sqrt{x+1}} - \frac{1}{\sqrt{x+1}}\right) dx + C$
 $f(x) \cdot x = \frac{1}{2} \int \left(\sqrt{x+1} - \frac{1}{\sqrt{x+1}}\right) dx + C$
 $f(x) \cdot x = \frac{1}{2} \left[\frac{2}{3}(x+1)^{\frac{3}{2}} - 2\sqrt{x+1}\right] + C$

:: f(3) = 2

than

$$2.3 = \frac{1}{2} \left[\frac{2}{3} \times 8 - 2 \times 2 \right] + C$$

$$6 = \frac{1}{2} \left[\frac{16}{3} - 4 \right] + C$$

$$6 = \frac{2}{3} + C$$

$$\boxed{C = \frac{16}{3}}$$

$$f(x). x = \frac{1}{2} \left[\frac{2}{3} (x+1)^{\frac{3}{2}} - 2\sqrt{x+1} \right] + \frac{16}{3}$$

Put x = 8

$$f(8) \cdot 8 = \frac{1}{2} \left[\frac{2}{3} \times 27 - 2 \times 3 \right] + \frac{16}{3}$$

$$f(8) \cdot 8 = \frac{1}{2} \left[12 \right] + \frac{16}{3}$$

$$f(8) \cdot 8 = 6 + \frac{16}{3} = \frac{34}{3}$$

$$\boxed{12f(8) = 17}$$

63. For all z ∈ C on the curve C₁: |z| = 4, let the locus of the point z + ¹/_z be the curve C₂. Then :
(1) the curve C₁ lies inside C₂
(2) the curve C₂ lies inside C₁
(3) the curves C₁ and C₂ intersect at 4 points (4) the curves C₁ and C₂ intersect at 2 points

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JEE READY?



Sol.

$$C_{1} : |z| = 4 \text{ then } z\overline{z} = 16$$

$$z + \frac{1}{z} = z + \frac{\overline{z}}{16}$$

$$= x + iy + \frac{x - iy}{16}$$

$$z + \frac{1}{z} = \frac{17x}{16} + i\frac{15y}{16}$$
Let $X = \frac{17x}{16}, \quad Y = \frac{15}{16}y$

$$\frac{X}{(\frac{17}{16})} = x, \quad \frac{Y}{(\frac{15}{16})} = y$$

$$\therefore x^{2} + y^{2} = 16$$

$$\frac{X^{2}}{(\frac{17}{16})^{2}} + \frac{Y^{2}}{(\frac{15}{16})^{2}} = 16$$

$$\Rightarrow C_{2} : \frac{x^{2}}{(\frac{17}{4})^{2}} + \frac{y^{2}}{(\frac{15}{4})^{2}} = 1 \quad \text{(Ellipse)}$$

$$x^{2} + y^{2} = 16$$

Curve C_1 and C_2 intersect at 4 point.

64.
$$y = f(x) = \sin^3 \left(\frac{\pi}{3} \left(\cos \left(\frac{\pi}{3\sqrt{2}} (-4x^3 + 5x^2 + 1)^{\frac{3}{2}} \right) \right) \right)$$
. Then, at $x = 1$,
(1) $\sqrt{2}y' - 3\pi^2 y = 0$ (2) $y' + 3\pi^2 y = 0$ (3) $2y' + 3\pi^2 y = 0$ (4) $2y' + \sqrt{3}\pi^2 y = 0$

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Sol.

$$y = f(x) = \sin^{3} \left(\frac{\pi}{3} \left(\cos \left(\frac{\pi}{3\sqrt{2}} \left(-4x^{3} + 5x^{2} + 1 \right)^{\frac{3}{2}} \right) \right) \right)$$

Let $g(x) = \frac{\pi}{3\sqrt{2}} \left(-4x^{3} + 5x^{2} + 1 \right)^{\frac{3}{2}}$
 $g(1) = \frac{2\pi}{3}$
 $y = \sin^{3} \left(\frac{\pi}{3} \cos(g(x)) \right)$
Differentiate w.r.t. x
 $y' = 3\sin^{2} \left(\frac{\pi}{3} \cos(g(x)) \right) \times \cos \left(\frac{\pi}{3} \cos(g(x)) \right) \times \frac{\pi}{3} \left(-\sin g(x) \right) g'(x)$
 $\therefore g^{1}(x) = \frac{\pi}{3\sqrt{2}} \left(-4x^{3} + 5x^{2} + 1 \right)^{\frac{1}{2}} \left(-12x^{2} + 10x \right)$
 $g^{1}(1) = \frac{\pi}{2\sqrt{2}} \left(\sqrt{2} \right) (-2) = -\pi$
 $y^{1}(1) = \frac{3}{4} \times \frac{\sqrt{3}}{2} \times \frac{\pi}{3} \left(-\frac{\sqrt{3}}{2} \right) (-\pi) = \frac{3\pi^{2}}{16}$
 $y(1) = \sin^{3} \left(\frac{\pi}{3} \cos \frac{2\pi}{3} \right) = \frac{-1}{8}$
 $2y^{1}(1) + 3\pi^{2}y(1) = 0$

65. A wire of length 20 m is to be cut into two pieces. A piece of length l_1 is bent to make a square of area A_1 and the other piece of length l_2 is made into a circle of area A_2 . If $2A_1 + 3A_2$ is minimum then $(\pi l_1): l_2$ is equal to :

$$(1) 1:6 (2) 6:1 (3) 3:1 (4) 4:1$$

Sol.

