

## FINAL JEE-MAIN EXAMINATION - JUNE, 2022

## (Held On Wednesday 29th June, 2022)

## TIME: 3:00 PM to 06:00 PM

# **PHYSICS**

## **SECTION-A**

A small toy starts moving from the position of rest 1. under a constant acceleration. If it travels a distance of 10m in t s, the distance travelled by the toy in the next t s will be :

(A) 10m	(B) 20m
(C) 30m	(D) 40m

Official Ans. by NTA (C)

**Sol.** u = 0, Say acceleration is a

For t s  $10 = \frac{1}{2}at^2$ For 2t s  $10 + x = \frac{1}{2}a(2t)^2$  $\frac{10+x}{10} = \frac{4}{1}$ x = 30 m

At what temperature a gold ring of diameter 6.230 2. cm be heated so that it can be fitted on a wooden bangle of diameter 6.241 cm? Both the diameters have been measured at room temperature (27°C). (Given: coefficient of linear thermal expansion of

gold  $\alpha_{\rm r} = 1.4 \times 10^{-5} \, {\rm K}^{-1}$ )

(A) 125.7°C (B) 91.7°C (C) 425.7° (D) 152.7°C

**Official Ans. by NTA (D)** 

Sol. 
$$\Delta \ell = 6.241 - 6.230 = 0.011$$
 cm  
 $\Delta \ell = \ell \alpha \Delta \theta$ 

 $0.011 = 6.230 \times 1.4 \times 10^{-5} (\theta - 27)$ 

$$\theta - 27 = \frac{0.011 \times 10^5}{6.230 \times 1.4}$$

 $\theta \approx 153.11$  nearest is 152.7°C.

TEST PAPER WITH SOLUTION

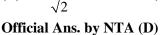
3. Two point charges Q each are placed at a distance d apart. A third point charge q is placed at a distance x from mid-point on the perpendicular bisector. The value of x at which charge q will experience the maximum Coulomb's force is :

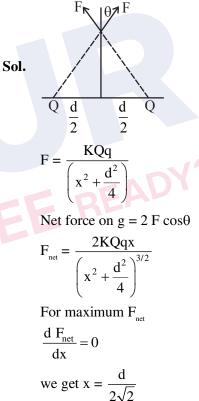
(D)  $x = \frac{d}{2\sqrt{2}}$ 

(A) 
$$x = d$$
 (B)  $x = \frac{d}{2}$ 

(C) 
$$x = \frac{d}{\sqrt{2}}$$







The speed of light in media 'A' and 'B' are 2.0  $\times$ 4.  $10^{10}$  cm/s and  $1.5 \times 10^{10}$  chm/s respectively. A ray of light enters from the medium B to A at an incident angle ' $\theta$ '. If the ray suffers total internal reflection, then

(A) 
$$\theta = \sin^{-1}\left(\frac{3}{4}\right)$$
 (B)  $\theta > \sin^{-1}\left(\frac{2}{3}\right)$   
(C)  $\theta < \sin^{-1}\left(\frac{3}{4}\right)$  (D)  $\theta > \sin^{-1}\left(\frac{3}{4}\right)$ 

**Official Ans. by NTA (D)** 



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Sol. 
$$\sin i_{c} = \frac{n_{r}}{n_{d}} = \frac{C_{d}}{C_{r}} = \frac{1.5 \times 10^{10}}{2 \times 10^{10}}$$
  
 $\sin i_{c} = \frac{3}{4}$   
 $i_{c} = \sin^{-1} \left(\frac{3}{4}\right)$ 

for T I R  $\theta > i_{\alpha}$ 

$$\theta > \sin^{-1}\left(\frac{3}{4}\right)$$

5. In the following nuclear rection,

$$D \xrightarrow{\alpha} D_1 \xrightarrow{\beta} D_2 \xrightarrow{\alpha} D_3 \xrightarrow{\gamma} D_4$$

Mass number of D is 182 and atomic number is 74.Mass number and atomic number of  $D_4$ respectively will be\_\_\_\_.(A) 174 and 71(B) 174 and 69

(C) 172 and 69 (D) 172 and 71 Official Ans. by NTA (A)

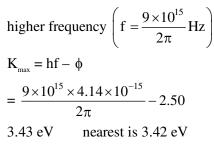
- Sol. Say for  $D_4$  Atomic No = Z Mass Number = A A = 182 - 4 - 4 = 174 Z = 74 - 2 + 1 - 2 = 71
- 6. The electric field at the point associated with a light wave is given by  $E = 200 [\sin(6 \times 10^{15}) t + \sin(9 \times 10^{15}) t] Vm^{-1}$

Given :  $h = 4.14 \times 10^{-15} \text{ eVs}$ 

If this light falls on a metal surface having a work function of 2.50 eV, the maximum kinetic energy of the photoelectrons will be :

Official Ans. by NTA	<b>A</b> ( <b>D</b> )
(C) 3.60 eV	(D) 3.42 eV
(A) 1.90 eV	(B) 3.27 eV

**Sol.** For maximum KE we will take



7. A capacitor is discharging through a resistor R. Consider in time  $t_1$ , the energy stored in the capacitor reduces to half of its initial value and in time  $t_2$ , the charge stored reduces to one eighth of its initial value. The ratio  $t_1/t_2$  will be :

(A) 1/2	(B) 1/3
(C) 1/4	(D) 1/6

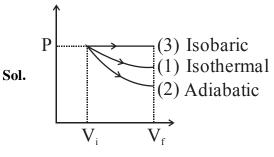
Official Ans. by NTA (D)

Sol. In  $t_1$  time energy becomes half so charge will

become 
$$\frac{1}{\sqrt{2}}$$
 time  
 $q = Q_0 e^{-\frac{t_1}{RC}} = \frac{Q_0}{\sqrt{2}}$   
and  $q = Q_0 e^{-\frac{t_1}{RC}} = \frac{Q_0}{8} = \left(\frac{Q_0}{\sqrt{2}}\right)^6$   
 $t_2 = 6t_1$   
 $\frac{t_1}{t_2} = \frac{1}{6}$ 

8. Starting with the same initial conditions, an ideal gas expands from volume  $V_1$  to  $V_2$  in three different ways. The work done by the gas is  $W_1$  if the process is purely isothermal.  $W_2$ . if the process is purely adiabatic and  $W_3$  if the process is purely isobaric. Then, choose the coned option

(A) 
$$W_1 < W_2 < W_3$$
 (B)  $W_2 < W_3 < W_1$   
(C)  $W_3 < W_1 < W_2$  (D)  $W_2 < W_1 < W_3$   
Official Ans. by NTA (D)



Area under curve is work

$$W_2 < W_1 < W_3$$

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- 9. Two long current carrying conductors are placed parallel to each other at a distance of 8 cm between them. The magnitude of magnetic field produced at mid-point between the two conductors due to current flowing in them is 300 μT. The equal current flowing in the two conductors is :
  (A) 30A in the same direction.
  - (B) 30A in the opposite direction.
  - (C) 60A in the opposite direction.
  - (D) 300A in the opposite direction.

## Official Ans. by NTA (B)

Sol. I O  
4cm 4cm  
B at 
$$O = 2 \frac{\mu_0 I}{2\pi r}$$
  
 $\frac{2 \times 4\pi \times 10^{-7} I}{2\pi 4 \times 10^{-2}} = 3 \times 10^{-4} T$ 

I = 30A in opp. direction

**10.** The time period of a satellite revolving around earth in a given orbit is 7 hours. If the radius of orbit is increased to three times its previous value, then approximate new time period of the satellite will be :

(A) 40 hours	(B) 36 hours
(C) 30 hours	(D) 25 hours

Official Ans. by NTA (B)

Sol. 
$$T = \frac{2\pi}{\sqrt{GM}} r^{3/2}$$
$$\frac{T_1}{T_2} = \left(\frac{r_1}{r_2}\right)^{3/2} = \left(\frac{1}{3}\right)^{3/2}$$
$$T_2 = T_1 \ 3\sqrt{3} = 21 \ \sqrt{3} \text{ hours}$$
$$\approx 36 \text{ hours}$$

11. The TV transmission tower at a particular station has a height of 125 m. For dubling the coverage of its range, the height of the tower should be increased by :
(A)125 m (B) 250 m

(C) 375 (D) 500 m Official Ans. by NTA (C)

Sol. Range d = 
$$\sqrt{2 \text{ Rh}}$$
  
 $d_2 = 2d_1$   
 $\sqrt{2 \text{ Rh}_2} = 2\sqrt{2 \text{ Rh}_1}$   
 $h_2 = 4h_1 = 500 \text{ m}$   
 $\Delta h = 500 \text{ m} - 125 \text{ m} = 375 \text{ m}$ 

**12.** The motion of a simple pendulum excuting S.H.M. is represented by following equation.

 $Y = A \sin (\pi t + \phi)$ , where time is measured in second.