Total length of wire = 20 m area of square (A₁) = $\left(\frac{\ell_1}{4}\right)^2$ area of circle (A₂) = $\pi \left(\frac{\ell_2}{2\pi}\right)^2$ Let S = 2A₁ + 3A₂

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 $S = \frac{\ell_1^2}{8} + \frac{3\ell_2^2}{4\pi}$ $\because \ \ell_1 + \ell_2 = 20 \text{ then}$ $1 + \frac{d\ell_2}{d\ell_1} = 0$ $\frac{d\ell_2}{d\ell_1} = -1$ $\frac{ds}{d\ell_1} = \frac{\ell_1}{4} + \frac{6\ell_2}{4\pi} \cdot \frac{d\ell_2}{d\ell_1} = 0$ $= \frac{\ell_1}{4} = \frac{6\ell_2}{4\pi}$ $= \frac{\pi\ell_1}{\ell_2} = \frac{6}{1}$

66. Let a circle C_1 be obtained on rolling the circle $x^2 + y^2 - 4x - 6y + 11 = 0$ upwards 4 units on the tangent T to it at the point (3,2). Let C_2 be the image of C_1 in T. Let A and B be the centers of circles C_1 and C_2 respectively, and M and N be respectively the feet of perpendiculars drawn from A and B on the x-axis. Then the area of the trapezium AMNB is :

(1)
$$4(1 + \sqrt{2})$$
 (2) $3 + 2\sqrt{2}$ (3) $2(1 + \sqrt{2})$ (4) $2(2 + \sqrt{2})$

Sol.



(x', y') point lies on line y = x - 1 have distance 4 unit from (3, 2).

$$x' = \frac{4}{\sqrt{2}} + 3 = 2\sqrt{2} + 3$$
$$y' = \frac{4}{\sqrt{2}} + 2 = 2\sqrt{2} + 2$$

Slope of line AB is –1.

i.e. =
$$\tan \theta = -1$$
 then $\sin \theta = \frac{1}{\sqrt{2}}$, $\cos \theta = -\frac{1}{\sqrt{2}}$

for point A and B

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$$\mathbf{x} = \pm \sqrt{2} \left(\frac{-1}{\sqrt{2}} \right) + \left(2\sqrt{2} + 3 \right)$$
$$\mathbf{y} = \pm \sqrt{2} \left(\frac{1}{\sqrt{2}} \right) + \left(2\sqrt{2} + 2 \right)$$

for point A we take +ve sign

$$(x_2, y_2) = (2\sqrt{2}+2, 2\sqrt{2}+3)$$

 $(x_1, y_1) = (2\sqrt{2} + 4, 2\sqrt{2} + 1)$ $MN = |x_2 - x_1| = 2$ $AM + BN = 2\sqrt{2} + 3 + 2\sqrt{2} + 1 = 4 + 4\sqrt{2}$ area of trapezium = $\frac{1}{2} \times 2 \times (4 + 4\sqrt{2})$ $= 4(1+\sqrt{2})$

 $(2)^{5}$

A bag contains 6 balls. Two balls are drawn from it at random and both are found to be black. The **67.** probability that the bag contains at least 5 black balls is $(3)\frac{5}{6}$ (4) $\frac{2}{7}$

(1)
$$\frac{3}{7}$$
 (2) $\frac{5}{7}$
Sol. Probability = $\frac{{}^{3}C_{2} + {}^{6}C_{2}}{{}^{2}C_{2} + {}^{3}C_{2} + {}^{4}C_{2} + {}^{5}C_{2} + {}^{6}C_{2}}$
= $\frac{10 + 15}{1 + 3 + 6 + 10 + 15}$
= $\frac{5}{7}$

Let y = f(x) represent a parabola with focus $\left(-\frac{1}{2}, 0\right)$ and directrix $y = -\frac{1}{2}$. **68**. Then $S = \left\{ x \in \mathbb{R} : \tan^{-1}(\sqrt{f(x)}) + \sin^{-1}(\sqrt{f(x)} + 1) = \frac{\pi}{2} \right\}$:

(2) contains exactly one element (1) contains exactly two elements (4) is an infinite set (3) is an empty set

equation of parabola which have focus $\left(-\frac{1}{2}, 0\right)$ and directrix $y = -\frac{1}{2}$ is Sol.

 $\left(x+\frac{1}{2}\right)^2 = \left(y+\frac{1}{4}\right)$ $y = f(x) = (x^2 + x)$

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$$\therefore S = \left\{ x \in R : \tan^{-1} \left(\left(\sqrt{f(x)} \right) + \sin^{-1} \left(\sqrt{f(x) + 1} \right) = \frac{\pi}{2} \right) \right\}$$

$$\tan^{-1} \left(\sqrt{f(x)} \right) + \sin^{-1} \left(\sqrt{f(x) + 1} \right) = \frac{\pi}{2}$$

$$f(x) \ge 0 & \sqrt{f(x) + 1} \text{ can not greater then 1, so } f(x) \text{ must be } 0$$

i.e. $f(x) = 0$
$$\Rightarrow x^2 + x = 0$$

$$x(x+1) = 0$$

$$x = 0, x = -1$$

S contain 2 element.