The length of pendulum is :

(A) 97.23 cm
(B) 25.3 cm
(C) 99.4 cm
(D) 406.1 cm
Official Ans. by NTA (C)

Sol. 
$$\omega = \sqrt{\frac{g}{\ell}} = \pi$$
  
 $\frac{g}{\ell} = \pi^2 \Longrightarrow \ell = \frac{g}{\pi^2}$   
 $\ell = \frac{980}{\pi^2} \approx 99.4 \,\mathrm{cm}$ 

A vessel contains 16g of hydrogen and 128 g of oxygen at standard temperature and pressure. The volume of the vessel in cm<sup>3</sup> is :

(A)  $72 \times 10^5$ (B)  $32 \times 10^5$ (C)  $27 \times 10^4$ (D)  $54 \times 10^4$ Official Ans. by NTA (C)

Sol. No of moles of  $H_2 = 8$  moles No of moles of  $O_2 = 4$  moles Total moles = 12 moles At STP 1 mole occupy =  $22.4\ell = 22.4 \times 10^3$  cm<sup>3</sup> 12 moles will occupy =  $12 \times 22.4 \times 10^3$  cm<sup>3</sup>  $\approx 26.8 \times 10^4$  cm<sup>3</sup>



**14.** Given below are two statements :

**Statement I:** The electric force changes the speed of the charged particle and hence changes its kinetic energy: whereas the magnetic force does not change the kinetic energy of the charged particle.

**Statement II:** The electric force accelerates the positively charged particle perpendicular to the direction of electric field. The magnetic force accelerates the moving charged particle along the direction of magnetic field. In the light of the above statements, choose the most appropriate answer from the options given below:

(A) Both Statement I and Statement II are correct.

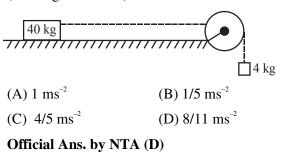
(B) Both Statement I and Statement II are incorrect.

(C) Statement I is correct but Statement II is incorrect.

(D) Statement I is incorrect but Statement II is correct.

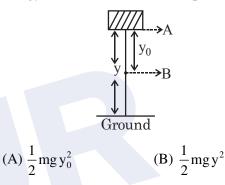
Official Ans. by NTA (C)

- Sol. Electric field can change speed and kinetic energy but magnetic field can not change speed  $\Delta$  KE. Because magnetic force is always  $\perp$  to velocity.
- 15. A block of mass 40 kg slides over a surface, when a mass of 4 kg is suspended through an inextensible massless string passing over frictionless pulley as shown below. The coefficient of kinetic friction between the surface and block is 0.02. The acceleration of block is. (Given  $g = 10 \text{ ms}^{-2}$ .)



Sol. For 4 kg block 4g - T = 4aFor 40 kg block  $T - 40g \times 0.02 = 40 a$ Adding both eq. 40 - 8 = 44a $a = \frac{32}{44} = \frac{8}{11} \text{ m / s}^2$ 

**16.** In the given figure, the block of mass m is dropped from the point 'A'. The expression for kinetic energy of block when it reaches point 'B' is :

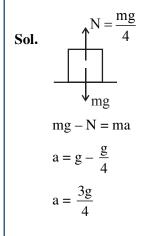




- Sol. Work done by gravity =  $K_B K_A$   $mgy_0 = K_B - 0$  $K_B = mgy_0$
- 17. A block of mass M placed inside a box descends vertically with acceleration 'a'. The block exerts a force equal to one-fourth of its weight on the floor of the box. The value of 'a' will be :

(A) 
$$\frac{g}{4}$$
 (B)  $\frac{g}{2}$  (C)  $\frac{3g}{4}$  (D) g

Official Ans. by NTA (C)



20.

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18. If the electric potential at any point (x, y, z)m in space is given by V = 3x<sup>2</sup> volt. The electric field at the point (1, 0, 3) m will be :
(A) 3 Vm<sup>-1</sup>, directed along positive x-axis.
(B) 3 Vm<sup>-1</sup>, directed along negative x-axis.
(C) 6 Vm<sup>-1</sup>, directed along positive x-axis.
(D) 6 Vm<sup>-1</sup>, directed along negative x-axis.

Official Ans. by NTA (D)

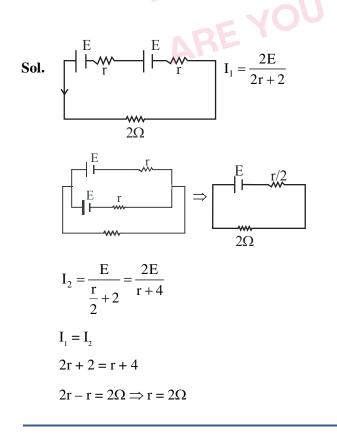
Sol.  $E_x = -\frac{\partial V}{\partial x} = -6x$ At (1, 0, 3)  $\vec{E} = -6V / m \hat{i}$ 

AYJR

19. The combination of two identical cells, whether connected in series or parallel combination provides the same current through an external resistance of  $2\Omega$ . The value of internal resistance of each cell is :

(A) 2Ω (B) 4Ω (C) 6Ω (D) 8Ω

Official Ans. by NTA (A)



of 100 m. How high	above the ground he can
throw the same ball?	
(A) 25 m	(B) 50 m
(C) 100 m	(D) 200 m

A person can throw a ball upto a maximum range

Official Ans. by NTA (B)

**Sol.** 
$$\mathbf{R} = \frac{u^2 \sin 2\theta}{g} R_{\max} = \frac{u^2}{g} = 100$$

$$H_{max} = \frac{u^2}{2g} = \frac{100}{2} = 50m$$

#### **SECTION-B**

 The vernier constant of Vernier callipers is 0.1 mm and it has zero error of (-0.05) cm. While measuring diameter of a sphere, the main scale reading is 1.7 cm and coinciding vernier division is 5. The corrected diameter will be \_\_\_\_\_ × 10<sup>-2</sup> cm.

Official Ans. by NTA (180)

- **Sol.** Measured diameter =  $MSR + VSR \times VC$ 
  - =  $1.7 + 0.01 \times 5$ = 1.75Corrected = Measured - Error = 1.75 - (-0.05)= 1.80 cm =  $180 \times 10^{-2}$  cm 180

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4.

2. A small spherical ball of radius 0.1 mm and density  $10^4$  kg m<sup>-3</sup> falls freely under gravity through a a distance h before entering a tank of water. If after entering the water the velocity of ball does not change and it continue to fall with same constant velocity inside water, then the value of h wil be\_\_\_\_m.

(Given  $g = 10 \text{ ms}^{-2}$ , viscosity of water  $= 1.0 \times 10^{-5} \text{ N-sm}^{-2}$ ).

Official Ans. by NTA (20)

Sol. Speed after falling through height h Should be equal to terminal velocity

2 . .

$$\sqrt{2gh} = \frac{2}{9} \frac{r^{2}(d-\rho)g}{\eta}$$

$$\sqrt{2gh} = \frac{2}{9} \frac{10^{-8}(10000 - 1000) \times 10}{10^{-5}}$$

$$= \frac{2}{9} \times 10^{-8} \frac{9 \times 10^{4}}{10^{-5}} = 20$$

$$2 \times 10 \times h = 400$$

$$h = 20 \text{ m}$$

3. In an experiment to determine the velocity of sound in air at room temperature using a resonance is observed when the air column has a length of 20.0 cm for a tuning fork of frequency 400 Hz is used. The velocity of the sound at room temperature is 336 ms<sup>-1</sup>. The third resonance is observed when the air column has a length of \_\_\_\_\_cm.

#### Official Ans. by NTA (104)

**Sol.** For first resonance

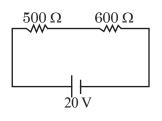
$$\ell_1 + e = \frac{\lambda}{4}$$

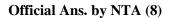
$$\lambda = \frac{336}{400} \times 100 \text{ cm} = 84 \text{ cm} \Rightarrow \frac{\lambda}{4} = 21 \text{ cm}$$

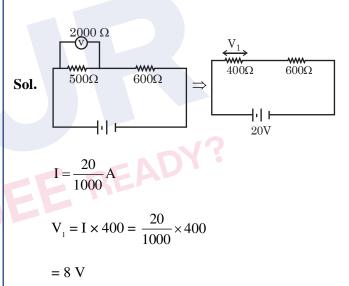
$$e = 21 - 20 = 1 \text{ cm}$$
For third resonance

$$\ell_3 + e = \frac{5\lambda}{4} = 105 \text{ cm} \Rightarrow \ell_3 = 104 \text{ cm}$$

Two resistors are connected in series across a battery as shown in figure. If a voltmeter of resistance 2000  $\Omega$  is used to measure the potential difference across 500  $\Omega$  resister, the reading of the voltmeter will be\_\_\_\_V.





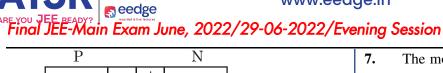


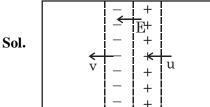
5. A potential barrier of 0.4 V exists across a p-n junction. An electron enters the junction from the n-side with a speed of  $6.0 \times 10^5 \text{ ms}^{-1}$ . The speed with which electron enters the p side will be

 $\frac{x}{3} \times 10^5 \text{ ms}^{-1}$  the value of x is \_\_\_\_\_.

(Given mass of electron =  $9 \times 10^{-31}$  kg, charge on electron =  $1.6 \times 10^{-19}$ C.)

Official Ans. by NTA (14)





Work done by Electric field =  $K_f - K_i$ 

0.4

$$\frac{1}{2}mv^{2} - \frac{1}{2}mu^{2} = -1.6 - 10^{-19} \times 0.$$
  
$$\frac{1}{2}9 \times 10^{-31} (v^{2} - u^{2}) = -0.64 \times 10^{-19}$$
  
$$u^{2} - v^{2} = \frac{2 \times 0.64 \times 10^{12}}{9}$$
  
$$v^{2} = \left(36 - \frac{128}{9}\right) \times 10^{10}$$
  
$$v = \frac{14}{3} \times 10^{5} \text{ m/s}$$
  
$$x = 14$$

6. The displacement current of 4.425 µA is developed in the space between the plates of parallel plate capacitor when voltage is changing at a rate of 10<sup>6</sup>  $Vs^{-1}$ . The area of each plate of the capacitor is 40 cm<sup>2</sup>. The distance between each plate of the capacitor is  $x \times 10^{-3}$ m. The value of x is,

(Permittivity of free space,  $E_0 = 8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$ )

Official Ans. by NTA (8)

**Sol.** Displacement Current = Conduction Current

$$= \frac{dq}{dt}$$

$$I_{d} = \frac{\epsilon_{0} A}{d} \frac{dV}{dt}$$

$$d = \frac{8.85 \times 10^{-12} \times 4 \times 10^{-3} \times 10^{6}}{4.425 \times 10^{-6}}$$

$$= 8 \text{ mm}$$

$$X = 8$$

7. The moment of inertia of a uniform thin rod about a perpendicular axis passing through one end is I<sub>1</sub>. The same rod is bent into a ring and its moment of inertia about a diameter is  $I_2$ . If  $\frac{I_1}{I_2}$  is  $\frac{x\pi^2}{3}$ , then the value of x will be\_\_\_\_

Official Ans. by NTA (8)

- $I_1 = \frac{ml^2}{3}$ Sol.  $\ell = 2\pi r \Rightarrow \frac{\ell}{r} = 2\pi$  $I_1 = \frac{mr^2}{2}$  $\frac{I_1}{I_2} = \frac{2}{3} \left(\frac{\ell}{r}\right)$  $=\frac{2}{3}\times 4\pi^2 = \frac{8\pi^2}{3}$ 
  - x = 8
- 8. The half life of a radioactive substance is 5 years. After x years a given sample of the radioactive substance gest reduced to 6.25% of its initial value of x is \_\_\_\_\_.

lives

Official Ans. by NTA (20)

Sol. 
$$T1/2 = 5$$
 year

$$N = N_0 \left(\frac{1}{2}\right)^{No \text{ of half}}$$
$$\frac{N}{N_0} = \frac{1}{16} = \left(\frac{1}{2}\right)^4$$

Time = 4 half lives = 20 years



EE READY?

9. In a double slit experiment with monochromatic light, fringes are obtained on a screen placed at some distance from the plane of slits. If the screen is moved by  $5 \times 10^{-2}$  m towards the slits, the change in fringe width is  $3 \times 10^{-3}$  cm. If the distance between the slits is 1 mm, then the wavelength of the light will be \_\_\_\_\_nm.

Official Ans. by NTA (600 )

Sol. 
$$\beta = \frac{\lambda D}{d}$$

$$\Delta p = \frac{\Delta \beta d}{d} \Delta D$$

 $\Delta D$ 

 $= \frac{3 \times 10^{-5} \times 1 \times 10^{-3}}{5 \times 10^{-2}}$  $= 60 \times 10^{-8} = 600 \times 10^{-9} m$ = 600 nm

10. An inductor of 0.5 mH, a capacitor of 200  $\mu$ F and a resistor of 2  $\Omega$  are connected in series with a 220 V ac source. If the current is in phase with the emf, the frequency of ac source will be\_\_\_x 10<sup>2</sup> Hz.

Official Ans. by NTA (5)

Sol. If Current is in phase with emf then the frequency

of source 
$$=\frac{1}{2\pi\sqrt{LC}}$$
 (Resonant frequency)

$$\frac{1}{2\pi\sqrt{\frac{1}{2} \times 10^{-3} \times 2 \times 10^{-4}}}$$
$$= \frac{1}{2\pi} \times \sqrt{10} \times 1000 = 500 \text{ Hz}$$



## **FINAL JEE-MAIN EXAMINATION - JUNE, 2022**

4.

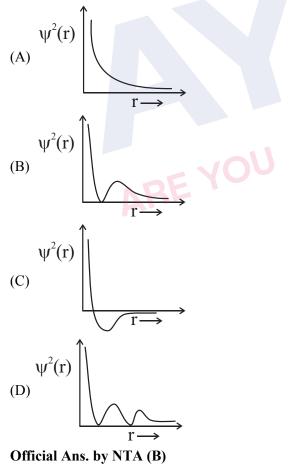
## (Held On Wednesday 29<sup>th</sup> June, 2022)

## TIME: 3:00 PM to 06:00 PM

## CHEMISTRY

SECTION-A		
1.	Using the rules for	significant figures, the correct
	answer for the expre	ssion $\frac{0.02858 \times 0.112}{0.5702}$ will be:
	(A) 0.005613	(B) 0.00561
	(C) 0.0056	(D) 0.006
	Official Ans. by NT	<sup>C</sup> A (B)

- **Sol.** Reported answer should not be more precise than least precise term in calculations, so there should be three significant figures in reported answer.
- 2. Which of the following is the correct plot for the probability density  $\psi^2(r)$  as a function of distance 'r' of the electron form the nucleus for 2s orbital?



Sol. For 2s, number of radial nodes = 2 - 0 - 1 = 1 and value of  $\psi^2$  is always positive.

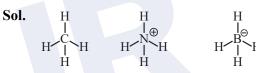
## TEST PAPER WITH SOLUTION

- Consider the species CH<sub>4</sub>, NH<sub>4</sub><sup>+</sup> and BH<sub>4</sub><sup>-</sup>. Choose the correct option with respect to the there species:
  (A) They are isoelectronic and only two have tetrahedral structures
  - (B) They are isoelectronic and all have tetrahedral structures

(C) Only two are isoelectronic and all have tetrahedral structures

(D) Only two are isoelectronic and only two have tetrahedral structures

### Official Ans. by NTA (B)



All are tetrahedral and each have 10 electrons.

4.0 moles of argon and 5.0 moles of PCI<sub>5</sub> are introduced into an evacuated flask of 100 litre capacity at 610 K. The system is allowed to equilibrate. At equilibrium, the total pressure of mixture was found to be 6.0 atm. The  $K_p$  for the reaction is [Given : R = 0.082L atm  $K^{-1}$  mol<sup>-1</sup>] (A) 2.25 (B) 6.24 (C) 12.13 (D) 15.24

2

Official Ans. by NTA (A)

Sol. 
$$PCl_5 = 5 \text{ mole}$$
  
 $Ar = 4 \text{ mole}$   
 $P_{Total} = \frac{9 \times 0.82 \times 610}{100} = 4.5 \text{ atm}$   
 $P_{PCl_5} = \frac{5 \times 4.5}{9} = 2.5 \text{ ; } P_{Ar} = \frac{4 \times 4.5}{9} =$   
 $PCl_5 \implies PCl_3 + Cl_2$   
 $2.5 - P P P$   
 $P_{total} = 2.5 - P + P + P + P_{Ar} = 6$   
 $P = 1.5$   
 $K_p = \frac{1.5 \times 1.5}{1} = 2.25$ 



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5.	A 42.12% (w/v) solution of NaCl causes	
	precipitation of a certain sol in 10 hours. The	
	coagulating value of NaCl for the sol is	
	[Given : Molar mass : $Na = 23.0 \text{ g mol}^{-1}$ ; $Cl = 35.5$	
	$g \text{ mol}^{-1}$ ]	
	(A) 36 mmol $L^{-1}$	
	(B) 36 mol $L^{-1}$	
	(C) 1440 mol $L^{-1}$	
	(D) 1440 mmol L <sup>-1</sup>	

Official Ans. by NTA (D)

Sol. Data insufficient.