69. Let a = 2î + ĵ + k̂, and b and c be two nonzero vectors such that |a + b + c| = |a + b - c| and b · c = 0. Consider the following two statements:
(A) |a + λc| ≥ |a| for all λ ∈ ℝ.
(B) a and c are always parallel. Then.

- (1) both (A) and (B) are correct
- (3) neither (A) nor (B) is correct

(2) only (A) is correct(4) only (B) is correct

Sol.

$$\begin{aligned} \left| \vec{a} + \vec{b} + \vec{c} \right| &= \left| \vec{a} + \vec{b} - \vec{c} \right|, \ \vec{b}.\vec{c} = 0 \\ \left| \vec{a} + \vec{b} + \vec{c} \right|^2 &= \left| \vec{a} + \vec{b} - \vec{c} \right|^2 \\ \left| \vec{a} \right|^2 + \left| \vec{b} \right|^2 + \left| \vec{c} \right|^2 + 2\vec{a}.\vec{b} + 2\vec{b}.\vec{c} + 2\vec{a}.\vec{c} \\ &= \left| \vec{a} \right|^2 + \left| \vec{b} \right|^2 + \left| \vec{c} \right|^2 + 2\vec{a}.\vec{b} - 2\vec{b}.\vec{c} - 2\vec{a}.\vec{c} \\ 2\vec{a}.\vec{b} + 2\vec{b}.\vec{c} + 2\vec{a}.\vec{c} = 2\vec{a}.\vec{b} - 2\vec{b}.\vec{c} - 2\vec{a}.\vec{c} \\ \vec{a}.\vec{b} + \vec{a}.\vec{c} = \vec{a}.\vec{b} - \vec{a}.\vec{c} \\ \vec{a}.\vec{c} = 0 \quad (B \text{ is incorrect}) \\ &\qquad \left| \vec{a} + \lambda \vec{c} \right|^2 \ge \left| \vec{a} \right|^2 \\ &\qquad \left| \vec{a} \right|^2 + \lambda^2 \left| \vec{c} \right|^2 + 2\lambda \vec{a} \cdot \vec{c} \ge \left| \vec{a} \right|^2 \\ &= \lambda^2 c^2 \ge 0 \\ \text{True } \forall \lambda \in \mathbb{R} \quad (A \text{ is correct}) \end{aligned}$$





70. The value of
$$\int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{(2+3\sin x)}{\sin x (1+\cos x)} dx$$
 is equal to
(1) $\frac{10}{3} - \sqrt{3} - \log_e \sqrt{3}$ (2) $\frac{2}{2} - \sqrt{3} - \log_e \sqrt{3}$
(3) $-2 + 3\sqrt{3} + \log_e \sqrt{3}$ (4) $\frac{10}{3} - \sqrt{3} + \log_e \sqrt{3}$
(4) $\int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{(2+3\sin x)}{\sin x (1+\cos x)} dx$
 $= \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{2}{\sin x + \sin x \cos x} dx + \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{3}{1+\cos x} dx$
 $= I_1 + I_2$
 $I_1 = \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{2dx}{\sin x (1+\cos x)} = 2 \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{(1+\tan^2 \frac{x}{2})dx}{2\tan \frac{x}{2} \times \left[1 + \tan^2 \frac{x}{2}\right]} dx}$
 $= 2 \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{(1+\tan^2 \frac{x}{2})(1+\tan^2 \frac{x}{2})dx}{2\tan \frac{x}{2} \times 2}$
 $= 2 \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{\sec^2 \frac{x}{2}(1+\tan^2 \frac{x}{2})}{4\tan \frac{x}{2}} dx$
Let, $\tan \frac{x}{2} = t$ then $\sec^2 \frac{x}{2} \times \frac{1}{2} dx = dt$
 $= 2 \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{1+t^2}{2t} dt$
 $= \left[\ell nt + \frac{t^2}{2} \right]_{\frac{1}{\sqrt{3}}}^{\frac{1}{3}} \frac{1}{\sqrt{3}}$
 $I_1 = \left[(n\sqrt{3} + \frac{1}{3} \right]$
 $I_2 = 3 \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{dx}{1+\cos x} = 3 \int_{\frac{\pi}{3}}^{\frac{\pi}{3}} \frac{1-\cos x}{3} dx$

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$$I_{2} = 3\left[\cos \exp - \cot x\right]_{\frac{\pi}{3}}^{\frac{\pi}{2}} = 3 - \sqrt{3}$$
$$I_{1} + I_{2} = \ln\sqrt{3} + \frac{1}{3} + 3 - \sqrt{3}$$
$$= \frac{10}{3} + \ln\sqrt{3} - \sqrt{3}$$