6. Given below are two statements. One is labelled as Assertion A and the other is labelled as Reason R.
Assertion A : The first ionization enthalpy for oxygen is lower than that of nitrogen.

**Reason R :** The four electrons in 2p orbitals of oxygen experience more electron-electron repulsion.

In the light of the above statements, choose the correct answer from the options given below.

(A) Both A and R are correct and R is the correct explanation of A.

(B) Both A and R are correct but R is NOT the correct explanation of A.

(C) A is correct but R is not correct.

(D) A is not correct but R is correct

Official Ans. by NTA (A)

**Sol.** Ionisation energy = N > O.

In oxygen atom, 2 of the 4 2p electrons must occupy the same 2p orbital resulting in an increased electron electron-repulsion. Match List I with List II.

7.

List I Ore	List II Composition
A. Siderite	I. Fe CO <sub>3</sub>
B. Malachite	II. CuCO <sub>3</sub> .Cu(OH) <sub>2</sub>
C. Sphalerite	III. ZnS
D. Calamine	IV. ZnCO <sub>3</sub>

Choose the correct answer from the options given below:

(A) A-I, B-II, C-III, D-IV
(B) A-III, B-IV, C-II, D-I
(C) A-IV, B-III, C-I, D-II
(D) A-I, B-II, C-IV, D-III
Official Ans. by NTA (A)

Sol. Siderite – FeCO<sub>3</sub> Malachite – CuCO<sub>3</sub>.Cu(OH)<sub>2</sub> Calamine – ZnCO<sub>3</sub> Sphalerite – ZnS

8. Given below are two statements .

**Statement I :** In CuSO<sub>4</sub>.5H<sub>2</sub>O, Cu–O bonds are present.

**Statement II** : In  $CuSO_4.5H_2O$ , ligands coordinating with Cu(II) ion are O-and S-based ligands.

In the light of the above statements, choose the correct answer from the options given below

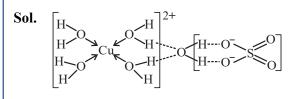
(A) Both Statement I and Statement II are correct

(B) Both Statement I and Statement II are incorrect

(C) Statement I is correct but Statement II is incorrect

(D) Statement I is incorrect but Statement II is correct

Official Ans. by NTA (C)



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- 9. Amongst baking soda, caustic soda and washing soda carbonate anion is present in :
  (A) washing soda only.
  (B) washing soda and caustic soda only.
  - (C) washing soda and baking soda only.
  - (D) baking soda, caustic soda and washing soda.

Official Ans. by NTA (A)

**Sol.** Baking soda  $\rightarrow$  NaHCO<sub>3</sub>

Washing soda  $\rightarrow$  Na<sub>2</sub>CO<sub>3</sub>.10H<sub>2</sub>O

Caustic soda  $\rightarrow$  NaOH

- 10. Number of lone pair (s) of electrons on central atom and the shape of  $BrF_3$  molecule respectively, are :
  - (A) 0, triangular planar.
  - (B) 1, pyramidal.
  - (C) 2, bent T-shape.
  - (D) 1, bent T-shape

Official Ans. by NTA (C)

Sol.

Steric no. = 5 ( $sp^3d$ ), lone pair = 2 Bent T shape.

 Aqueous solution of which of the following boron compounds will be strongly basic in nature?

 $(A) NaBH_4 (B) LiBH_4$ 

(C)  $B_2H_6$  (D)  $Na_2B_4O_7$ 

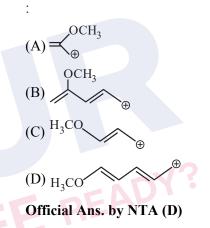
Official Ans. by NTA (D)

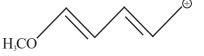
**Sol.** Na<sub>2</sub>B<sub>4</sub>O<sub>7</sub> gives H<sub>3</sub>BO<sub>3</sub> and NaOH (strong base) in water.

12. Sulphur dioxide is one of the components of polluted air. SO<sub>2</sub> is also a major contributor to acid rain. The correct and complete reaction to represent acid rain caused by SO<sub>2</sub> is :

(A)  $2 \operatorname{SO}_2 + \operatorname{O}_2 \rightarrow 2 \operatorname{SO}_3$ (B)  $\operatorname{SO}_2 + \operatorname{O}_3 \rightarrow \operatorname{SO}_3 + \operatorname{O}_2$ (C)  $\operatorname{SO}_2 + \operatorname{H}_2\operatorname{O}_2 \rightarrow \operatorname{H}_2\operatorname{SO}_4$ (D)  $2 \operatorname{SO}_2 + \operatorname{O}_2 + 2 \operatorname{H}_2\operatorname{O} \rightarrow 2 \operatorname{H}_2\operatorname{SO}_4$ Official Ans. by NTA (D)

- Sol.  $2SO_2 + O_2 + 2H_2O \rightarrow 2H_2SO_4$  (Acid rain)
- **13.** Which of the following carbocations is most stable





Is most stable carbocation

The stable carbocation formed in the above reaction is :

(A) 
$$CH_3CH_2\overset{\oplus}{C}H_2$$
 (B)  $CH_3\overset{\oplus}{C}H_2$   
(C)  $CH_3 - \overset{\oplus}{C}H - CH_3$  (D)  $\overset{\oplus}{C}HCH_2CH_3$ 

Official Ans. by NTA (C)

**Sol.**  $CH_3$ -CH- $CH_3$  is formed in the above reaction

Give yourself an extra edge

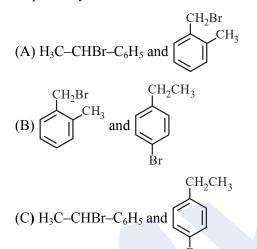
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Sol.



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15. Two isomers (A) and (B) with Molar mass 184 g/mol and elemental composition C, 52.2%; H, 4.9% and Br 42.9% gave benzoic acid and p-bromobenzoic acid, respectively on oxidation with KMnO<sub>4</sub>. Isomer 'A' is optically active and gives a pale yellow precipitate when warmed with alcoholic AgNO<sub>3</sub>. Isomer 'A' and 'B' are, respectively :

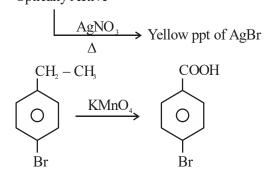


(D) 
$$H_2CH_3$$
 and  $H_3C$ -CHBr-C<sub>6</sub>H<sub>5</sub>

Official Ans. by NTA (C)

Sol. Br I  $CH - CH_3$  $KMnO_2$ 

> (A) Optically Active



COOH

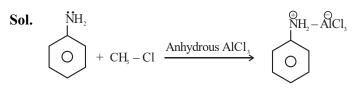
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**16.** In Friedel-Crafts alkylation of aniline, one gets :

(A) alkylated product with ortho and para substitution.

- (B) secondary amine after acidic treatment.
- (C) an amide product.
- (D) positively charged nitrogen at benzene ring.

#### Official Ans. by NTA (D)



17. Given below are two statements : one is labelled asAssertion A and the other is labelled as Reason R.Assertion A: Dacron is an example of polyester polymer.

**Reason R:** Dacron is made up of ethylene glycol and terephthalic acid monomers.

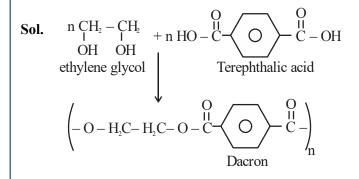
In the light of the above statements, choose the *most appropriate* answer from the options given below.

(A) Both A and B are correct and R is the correct explanation of A.

(B) Both **A** and **B** are correct but **R** is NOT the correct explanation of **A**.

- (C) A is correct but **R** is not correct.
- (D) A is not correct but **R** is correct.

Official Ans. by NTA (A)



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18. The structure of protein that is unaffected by heating is :(A) secondary structure (B) tertiary structure(C) primary structure (D) quaternary structure

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- **Sol.** Primary structure of protein is unaffected by physical 'or' chemical changes.
- **19.** The mixture of chloroxylenol and terpineol is an example of :
  - (A) antiseptic (B) pesticide
  - (C) disinfectant (D) narcotic analgesic

Official Ans. by NTA (A)

Official Ans. by NTA (C)

- **Sol.** Antiseptic Dettol is mixture of chloroxylenol and terpineol.
- 20. A white precipitate was formed when BaCl<sub>2</sub> was added to water extract of an inorganic salt. Further, a gas 'X' with characteristic odour was released when the formed white precipitate was dissolved in dilute HCl. The anion present in the inorganic salt is :
  - (A) [⁻
  - (C)  $S^{2-}$

Official Ans. by NTA (B)

**Sol.** BaCl<sub>2</sub> + SO<sub>3</sub><sup>2-</sup>  $\rightarrow$  BaSO<sub>3</sub>  $\downarrow \xrightarrow{\text{dil.HCl}}$  SO<sub>2</sub>  $\uparrow$ 

white

burning sulphur like smell

(B)  $SO_3^{2-}$ 

 $(D) NO_{2}$ 

#### SECTION-B

 A box contains 0.90 g of liquid water in equilibrium with water vapour at 27°C. The equilibrium vapour pressure of water at 27°C 32.0 Torr. When the volume of the box is increased, some of the liquid water evaporates to maintain the equilibrium pressure. If all the liquid water evaporates, then the volume of the box must be\_\_\_\_\_ litre. [nearest integer]

(Given:  $R = 0.082 L \text{ atm } K^{-1} \text{ mol}^{-1}$ )

(Ignore the volume of the liquid water and assume water vapours behave as an ideal gas.)

### Official Ans. by NTA (29)

Sol. 
$$V = \frac{nRT}{P} = \frac{0.90 \times 0.82 \times 300 \times 760}{18 \times 32} = 29.21$$

2. 2.2 g of nitrous oxide (N<sub>2</sub>O) gas is cooled at a constant pressure of 1 atm from 310 K to 270 K causing the compression of the gas from 217.1 mL to 167.75 mL. The change in internal energy of the process,  $\Delta U$  is '-x' J. The value of 'x' is \_\_.

[nearest integer]

(Given: atomic mass of N = 14 g mol<sup>-1</sup> and of O =  $16 \text{ g mol}^{-1}$ .

Molar heat capacity of N<sub>2</sub>O is 100 JK<sup>-1</sup> mol<sup>-1</sup>)

Official Ans. by NTA (195)

Sol. 
$$N_2O \text{ moles} = \frac{2.2}{44} = \frac{1}{20}$$
  
 $\Delta H = nC_p \Delta T = \frac{1}{20} \times 100(-40) = -200J$   
 $\Delta U = q_p + w$   
 $w = -P_{ext} \Delta V$   
 $W = -1 \frac{(167.75 - 217.1)}{1000} \times 101.3J$   
 $w = +5J$   
 $\Delta U = -200 + 5 = -195J$ 

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3. Elevation in boiling point for 1.5 molal solution of glucose in water is 4K. The depression in freezing point for 4.5 molal solution of glucose in water is 4K. The ratio of molal elevation constant to molal depression constant ( $K_b/K_f$ ) is\_\_\_\_.

#### Official Ans. by NTA (3)

**Sol.**  $\Delta T_{\rm b} = iK_{\rm b}m$ 

 $\Delta T_{f} = iK_{f}m$   $\frac{4}{4} = \frac{K_{b}1.5}{K_{f}4.5}$   $\frac{K_{b}}{K_{f}} = 3$ 

The cell potential for the given cell at 298 K
Pt | H<sub>2</sub>(g,1 bar) | H<sup>+</sup>(aq) || Cu<sup>2+</sup>(aq) | Cu(s) is 0.31V. The pH of the acidic solution is found to be 3, whereas the concentration of Cu<sup>2+</sup> is 10<sup>-x</sup> M.

(Given: 
$$E_{Cu^{2+}/Cu}^{\Theta} = 0.34 \text{ V and } \frac{2.303 \text{RT}}{\text{F}} = 0.06 \text{V}$$
)

Official Ans. by NTA (7)

The value of x is \_\_\_\_\_.

Sol. 
$$H_2(g) + Cu^{2+}(aq.) \rightarrow 2H^+(aq.) + Cu(s)$$
  
 $0.31 = 0.34 - \frac{0.06}{2} \log \frac{[H^+]^2}{[Cu^{2+}]}$   
 $[Cu^{2+}] = 10^{-7} M$   
 $x = 7$ 

5. The equation

$$k = (6.5 \times 10^{12} \text{ s}^{-1}) \text{ e}^{-26000 \text{ K/T}}$$

is followed for the decomposition of compound A. The activation energy for the reaction is \_\_\_\_\_ kJ mol<sup>-1</sup>. [nearest integer] (Given:  $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$ ) Official Ans. by NTA (216)

)

**Sol.** 
$$K = Ae^{-Ea/RT} = (6.5 \times 10^{12} s^{-1}) e^{-26000 K/T}$$

$$\frac{\text{Ea}}{8.314} = 26000$$
  
Ea = 216.164 kJ/mol.

6. Spin only magnetic moment of [MnBr<sub>6</sub>]<sup>4-</sup> is\_\_\_\_\_
 B.M. (round off to the closest integer)

#### Official Ans. by NTA (6)

**Sol.** 
$$Mn^{2+} \rightarrow t_{2g^{111}}e_{g^{11}}$$
  
 $\mu_s = \sqrt{35}$   
 $= 5.91$   
 $= 6$ 

7. For the reaction given below:

 $CoCl_3 \cdot xNH_3 + AgNO_3(aq) \rightarrow$ 

If two equivalents of AgCl precipitate out, then the value of x will be \_\_\_\_\_.

Official Ans. by NTA (5)

**Sol.** 
$$CoCl_3.xNH_3 + AgNO_3 \rightarrow AgCl \downarrow$$

2 mol

$$[Co(NH_3)_5Cl]Cl_2 + AgNO_3 \rightarrow AgCl \downarrow$$

2 mol

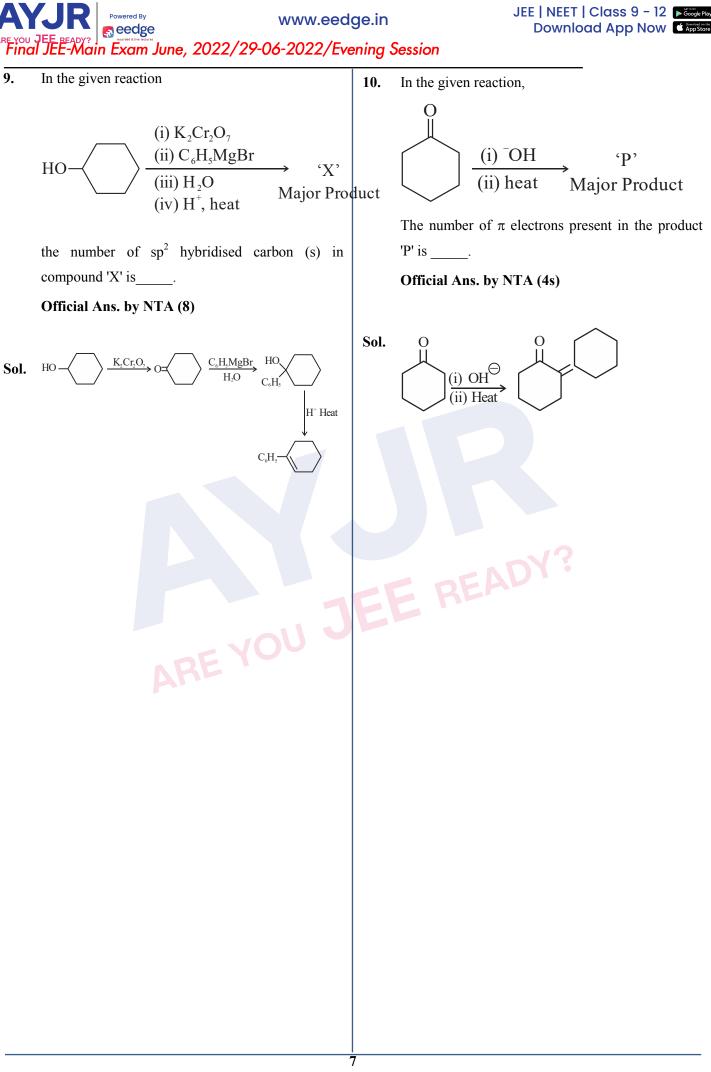
x = 5

8. The number of chiral alcohol(s) with molecular formula  $C_4H_{10}O$  is\_\_\_\_\_.

Official Ans. by NTA (1)

Sol. 
$$CH_3 - CH_2 - CH_2 - CH_2 - OH$$
  
 $CH_3 - CH_2 - CH_2 - CH_3$   
 $I$  (±)  
 $OH$  (±)  
 $CH_3 - CH - CH_2 - OH$   
 $CH_3 - CH - CH_2 - OH$   
 $CH_3 - CH - CH_2 - OH$   
 $CH_3 - CH_3 - CH_3$   
 $OH$ 