Let the shortest distance between the lines $L: \frac{x-5}{-2} = \frac{y-\lambda}{0} = \frac{z+\lambda}{1}$, $\lambda \ge 0$ and 71. $L_1: x + 1 = y - 1 = 4 - z$ be $2\sqrt{6}$. If (α, β, γ) lies on L, then which of the following is NOT possible ? (3) $2\alpha - \gamma = 9$ (1) $\alpha - 2\gamma = 19$ (2) $2\alpha + \gamma = 7$ (4) $\alpha + 2\gamma = 24$ Sol. (4) $\vec{b}_1 = <-2, 0, 1 > \vec{a}_1 = (5, \lambda, -\lambda)$ Let $\vec{b}_2 = <1, 1, -1 > \vec{a}_2 = (-1, 1, 4)$ $b_2 = <1, 1, -1 < a_2$ Normal vector of both line is $\vec{b}_1 \times \vec{b}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -2 & 0 & 1 \\ 1 & 1 & -1 \end{vmatrix}$ JEE READY? $\hat{i}(-1) - \hat{j}(1) + \hat{k}(-2)$ $\vec{b}_1 \times \vec{b}_2 = <-1, -1, -2>$ $\vec{a}_{1} - \vec{a}_{2} = <6, \lambda - 1, -\lambda - 4 >$ Shortest distance d = $\left| \frac{(\vec{a}_{2} - \vec{a}_{1}) \times (\vec{b}_{1} \times \vec{b}_{2})}{|\vec{b}_{1} \times \vec{b}_{2}|} \right|$ $2\sqrt{6} = \left| \frac{<6, \lambda - 1, -\lambda - 4 > \times <-1, -1, -2 >}{\sqrt{(1)^{2} + (1)^{2} + (2)^{2}}} \right|$

$$12 = |-6 - \lambda + 1 + 2\lambda + 8|$$
$$|\lambda + 3| = 12$$
$$\lambda = 9, -15$$
$$\lambda = 9(\because \lambda \ge 0)$$

 \therefore (α , β , γ) lies on line L then

$$\frac{\alpha-5}{-2} = \frac{\beta-9}{0} = \frac{\gamma+9}{1} = K$$

$$\alpha = 5 - 2K, \ \beta = 9K, \ \gamma = -9 + K$$

$$\alpha + 2\gamma, = 5 - 2K - 18 + 2K = -13 \neq 24$$

Therefore $\alpha + 2\gamma = 24$ is not possible.



72. For the system of linear equations

x + y + z = 6

 $\alpha x + \beta y + 7z = 3$

x + 2y + 3z = 14

which of the following is NOT true ?

(1) If $\alpha = \beta$ and $\alpha \neq 7$, then the system has a unique solution

(2) If $\alpha = \beta = 7$, then the system has no solution

(3) For every point $(\alpha, \beta) \neq (7,7)$ on the line x - 2y + 7 = 0, the system has infinitely many solutions

(4) There is a unique point (α, β) on the line x + 2y + 18 = 0 for which the system has infinitely many solutions

Sol. (3)

... (1) x + y + z = 6 $\alpha x + \beta y + 7z = 3$... (2) x + 2y + 3z = 14 ... (3) equation (3) – equation (1)JEE READY? y + 2z = 8y = 8 - 2zFrom (1) x = -2 + zValue of x and y put in equation (2) $\alpha(-2 + z) + \beta(8 - 2z) + 7z = 3$ $-2\alpha + \alpha z + 8\beta - 2\beta z + 7z = 3$ $(\alpha - 2\beta + 7) z = 2\alpha - 8\beta + 3$ if $\alpha - 2\beta + 7 \neq 0$ then system has unique solution if $(\alpha - 2\beta + 7 = 0)$ and $2\alpha - 8\beta + 3 \neq 0$ then system has no solution if $(\alpha - 2\beta + 7 = 0)$ and $2\alpha - 8\beta + 3 = 0$ then system has infinite solution

73. If the domain of the function $f(x) = \frac{[x]}{1+x^2}$, where [x] is greatest integer $\leq x$, is [2,6), then its range is

$$(1) \left(\frac{5}{26}, \frac{2}{5}\right] \qquad (2) \left(\frac{5}{37}, \frac{2}{5}\right] - \left\{\frac{9}{29}, \frac{27}{109}, \frac{18}{89}, \frac{9}{53}\right\} \\ (3) \left(\frac{5}{37}, \frac{2}{5}\right] \qquad (4) \left(\frac{5}{26}, \frac{2}{5}\right] - \left\{\frac{9}{29}, \frac{27}{109}, \frac{18}{89}, \frac{9}{53}\right\}$$

Sol. (3)

$$f(x) = \frac{[x]}{1 + x^2}, \qquad x = \in [2, \, 6]$$

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$$f(x) = \begin{cases} \frac{2}{1+x^2} & x \in [2,3) \\ \frac{3}{1+x^2} & x \in [3,4) \\ \frac{4}{1+x^2} & x \in [4,5) \\ \frac{5}{1+x^2} & x \in [5,6) \end{cases}$$

 $\therefore f(\mathbf{x})$ is \downarrow in $\mathbf{x} \in [2, 6)$



74. Let R be a relation on N×N defined by (a, b)R(c, d) if and only if ad(b - c) = bc(a - d). Then R is (1) transitive but neither reflexive nor symmetric

- (2) symmetric but neither reflexive nor transitive
- (3) symmetric and transitive but not reflexive
- (4) reflexive and symmetric but not transitive

Sol. (2)

 $(a, b) R (c, d) \Leftrightarrow ad(b - c) = bc(a - d)$ For reflexive (a, b) R (a, b) $\Rightarrow ab (b - a) \neq ba(a - b)$ R is not reflexive For symmetric: $(a,b) R(c,d) \Rightarrow ad(b - c) = bc (a - d)$ then we check $(c, d) R (a, b) \Rightarrow cb(d - a) = ad(c - b)$ $\Rightarrow cb(a - d) = ad(b - c)$ R is symmetric : For transitive:

 \therefore (2,3) R (3,2) and (3,2) R (5,30)

But (2,3) is not related to (5,30) R is not transitive.





75.	5. $(S1)(p \Rightarrow q) \lor (p \land (\sim q))$ is a tautology							
	(S2)	$(S2)((\sim p) \Rightarrow (\sim q)) \land ((\sim p) \lor q)$ is a contradiction.						
	Ther	Then						
	(1) b	oth (S1)) and (S2	2) are	correct	(2) only (S1) is correct		
	(3) o	nly (S2)) is corre	ct		(4) both (S1) and (S2) are wrong		
Sol.	(2)							
	S ₁ : ($(\mathbf{P} \Rightarrow \mathbf{q})$	V (P ∧	(~q))				
	Р	q	P⇒q	$\sim q$	РЛ~q	$(P \Rightarrow q) V (P \land \sim q)$		
	Т	Т	Т	F	F	Т		
	Т	F	F	Т	Т	Т		
	F	Т	Т	F	F	Т		
	F	F	Т	Т	F	Т		
	S_1 is	a tautol	ogy					
	S ₂ : ($((\sim P) \Rightarrow$	(~q)) Λ	((~P)	Vq)			
	~P	$\sim q$	~P⇒~	~q	~P v q	$((\sim P) \Rightarrow (\sim q)) \land (\sim P) vq)$		
	F	F	Т		Т	Т		
	F	Т	Т		F	F		
	Т	F	F		Т	F		
	Т	Т	Т		Т	Т		
	S ₂ is	not a co	ontradict	ion				

76. If the sum and product of four positive consecutive terms of a G.P., are 126 and 1296, respectively, then the sum of common ratios of all such GPs is

(1) 7 (2) 3 (3)
$$\frac{9}{2}$$
 (4) 14

Four term of G.P.
$$\frac{a}{r^3}, \frac{a}{r}, ar, ar^3$$

 $\frac{a}{r^3} + \frac{a}{r} + ar + ar^3 = 126$
 $\frac{a}{r^3} \cdot \frac{a}{r} \cdot ar \cdot ar^3 = 1296$
 $a^4 = 1296$
 $a = 6$
 $\frac{6}{r^3} + \frac{6}{r} + 6r + 6r^3 = 126$

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77.

$$\left(r + \frac{1}{r}\right) + r^{3} + \frac{1}{r^{3}} = 21$$

$$\left(r + \frac{1}{r}\right) + \left(r + \frac{1}{r}\right)^{3} - 3\left(r + \frac{1}{r}\right) = 21$$
Let $r + \frac{1}{r} = t$

$$t^{3} - 2t = 21$$

$$\Rightarrow t = 3$$

$$r + \frac{1}{r} = 3$$

$$r^{2} - 3r + 1 = 0$$

$$r = \frac{3 \pm \sqrt{5}}{2}$$
Sum of common ratio $= \frac{9}{4} + \frac{5}{4} + \frac{3\sqrt{5}}{2} + \frac{9}{4} + \frac{5}{4} - \frac{3\sqrt{5}}{2}$

$$= 7$$
77. Let $A - \left(\begin{matrix} 1 & 0 & 0 \\ 0 & 4 & -1 \\ 0 & 12 & -3 \end{matrix}\right)$. Then the sum of the diagonal elements of the matrix $(A + I)^{11}$ is equal to
$$(1) 6144 \qquad (2) 2050 \qquad (3) 4097 \qquad (4) 4094$$
Sol. (3)
$$A = \left[\begin{matrix} 1 & 0 & 0 \\ 0 & 4 & -1 \\ 0 & 12 & -3 \end{matrix}\right]$$

$$A^{2} = \left[\begin{matrix} 1 & 0 & 0 \\ 0 & 4 & -1 \\ 0 & 12 & -3 \end{matrix}\right] = \left[\begin{matrix} 1 & 0 & 0 \\ 0 & 4 & -1 \\ 0 & 12 & -3 \end{matrix}\right]$$

$$A^{3} = A^{4} = A^{5} \dots = A$$

$$(A + I)^{11} = ^{11}C_{4}A^{11} + ^{11}C_{7}A^{11} + ^{11}C_{2}A^{5} + \dots ^{11}C_{11}I$$

$$= (^{11}C_{6} + ^{11}C_{7} + ^{11}C_{7} + ^{11}C_{7}A^{11} + ^{11}C_{12}A^{5} + \dots ^{11}C_{11}I$$

$$= (^{11}C_{6} + ^{11}C_{7} + ^{11}C_{7} + ^{11}C_{7}A^{11} + ^{11}C_{12}A^{5} + \dots ^{11}C_{11}I$$

$$= (^{11}C_{6} + ^{11}C_{7} + ^{11}C_{7} + \dots ^{11}C_{10}) A + I$$

$$= 2047 A + I$$
Sum of diagonal element $- 2047(1 + 4 - 3) + 3$

$$= 4097$$

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78. The number of real roots of the equation $\sqrt{x^2 - 4x + 3} + \sqrt{x^2 - 9} = \sqrt{4x^2 - 14x + 6}$, is : (1) 3 (2) 1 (3) 2 (4) 0