Out of which only two are chiral





**FINAL JEE-MAIN EXAMINATION - JUNE, 2022** (Held On Wednesday 29th June, 2022) TIME: 3:00 PM to 06:00 PM **MATHEMATICS TEST PAPER WITH SOLUTION SECTION-A** Let  $A = \begin{pmatrix} 2 & -1 \\ 0 & 2 \end{pmatrix}$ . If  $B = I - {}^{5}C_{1} \text{ (adjA)} + {}^{5}C_{2}$ 3. Let  $\alpha$  be a root of the equation  $1 + x^2 + x^4 = 0$ . 1.  $(adjA)^2 - \dots - {}^5C_5 (adjA)^5$ , then the sum of all Then the value of  $\alpha^{1011} + \alpha^{2022} - \alpha^{3033}$  is equal to: elements of the matrix B is: (A) 1 (B)  $\alpha$ (A) - 5(B) - 6(C) - 7(D) - 8(C)  $1 + \alpha$ (D)  $1 + 2\alpha$ Official Ans. by NTA (C) Official Ans. by NTA (A) **Sol.**  $B = (I - adjA)^5 = \begin{bmatrix} -1 & -1 \\ 0 & -1 \end{bmatrix}^5 = \begin{bmatrix} -1 & -5 \\ 0 & -1 \end{bmatrix}$ **Sol.**  $x^4 + x^2 + 1 = 0$  $\Rightarrow (x^2 + x + 1)(x^2 - x + 1) = 0$ Sum of its all elements = -7. 4.  $\Rightarrow$  x = ±  $\omega$ , ±  $\omega^2$  where  $\omega = 1^{1/3}$  and imaginary. The sum of the infinite series  $1 + \frac{5}{6} + \frac{12}{6^2} + \frac{22}{6^3} + \frac{35}{6^4} + \frac{51}{6^5} + \frac{70}{6^6} + \dots$  is equal to: So  $\alpha^{1011} + \alpha^{2022} - \alpha^{3033} = 1 + 1 - 1 = 1$ 2. Let arg (z) represent the principal argument of the (A)  $\frac{425}{216}$ (B)  $\frac{429}{216}$ complex number z. The, |z| = 3 and arg (z - 1) -(C)  $\frac{288}{125}$ (D) <u>280</u> arg  $(z + 1) = \frac{\pi}{4}$  intersect: Official Ans. by NTA (C) = YOV (A) Exactly at one point **Sol.**  $S = 1 + \frac{5}{6} + \frac{12}{6^2} + \frac{22}{6^3} + \frac{35}{6^4} + \dots$ (B) Exactly at two points (C) Nowhere  $\frac{S}{6} = \frac{1}{6} + \frac{5}{6^2} + \frac{12}{6^3} + \frac{22}{6^4} + \dots$ (D) At infinitely many points. Official Ans. by NTA (C) on subtraction  $\frac{5}{6}$ S = 1 +  $\frac{4}{6}$  +  $\frac{7}{6^2}$  +  $\frac{10}{6^3}$  +  $\frac{13}{6^4}$  + ....  $(0,1+\sqrt{2})$  $\frac{5}{36}S = 1 + \frac{4}{6^2} + \frac{7}{6^3} + \frac{10}{6^4} + \frac{13}{6^5} + \dots$ Sol. (0,1)|z| = 3on subtraction



$$S = \frac{288}{125}$$

5. The value of 
$$\lim_{x \to 1} \frac{(x^2 - 1)\sin^2(\pi x)}{x^4 - 2x^3 + 2x - 1}$$
 is equal to:

(A) 
$$\frac{\pi^2}{6}$$
 (B)  $\frac{\pi^2}{3}$   
(C)  $\frac{\pi^2}{2}$  (D)  $\pi^2$ 

Official Ans. by NTA (D)

**Sol.** 
$$\lim_{x \to 1} \frac{(x^2 - 1)\sin^2 \pi x}{(x^2 - 1)(x - 1)^2} = \lim_{x \to 1} \left( \frac{\sin((1 - x)\pi)}{\pi(1 - x)} \right)^2 \pi^2 = \pi^2$$

6. Let  $f : \mathbb{R} \to \mathbb{R}$  be a function defined by  $f(x) = (x-3)^{n_1} (x-5)^{n_2}, n_1, n_2 \in \mathbb{N}$ . The, which of the following is <u>NOT</u> true?

(A) For  $n_1 = 3$ ,  $n_2 = 4$ , there exists  $\alpha \in (3,5)$  where *f* attains local maxima.

(B) For  $n_1 = 4$ ,  $n_2 = 3$ , there exists  $\alpha \in (3,5)$  where *f* attains local manima.

(C) For  $n_1 = 3$ ,  $n_2 = 5$ , there exists  $\alpha \in (3,5)$  where *f* attains local maxima.

(D) For  $n_1 = 4$ ,  $n_2 = 6$ , there exists  $\alpha \in (3,5)$  where *f* attains local maxima.

Official Ans. by NTA (C)

Sol. 
$$f'(x) = (x-3)^{n_1-1}(x-5)^{n_2-1}(n_1+n_2)\left(x-\frac{5n_1+3n_2}{n_1+n_2}\right)$$
  
Option (3) is incorrect since

Option (3) is incorrect since

for  $n_1 = 3$ ,  $n_2 = 5$ 

$$f'(x) = 8(x-3)^2(x-5)^4 \left(x - \frac{30}{8}\right)^2$$
  
minima at  $x = \frac{30}{8}$ 

7. Let *f* be a real valued continuous function on [0,1] and  $f(x) = x + \int_{0}^{1} (x-t)f(t)dt$ . Then which of the following points (x,y) lies on the curve y = f(x)? (A) (2, 4) (B) (1, 2) (C) (4, 17) (D) (6, 8) Official Ans. by NTA (D)

Sol. 
$$f(x) = \left(1 + \int_{0}^{1} f(t)dt\right)x - \int_{0}^{1} tf(t)dt$$
$$f(x) = Ax - B \qquad ...(i)$$
$$A = 1 + \int_{0}^{1} f(t)dt = 1 + \int_{0}^{1} (At - B)dt$$
$$\Rightarrow A = 2(1 - B) \qquad ...(ii)$$
$$Also B = \int_{0}^{1} tf(t)dt = \int_{0}^{1} (At^{2} - Bt)dt$$
$$A = \frac{9}{2}B \qquad ...(iii)$$
From (2), (3)
$$A = \frac{18}{13}, B = \frac{4}{13}$$
so f(6) = 8
$$If \int_{0}^{2} (\sqrt{2x} - \sqrt{2x - x^{2}})dx =$$
$$\int_{0}^{1} (1 - \sqrt{1 - y^{2}} + \frac{y^{2}}{2})dy + \int_{1}^{2} (2 - \frac{y^{2}}{2})dy +$$
$$(A) \int_{0}^{1} (1 + \sqrt{1 - y^{2}})dy$$
$$(B) \int_{0}^{1} (\frac{y^{2}}{2} - \sqrt{1 - y^{2}} + 1)dy$$
$$(C) \int_{0}^{1} (1 - \sqrt{1 - y^{2}})dy$$
$$(D) \int_{0}^{1} (\frac{y^{2}}{2} + \sqrt{1 - y^{2}} + 1)dy$$

Ι

Official Ans. by NTA (C)

Sol. LHS = 
$$\int_{0}^{2} \left(\sqrt{2x} - \sqrt{2x - x^{2}}\right) dx = \frac{8}{3} - \frac{\pi}{2}$$
  
RHS =  $\int_{0}^{1} \left(1 - \sqrt{1 - y^{2}} - \frac{y^{2}}{2}\right) dy + \int_{1}^{2} \left(2 - \frac{y^{2}}{2}\right) dy + I$ 

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$$I + \frac{1}{3} - \frac{1}{4}$$
  
So, I =  $1 - \frac{\pi}{4} = \int_{0}^{1} (1 - \sqrt{1 - y^{2}}) dy$ 

9. If y = y(x) is the solution of the differential equation  $(1 + e^{2x})\frac{dy}{dx} + 2(1 + y^2)e^x = 0$  and y(0) = 0, then  $6\left(y'(0) + \left(y\left(\log_e \sqrt{3}\right)\right)^2\right)$  is equal to: (A) 2 (B) - 2(C) - 4(D) - 1

Official Ans. by NTA (C)

**Sol.** 
$$\frac{dy}{1+y^2} + \frac{2e^x}{1+e^{2x}}dx = 0$$
 (i)

on integration

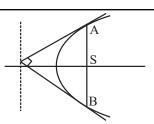
$$\tan^{-1} y + 2\tan^{-1} e^{x} = c$$
  

$$\because y(0) = 0$$
  
so,  $C = \frac{\pi}{2} \Longrightarrow \tan^{-1} y + 2\tan^{-1} e^{x} = \frac{\pi}{4}$   
from eq.(i),  $\left(\frac{dy}{dx}\right)_{x=0} = -1$   
arg y(ln  $\sqrt{3}$ ) =  $-\frac{1}{\sqrt{3}}$   
 $6\left[y'(0) + (y(\ln\sqrt{3})^{2}\right] = 6\left[-1 + \frac{1}{3}\right] = -4$ 

Let P :  $y^2 = 4ax$ , a > 0 be a parabola with focus 10. S.Let the tangents to the parabola P make an angle of  $\frac{\pi}{4}$  with the line y = 3x + 5 touch the parabola P at A and B. Then the value of a for which A,B and S are collinear is: (A) 8 only (B) 2 only

(C) 
$$\frac{1}{4}$$
 only (D) any  $a > 0$   
Official Ans. by NTA (D)

**Sol.** Lines making angle  $\frac{\pi}{4}$  with y = 3x + 5have slope -2 & 1/2. Which are perpendicular to each-other so, A, S, B are collinear for all a > 0.