(2)

$$\sqrt{x^{2} - 4x + 3} + \sqrt{x^{2} - 9} = \sqrt{4x^{2} - 14x + 6}$$

$$\sqrt{(x - 3)(x - 1)} + \sqrt{(x - 3)(x + 3)} = \sqrt{4x^{2} - 12x - 2x + 6}$$

$$\Rightarrow \sqrt{x - 3} (\sqrt{x - 1} + \sqrt{x + 3}) = \sqrt{4x(x - 3) - 2(x - 3)}$$

$$\Rightarrow \sqrt{x - 3} (\sqrt{x - 1} + \sqrt{x + 3}) = \sqrt{(4x - 2)(x - 3)}$$

$$\Rightarrow \sqrt{x - 3} (\sqrt{x - 1} + \sqrt{x + 3}) = \sqrt{2(2x - 1)}) = 0$$

$$\sqrt{x - 3} = 0 \text{ or } \sqrt{x - 1} + \sqrt{x + 3} - \sqrt{2(2x - 1)}) = 0$$

$$x = 3 \text{ or } \sqrt{x - 1} + \sqrt{x + 3} = \sqrt{2(2x - 1)}$$

$$x - 1 + x + 3 + 2\sqrt{(x - 1)(x + 3)} = 4x - 2$$

$$\Rightarrow 2\sqrt{(x - 1)(x + 3)} = 2x - 4$$

$$\Rightarrow (x - 1)(x + 3) = (x - 2)^{2}$$

$$\Rightarrow x^{2} + 2x - 3 = x^{2} + 4 - 4x$$

$$\Rightarrow 6x = 7$$

$$x = \frac{7}{6} \text{ (not possible)}$$

Number of real root = 1

79. If
$$\sin^{-1}\frac{\alpha}{17} + \cos^{-1}\frac{4}{5} - \tan^{-1}\frac{77}{36} = 0, 0 < \alpha < 13$$
, then $\sin^{-1}(\sin \alpha) + \cos^{-1}(\cos \alpha)$ is equal to
(1) 16 (2) 0 (3) π (4) 16 - 5 π

Sol. (3)

$$\sin^{-1}\frac{\alpha}{17} + \cos^{-1}\frac{4}{5} - \tan^{-1}\frac{77}{36} = 0, \ 0 < \alpha < 13$$
$$\sin^{-1}\frac{\alpha}{17} = \tan^{-1}\frac{77}{36} - \tan^{-1}\frac{3}{4}$$
$$= \tan^{-1}\left(\frac{\frac{77}{36} - \frac{3}{4}}{1 + \frac{77}{36} \cdot \frac{3}{4}}\right)$$

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$$\sin^{-1}\frac{\alpha}{17} = \tan^{-1}\left(\frac{8}{15}\right) = \sin^{-1}\left(\frac{8}{17}\right)$$
$$\frac{\alpha}{17} = \frac{8}{17}$$
$$\alpha = 8$$
$$\sin^{-1}(\sin 8) + \cos^{-1}(\cos 8)$$
$$= 3\pi - 8 + 8 - 2\pi$$
$$= \pi$$

80. Let
$$\alpha \in (0,1)$$
 and $\beta = \log_e(1-\alpha)$. Let $P_n(x) = x + \frac{x^2}{2} + \frac{x^3}{3} + \dots + \frac{x^n}{n}, x \in (0,1)$.
Then the integral $\int_0^{\alpha} \frac{t^{50}}{1-t} dt$ is equal to
(1) $\beta + P_{50}(\alpha)$ (2) $P_{50}(\alpha) - \beta$ (3) $\beta - P_{50}(\alpha)$ (4)- $(\beta + P_{50}(\alpha))$
Sol. 4
 $\alpha \in (0,1), \beta = \log_e(1-\alpha)$
 $P_n(x) = x + \frac{x^2}{2} + \frac{x^3}{3} + \dots + \frac{x^n}{n}, x \in (0,1)$
 $\int_0^{\alpha} \frac{t^{50} - 1 + 1}{1 - t} dt$

$$-\int_{0}^{\alpha} \frac{1-t^{50}}{1-t} dt + \int_{0}^{\alpha} \frac{1}{1-t} dt$$

$$-\int_{0}^{\alpha} \left(1+t+t^{2}+\dots,t^{49}\right) dt - \left[\ln(1-t)\right]_{0}^{\alpha}$$

$$-\left[t+\frac{t^{2}}{2}+\frac{t^{3}}{3}+\dots,\frac{t^{50}}{50}\right]_{0}^{\alpha} - \ln(1-\alpha)$$

$$-\left[\alpha+\frac{\alpha^{2}}{2}+\frac{\alpha^{3}}{3}+\dots,+\frac{\alpha^{50}}{50}\right] - \ln(1-\alpha)$$

$$-P_{50}(\alpha) - \ln(1-\alpha)$$

$$-(\beta+P_{50}(\alpha))$$

Section : Mathematics Section B

81. Let $\alpha > 0$, be the smallest number such that the expansion of $\left(x^{\frac{2}{3}} + \frac{2}{x^{3}}\right)^{30}$ has a term

 $\beta x^{-\alpha}, \beta \in \mathbb{N}$. Then α is equal to

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Sol. 2

$$T_{r+1} = {}^{30}C_r \left(x^{\frac{2}{3}}\right)^{30-r} \left(\frac{2}{x^3}\right)^4$$

= ${}^{30}C_r 2^r x^{\frac{60-11r}{3}}$
 $\frac{60-11r}{3} < 0$
11 r > 60
r > $\frac{60}{11}$
r = 6
 $T_7 = {}^{30}C_6 2^6 x^{-2}$ then
 $\beta = {}^{30}C_6 \times 2^6 \in \mathbb{N}$
 $\alpha = 2$

82. Let for $x \in \mathbb{R}$,

$$f(x) = \frac{x + |x|}{2}$$
 and $g(x) = \begin{cases} x, & x < 0\\ x^2, & x \ge 0 \end{cases}$

Then area bounded by the curve $y = (f \circ g)(x)$ and the lines y = 0, 2y - x = 15 is equal to Sol. 72 $f(x) = \frac{x + |x|}{2} = \begin{cases} x & x \ge 0 \\ 0 & x < 0 \end{cases}$ $g(x) = \begin{cases} x^2 & x \ge 0 \\ x & x < 0 \end{cases}$

$$f(x) = \frac{x + |x|}{2} = \begin{cases} x & x \ge 0\\ 0 & x < 0 \end{cases}$$

$$g(x) = \begin{cases} x^2 & x \ge 0\\ x & x < 0 \end{cases}$$
Fog(x) = f{g(x)} = \begin{cases} g(x) & g(x) \ge 0\\ 0 & g(x) < 0 \end{cases}
fog(x) =
$$\begin{cases} x^2 & x \ge 0\\ 0 & x < 0 \end{cases}$$
given lines are 2y - x = 15 and y = 0
$$\begin{pmatrix} 0, \frac{15}{2} \end{pmatrix}$$



Area =
$$\int_{0}^{3} \left(\frac{x+15}{2} - x^{2} \right) dx + \frac{1}{2} \times \frac{15}{2} \times 15$$

= $\frac{x^{2}}{4} + \frac{15x}{2} - \frac{x^{3}}{3} \Big]_{0}^{3} + \frac{225}{4}$
= $\frac{9}{4} + \frac{45}{2} - 9 + \frac{225}{4}$
Area = 72

83. Number of 4-digit numbers that are less than or equal to 2800 and either divisible by 3 or by 11, is equal to

710 Sol.

4 digit number which are less then 2800 are 1000 - 2799

Number which are divisible by 3

$$2799 = 1002 + (n-1) 3$$

n = 600

Number which are divisible by 11 in 1000 - 2799

= (Number which are divisible by 11 in 1 - 2799)

JEE READY? - (Number which are divisible by 11 in 1 - 999)

$$= \left\lceil 2799 \right\rceil \left\lceil 999 \right\rceil$$

$$= 254 - 90$$

Number which are divisible by 33 in 1000 - 2799

= (Number which are divisible by 33 in 1 - 2799) – (Number which are divisible by 33 in 1 - 999)

$$= \left[\frac{2799}{33}\right] - \left[\frac{999}{33}\right]$$
$$= 84 - 30 = 54$$

total number =
$$n(3) + n(11) - n(33)$$

$$=600 + 164 - 54 = 710$$

If the variance of the frequency distribution 84.

x_i	2	3	4	5	6	7	8
Frequency f_i	3	6	16	α	9	5	6

is 3, then α is equal to

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5	-		-			
Xi	\mathbf{f}_{i}	$d_i = x_i - 5$	$(f_i d_i)^2$	$f_i d_i$		
2	3	-3	27	-9		
3	6	-2	24	-12		
4	16	-1	16	-16		
5	α	0	0	0		
6	9	1	9	9		
7	5	2	20	10		
8	6	3	54	18		
$\sigma^{2} = \frac{\sum f_{i}d_{i}^{2}}{\sum f_{i}} - \left(\frac{\sum f_{i}d_{i}}{\sum f_{i}}\right)$						
$=\frac{150}{45+\alpha}-0=3$						
$\Rightarrow 150 = 135 + 3\alpha$						
$\Rightarrow 3\alpha = 15$						
=	$\Rightarrow \alpha = 5$					

- Let θ be the angle between the planes $P_1: \vec{r} \cdot (\hat{\iota} + \hat{j} + 2\hat{k}) = 9$ and $P_2: \vec{r} \cdot (2\hat{\iota} \hat{j} + \hat{k}) = 15$. Let L be the line that meets P_2 at the point (4, -2, 5) and makes an angle θ with the normal of P_2 . If α is the 85. angle between L and P_2 , then $(\tan^2 \theta)(\cot^2 \alpha)$ is equal to JU JEE READY?
- Sol.