Let a triangle *ABC* be inscribed in the circle  $x^2$  – 11.

$$\sqrt{2}(x+y)+y^2=0$$
 such that  $\angle BAC = \frac{\pi}{2}$ . If the

length of side AB is  $\sqrt{2}$ , then the area of the  $\triangle$ ABC is equal to:

(A) 
$$(\sqrt{2} + \sqrt{6})/3$$
 (B)  $(\sqrt{6} + \sqrt{3})/2$   
(C)  $(3 + \sqrt{3})/4$  (D)  $(\sqrt{6} + 2\sqrt{3})/4$ 

**Official Ans. by NTA (Dropped)** 

Sol. Radius of given circle is 1.  
BC = diameter = 2, AB = 
$$\sqrt{2}$$
  
AC =  $\sqrt{BC^2 - AB^2} = \sqrt{2}$   
 $\Delta ABC = \frac{1}{2}AB.AC = 1$   
B  
C

12. Let  $\frac{x-2}{3} = \frac{y+1}{-2} = \frac{z+3}{-1}$  lie on the plane px - qy + z = 5, for some p,  $q \in \mathbb{R}$ . The shortest distance of the plane from the origin is:

(A) 
$$\sqrt{\frac{3}{109}}$$
 (B)  $\sqrt{\frac{5}{142}}$ 

(C) 
$$\sqrt{\frac{5}{71}}$$
 (D)  $\sqrt{\frac{1}{142}}$ 

Official Ans. by NTA (B)

**Sol.** (2, -1, -3) satisfy the given plane. So 2p + q = 8.... (i) Also given line is perpendicular to normal plane so 3p + 2q - 1 = 0.... (ii)



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 $\Rightarrow p = 15, q = -22$ Eq. of plane 15x - 22y + z - 5 = 0

its distance from origin  $=\frac{6}{\sqrt{710}} = \sqrt{\frac{5}{142}}$ 

- 13. The distance of the origin from the centroid of the triangle whose two sides have the equations x 2y + 1 = 0 and 2x y 1 = 0 and whose orthocenter is  $\left(\frac{7}{3}, \frac{7}{3}\right)$  is:
  - (A)  $\sqrt{2}$  (B) 2

(C) 
$$2\sqrt{2}$$
 (D) 4

Official Ans. by NTA (C)

**Sol.** AB = x - 2y + 1 = 0

 $AC \equiv 2x - y - 1 = 0$ 

So A(1, 1)

Altitude from B is BH =  $x + 2y - 7 = 0 \Rightarrow B(3, 2)$ Altitude from C is CH =  $2x + y - 7 = 0 \Rightarrow C(2, 3)$ Centroid of  $\triangle ABC = E(2, 2) \ OE = 2\sqrt{2}$ 

14. Let Q be the mirror image of the point P(1, 2, 1) with respect to the plane x + 2y + 2z = 16. Let T be a plane passing through the point Q and contains the line  $\vec{r} = -\hat{k} + \lambda (\hat{i} + \hat{j} + 2\hat{k}), \lambda \in \mathbb{R}$ . Then, which

of the following points lies on T?

(A) (2, 1, 0) (B) (1, 2, 1)

(C) (1, 2, 2) (D) (1, 3, 2)

Official Ans. by NTA (B)

**Sol.** Image of P(1, 2, 1) in x + 2y + 2z - 16 = 0

is given by Q(4, 8, 7)

Eq. of plane 
$$T = \begin{vmatrix} x & y & z+1 \\ 4 & 8 & 6 \\ 1 & 1 & 2 \end{vmatrix} = 0$$

 $\Rightarrow$  2x - z = 1 so B(1, 2, 1) lies on it.

**15.** Let A, B, C be three points whose position vectors respectively are:

 $\vec{a} = \hat{i} + 4\hat{j} + 3\hat{k}$  $\vec{b} = 2\hat{i} + \alpha\hat{j} + 4\hat{k}, \alpha \in \mathbb{R}$  $\vec{c} = 3\hat{i} - 2\hat{j} + 5\hat{k}$ 

If  $\alpha$  is the smallest positive integer for which  $\vec{a}, \vec{b}, \vec{c}$  are non-collinear, then the length of the median, in  $\triangle ABC$ , through A is:

(A) 
$$\frac{\sqrt{82}}{2}$$
 (B)  $\frac{\sqrt{62}}{2}$   
(C)  $\frac{\sqrt{69}}{2}$  (D)  $\frac{\sqrt{66}}{2}$ 

Official Ans. by NTA (A)

**Sol.**  $\overrightarrow{AB} \parallel \overrightarrow{AC}$  if  $\frac{1}{2} = \frac{\alpha - 4}{-6} = \frac{1}{2} \Rightarrow \alpha = 1$ 

 $\vec{a}, \vec{b}, \vec{c}$  are non-collinear for  $\alpha = 2$  (smallest positive integer)

Mid-point of BC = M $\left(\frac{5}{2}, 0, \frac{9}{2}\right)$ 

$$AM = \sqrt{\frac{9}{4} + 16 + \frac{9}{4}} = \frac{\sqrt{82}}{2}$$

A

16. The probability that a relation R from {x,y} to {x,y} is both symmetric and transitive, is equal to:

(A) 
$$\frac{5}{16}$$
 (B)  $\frac{9}{16}$   
(C)  $\frac{11}{16}$  (D)  $\frac{13}{16}$ 

Official Ans. by NTA (A)

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Sol. Total no. of relations = 
$$2^{2\times 2} = 16$$
  
Fav. relation =  $\phi$ , {(x, x)}, {(y, y)}, {(x, x)(y, y)}  
{(x, x), (y, y), (x, y)(y, x)}  
Prob. =  $\frac{5}{16}$ 

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- f .... 1 - 4<sup>1</sup> - ....

The number of values of  $a \in \mathbb{N}$  such that the 17. variance of 3, 7, 12 a, 43 – a is a natural number is: (A) 0 (B) 2 (C) 5 (D) infinite

Official Ans. by NTA (A)

Sol. Mean =13

Variance =  $\frac{9+49+144+a^2+(43-a)^2}{5} - 13^2 \in \mathbb{N}$ 

 $\Rightarrow \frac{2a^2 - a + 1}{5} \in \mathbb{N}$ 

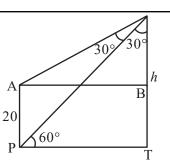
 $\Rightarrow$  2a<sup>2</sup> - a + 1 - 5n = 0 must have solution as natural numbers

its D = 40n - 7 always has 3 at unit place  $\Rightarrow$ D can't be perfect square So, a can't be integer.

18. From the base of a pole of height 20 meter, the angle of elevation of the top of a tower is 60°. The pole subtends an angle  $30^{\circ}$  at the top of the tower. Then the height of the tower is:

Official Ans. by NTA (4)	
(C) $20 + 10\sqrt{3}$	(D) 30
(A) 15 <del>√3</del>	(B) 20√3

Sol. 
$$PT = \frac{h}{\sqrt{3}} = AB$$
$$\frac{AB}{h - 20} = \sqrt{3}$$
$$h = 3(h - 20)$$
$$h = 30$$



19. Negation Boolean of the statement  $(p \lor q) \Rightarrow ((\sim r) \lor p)$  is equivalent to:

(A) 
$$p \land (\sim q) \land r$$
 (B)  $(\sim p) \land (\sim q) \land r$   
(C)  $(\sim p) \land q \land r$  (D)  $p \land q \land (\sim r)$ 

Official Ans. by NTA (C)

Sol. 
$$P \lor q \Longrightarrow (\sim r \lor p)$$
  
 $\equiv \sim (p \lor q) \lor (\sim r \lor p)$   
 $\equiv (\sim p \land \sim q) \lor (p \lor \sim r)$   
 $\equiv [\sim p \lor p) \land (\sim q \lor p)] \lor \sim r$   
 $\equiv [\sim q \lor p) \lor \sim r$   
Its negation is  $\sim p \land q \land r$   
20. Let  $n \ge 5$  be an integer. If  $9^n - 8n - 1 = 64 \alpha$  and  $6^n - 5n - 1 = 25 \beta$ , then  $\alpha - \beta$  is equal to:  
(A)  $1 + {}^{n}C_2 (8-5) + {}^{n}C_3 (8^2 - 5^2) + ... + {}^{n}C_n (8^{n-1} - 5^{n-1})$   
(B)  $1 + {}^{n}C_3 (8-5) + {}^{n}C_4 (8^2 - 5^2) + ... + {}^{n}C_n (8^{n-2} - 5^{n-2})$   
(C)  ${}^{n}C_3 (8-5) + {}^{n}C_4 (8^2 - 5^2) + ... + {}^{n}C_n (8^{n-2} - 5^{n-2})$   
(D)  ${}^{n}C_4 (8-5) + {}^{n}C_5 (8^2 - 5^2) + ... + {}^{n}C_n (8^{n-3} - 5^{n-3})$   
Official Ans. by NTA (C)

Sol. 
$$\alpha = \frac{(1+8)^n - 8n - 1}{64} = {}^nC_2 + {}^nC_38 + {}^nC_48^2 + ...$$
  
 $\beta = {}^nC_2 + {}^nC_35 + {}^nC_45^2 + ....$   
option (3) will be the answer.