86. Let 5 digit numbers be constructed using the digits 0,2,3,4,7,9 with repetition allowed, and are arranged in ascending order with serial numbers. Then the serial number of the number 42923 is
Sol. 2997

2	$\overline{6}$	6	$\overline{6}$	$\frac{1}{6} = 1296$
3	$\overline{6}$	6	$\overline{6}$	$\frac{1}{6} = 1296$
4	0	$\overline{6}$	$\overline{6}$	$\frac{1}{6} = 216$
4	2	0	$\overline{6}$	$\frac{1}{6} = 36$
4	2	2	$\overline{6}$	$\frac{1}{6} = 36$
4	2	3	$\overline{6}$	$\frac{1}{6} = 36$
4	2	4	6	$\frac{1}{6} = 36$
4	2	7	$\overline{6}$	$\frac{1}{6} = 36$
4	2	9	0	$\overline{6} = 6$
4	2	9	2	$\underline{0} = 1$
4	2	9	2	<u>2</u> = 1
4	2	9	2	$\underline{3} = \frac{1}{2997}$

87. Let \vec{a} and \vec{b} be two vectors such that $|\vec{a}| = \sqrt{14}$, $|\vec{b}| = \sqrt{6}$ and $|\vec{a} \times \vec{b}| = \sqrt{48}$. Then $(\vec{a} \cdot \vec{b})^2$ is equal to

Sol. 36

$$\begin{vmatrix} \vec{a} \times \vec{b} \end{vmatrix}^2 = |\vec{a}|^2 |\vec{b}|^2 - (\vec{a} \cdot \vec{b})^2$$
$$48 = 14 \times 6 - (\vec{a} \cdot \vec{b})^2$$
$$(\vec{a} \cdot \vec{b})^2 = 84 - 48$$
$$(\vec{a} \cdot \vec{b})^2 = 36$$

88. Let the line $L: \frac{x-1}{2} = \frac{y+1}{-1} = \frac{z-3}{1}$ intersect the plane 2x + y + 3z = 16 at the point *P*. Let the point *Q* be the foot of perpendicular from the point R(1, -1, -3) on the line *L*. If α is the area of triangle *PQR*, then α^2 is equal to

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180 Sol. Point on line L is $(2\lambda + 1, -\lambda - 1, \lambda + 3)$ If above point is intersection point of line L and plane then $2(2\lambda + 1) + (-\lambda - 1) + 3(\lambda + 3) = 16$ $\lambda = 1$ Point P = (3, -2, 4)Dr of QR = $< 2 \lambda, -\lambda, \lambda + 6 >$ Dr of L = < 2, -1, 1 > $4\lambda + \lambda + \lambda + 6 = 0$ $\lambda = -1$ Q = (-1, 0, 2)P(3, -2, 4) $\overrightarrow{QR} \times \overrightarrow{QP} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & -1 & -5 \\ 4 & -2 & 2 \end{vmatrix} = -12\hat{i} - 24\hat{j}$ R(1,-1,-3) $\alpha = \frac{1}{2} \times \sqrt{144 + 576}$ $\alpha^2 = \frac{720}{4} = 180$ $\alpha^2 = 180$

89. Let $a_1, a_2, ..., a_n$ be in A.P. If $a_5 = 2a_7$ and $a_{11} = 18$, then $12\left(\frac{1}{\sqrt{a_{10}} + \sqrt{a_{11}}} + \frac{1}{\sqrt{a_{11}} + \sqrt{a_{12}}} + \dots + \frac{1}{\sqrt{a_{17}} + \sqrt{a_{18}}}\right)$ is equal to Sol. 8

> Given that $a_5 = 2a_7$ $a_1 + 4d = 2(a_1 + 6d)$ $a_1 + 8d = 0$ $a_1 + 10 d = 18$

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$$a_{1} = -72, d = 9$$

$$a_{18} = a_{1} + 17d = -72 + 153 = 81$$

$$a_{10} = a_{1} + 9d = 9$$

$$12\left(\frac{\sqrt{a_{11}} - \sqrt{a_{10}}}{d} + \frac{\sqrt{a_{12}} - \sqrt{a_{11}}}{d} + \dots \frac{\sqrt{a_{18}} - \sqrt{a_{17}}}{d}\right)$$

$$= 12\left(\frac{\sqrt{a_{18}} - \sqrt{a_{10}}}{d}\right)$$

$$= \frac{12 \times (9 - 3)}{9} = 8$$

90. The remainder on dividing 5^{99} by 11 is :

Sol. 9

 $5^{99} = 5^{4} 5^{95}$ $= 625 (5^{5})^{19}$ $= 625 (3125)^{19}$ $= 625(3124 + 1)^{19}$ $= 625(11\lambda + 1)$ $= 11 \lambda \times 625 + 625$ $= 11 \lambda \times 625 + 616 + 9$ $= 11 \times k + 9$ Remainder = 9
Remainder = 9
Remainder = 9