**SECTION-B** 



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1. Let 
$$\vec{a} = \hat{i} - 2\hat{j} + 3\hat{k}$$
,  $\vec{b} = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{c}$  be a vector  
such that  $\vec{a} + (\vec{b} \times \vec{c}) = \vec{0}$  and  $\vec{b} \cdot \vec{c} = 5$ . Then, the  
value of  $3(\vec{c} \cdot \vec{a})$  is equal to\_\_\_\_.

#### Official Ans. by NTA (DROP)

**Sol.**  $\vec{a} + \vec{b} \times \vec{c} = 0$ 

 $\vec{a} \times \vec{b} + |\vec{b}|^2 \vec{c} - 5\vec{b} = 0$ It gives  $\vec{c} = \frac{1}{3}(10\hat{i} + 3\hat{j} + 2\hat{k})$ so  $3\vec{a}.\vec{c} = 10$ But it does not satisfy  $\vec{a} + \vec{b} \times \vec{c} = 0$ . This question has data error.

Alternate (Explanation) : According to given  $\vec{a} \& \vec{b}$  $\vec{a} \cdot \vec{b} = 1 - 2 + 3 = 2 \dots (i)$ but given equation  $\vec{a} = -(\vec{b} \times \vec{c})$  $\Rightarrow \vec{a} \perp \vec{b} \Rightarrow \vec{a} \cdot \vec{b} = 0$ which contradicts.

2. Let y = y(x), x > 1, be the solution of the differential equation  $(x-1)\frac{dy}{dx} + 2xy = \frac{1}{x-1}$ , with

$$y(2) = \frac{1 + e^4}{2e^4}$$
. If  $y(3) = \frac{e^{\alpha} + 1}{\beta e^{\alpha}}$ . then the value of

 $\alpha + \beta$  is equal to\_\_\_\_\_

Official Ans. by NTA (14)

Sol. 
$$\frac{dy}{dx} + \frac{2x}{x-1} \cdot y = \frac{1}{(x-1)^2}$$
  
 $y = \frac{1}{(x-1)^2} \left[ \frac{e^{2x} + 1}{2e^{2x}} \right]$   
 $y(3) = \frac{e^6 + 1}{8e^6}$   
 $\alpha + \beta = 14$ 

Let 3, 6, 9, 12,... upto 78 terms and 5, 9, 13, 17,... upto 59 terms be two series. Then, the sum of the terms common to both the series is equal to\_\_\_\_.

Official Ans. by NTA (2223)

**Sol.** For series of common terms

a=9, d=12, n=19

$$S_{19} = \frac{19}{2} [2(9) + 18(12)] = 2223$$

4. The number of solutions of the equation  $\sin x = \cos^2 x$  in the interval (0,10) is\_\_.

Official Ans. by NTA (4)

**Sol.** 
$$\sin^2 x + \sin x - 1 = 0$$

$$\sin x = \frac{-1 + \sqrt{5}}{2} = +ve$$

Only 4 roots

5. For real numbers 
$$a$$
,  $b$  ( $a > b > 0$ ), let

Area 
$$\left\{ (x, y) : x^2 + y^2 \le a^2 \text{ and } \frac{x^2}{a^2} + \frac{y^2}{b^2} \ge 1 \right\} = 30\pi$$

and

$$Area\left\{ (x,y): x^2 + y^2 \ge b^2 \text{ and } \frac{x^2}{a^2} + \frac{y^2}{b^2} \le 1 \right\} = 18\pi$$
  
Then the value of  $(a-b)^2$  is equal to\_\_.

Official Ans. by NTA (12)

- Sol. given  $\pi a^2 \pi ab = 30 \pi$  and  $\pi ab \pi b^2 = 18 \pi$ on subtracting, we get  $(a-b)^2 = a^2 - 2ab + b^2 = 12$
- 6. Let f and g be twice differentiable even functions on (-2, 2) such that  $f\left(\frac{1}{4}\right) = 0, f\left(\frac{1}{2}\right) = 0, f(1) = 1$

and  $g\left(\frac{3}{4}\right) = 0, g(1) = 2$  Then, the minimum number

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of solutions of f(x) g"(x) + f'(x)g'(x) = 0 in (-2,2) is equal to\_\_\_.

#### Official Ans. by NTA (4)

- **Sol.** Let  $h(x) = f(x) g'(x) \rightarrow 5$  roots
  - $\therefore$  f (x) is even  $\Rightarrow$

$$f\left(\frac{1}{4}\right) = f\left(\frac{1}{2}\right) = f\left(-\frac{1}{2}\right) = f\left(\frac{1}{4}\right) = 0$$
  
g(x) is even  $\Rightarrow g\left(\frac{3}{4}\right) = g\left(-\frac{3}{4}\right) = 0$ 

- g'(x) = 0 has minimum one root
- h'(x) has at last 4 roots
- 7. Let the coefficients of  $x^{-1}$  and  $x^{-3}$  in the expansion

of 
$$\left(2x^{\frac{1}{5}} - \frac{1}{x^{\frac{1}{5}}}\right)^{15}$$
, x > 0, be *m* and *n* respectively. If

r is a positive integer such  $mn^2 = {}^{15}$  C<sub>r</sub>. 2<sup>r</sup>, then the value of r is equal to\_\_\_.

### Official Ans. by NTA (5)

Sol. 
$$T_{r+1} = (-1)^r \cdot {}^{15}C_r \cdot 2^{15-r} x$$
  
 $m = {}^{15}C_{10} 2^5$   
 $n = -1$   
so  $mn^2 = {}^{15}C_5 2^5$ 

8. The total number of four digit numbers such that each of the first three digits is divisible by the last digit, is equal to\_\_\_\_\_.

### Official Ans. by NTA (1086)

**Sol.** Let the number is abcd, where a,b,c are divisible by d.

	No. of such numbers
d = 1,	$9 \times 10 \times 10 = 900$
d = 2	$4 \times 5 \times 5 = 100$
d = 3	$3 \times 4 \times 4 = 48$
d = 4	$2 \times 3 \times 3 = 18$

$$d = 5 1 \times 2 \times 2 = 4$$
  

$$d = 6, 7, 8, 9 4 \times 4 = 16$$
  
1086

9. Let  $M = \begin{bmatrix} 0 & -\alpha \\ \alpha & 0 \end{bmatrix}$ , where  $\alpha$  is a non-zero real number an  $N = \sum_{k=1}^{49} M^{2k}$ . If  $(I - M^2)N = -2I$ , then the positive integral value of  $\alpha$  is \_\_\_\_\_. Official Ans. by NTA (1)

Sol. 
$$M = \begin{bmatrix} 0 & -\alpha \\ \alpha & 0 \end{bmatrix}$$
;  $M^2 = \begin{bmatrix} -\alpha^2 & 0 \\ 0 & -\alpha^2 \end{bmatrix} = -\alpha^2 I$   
 $N = M^2 + M^4 + \dots + M^{98} = [-\alpha^2 + \alpha^4 - \alpha^6 + \dots]I$   
 $= -\alpha^2 \frac{(1 - (-\alpha^2)^{49})}{1 + \alpha^2} .I$   
 $I - M^2 = (1 + \alpha^2) I$   
 $(I - M^2)N = -\alpha^2 (\alpha^{98} + 1) = -2$   
 $\alpha = 1$ 

10. Let f(x) and g(x) be two real polynomials of degree 2 and 1 respectively. If  $f(g(x)) = 8x^2 - 2x$ , and  $g(f(x)) = 4x^2 + 6x + 1$ , then the value of f(2) + g(2)is\_\_\_\_.

Official Ans. by NTA (18)

Sol. 
$$f(g(x) = 8x^2 - 2x$$
  
 $g(f(x) = 4x^2 + 6x + 1)$   
So,  $g(x) = 2x - 1$   
 $g(2) = 3$   
&  $f(x) = 2x^2 + 3x + 1$   
 $f(2) = 8 + 6 + 1 = 15$   
Ans. 18