

FINAL JEE-MAIN EXAMINATION – JUNE, 2022

(Held On Monday 27th June, 2022)

PHYSICS

SECTION-A

The SI unit of a physical quantity is pascal-second.

(B) $[ML^{-1}T^{-2}]$

(D) $[M^{-1}L^{3}T^{0}]$

The dimensional formula of this quantity will be

TEST PAPER WITH SOLUTION

TIME: 3:00 PM to 6:00 PM

3. When a ball is dropped into a lake from a height 4.9 m above the water level, it hits the water with a velocity v and then sinks to the bottom with the constant velocity v. It reaches the bottom of the lake 4.0 s after it is dropped. The approximate depth of the lake is :

(A) 19.6 m	(B) 29.4 m
(C) 39.2 m	(D) 73.5 m

Official Ans. by NTA (B)

Sol.
$$V^2 = 2 \times 9.8 \times 4.9$$

V = 9.8 m/s

4.

Depth = distance travelled in 3 seconds

 $= 9.8 \times 3 = 29.4$ m

One end of a massless spring of spring constant k and natural length l_0 is fixed while the other end is connected to a small object of mass m lying on a frictionless table. The spring remains horizontal on the table. If the object is made to rotate at an angular velocity ω about an axis passing through fixed end, then the elongation of the spring will be:

(A)
$$\frac{\mathbf{k} - \mathbf{m}\omega^2 l_0}{\mathbf{m}\omega^2}$$
 (B) $\frac{\mathbf{m}\omega \ l_0}{\mathbf{k} + \mathbf{m}\omega^2}$
(C) $\frac{\mathbf{m}\omega^2 l_0}{\mathbf{k} - \mathbf{m}\omega^2}$ (D) $\frac{\mathbf{k} + \mathbf{m}\omega^2 l_0}{\mathbf{m}\omega^2}$

Official Ans. by NTA (C)

(A) $[ML^{-1}T^{-1}]$

(C) $[ML^2T^{-1}]$

1.

Sol. Pascal second

$$\frac{F}{A}t = \frac{MLT^{-2}}{L^2}T = ML^{-1}T^{-1}$$

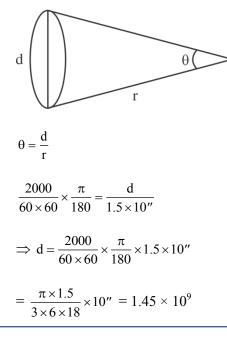
Official Ans. by NTA (A)

2. The distance of the Sun from earth is 1.5×10^{11} m and its angular diameter is (2000) s when observed from the earth. The diameter of the Sun will be :

(A) 2.45×10^{10} m (B) 1.45×10^{10} m (C) 1.45×10^{9} m (D) 0.14×10^{9} m

Official Ans. by NTA (C)

Sol.





Sol.

$$\mathbf{K} \Delta \mathbf{x} = \mathbf{m}(\ell_0 + \underline{\Delta}\mathbf{x})\mathbf{w}^2$$

$$\mathbf{K} \Delta \mathbf{x} = \mathbf{m} \,\ell_0 \,\mathbf{w}^2 + \mathbf{m} \mathbf{w}^2 \,\Delta \mathbf{x}$$

$$\Delta x = \frac{m\ell_0 w^2}{k - mw^2}$$

5. A stone tide to a string of length L is whirled in a vertical circle with the other end of the string at the centre. At a certain instant of time, the stone is at its lowest position and has a speed u. The magnitude of change in its velocity, as it reaches a position where the string is horizontal, is $\sqrt{x(u^2 - gL)}$. The value of x is

(B) 2

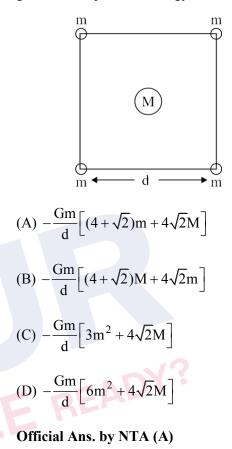
D) 5

Official Ans. by NTA (B)

Sol.
$$v = \sqrt{u^2 - 2gL}$$

 $\Delta v = \sqrt{u^2 + v^2}$
 $\Delta v = \sqrt{u^2 + v^2 - 2gL}$
 $\Delta v = \sqrt{2u^2 - 2gL}$
 $\Delta v = \sqrt{2(u^2 - gL)}$ $x = \sqrt{2(u^2 - gL)}$

6. Four spheres each of mass m form a square of side d (as shown in figure). A fifth sphere of mass M is situated at the centre of square. The total gravitational potential energy of the system is :

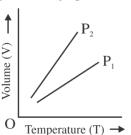


Sol.

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2

7. For a perfect gas, two pressures P_1 and P_2 are 9. shown in figure. The graph shows:



(A) $P_1 > P_2$

(B) $P_1 < P_2$

(C) $P_1 = P_2$

(D) Insufficient data to draw any conclusion

Official Ans. by NTA (A)

Sol. PV = nRT

 $\frac{V}{T} = \frac{nR}{P}$ $\frac{nR}{P_1} < \frac{nR}{P_2}$ $P_2 < P_1$

- According to kinetic theory of gases, 8.
 - A. The motion of the gas molecules freezes at 0°C
 - B. The mean free path of gas molecules decreases if the density of molecules is increased.
 - C. The mean free path of gas molecules increases if temperature is increased keeping pressure constant.
 - D. Average kinetic energy per molecule per degree
 - of freedom is $\frac{3}{2}k_{B}T$ (for monoatomic gases)

Choose the most appropriate answer from the options given below:

(A) A and C only	(B) B and C only
------------------	------------------

(C) A and B only (D) C and D only

Official Ans. by NTA (B)

Sol.
$$\lambda = \frac{kT}{\sqrt{2}\pi d^2 P}$$

A lead bullet penetrates into a solid object and melts. Assuming that 40% of its kinetic energy is used to heat it, the initial speed of bullet is:

(Given, initial temperature of the bullet = 127° C, Melting point of the bullet = 327° C,

Latent heat of fusion of lead = $2.5 \times 10^4 \text{J Kg}^{-1}$,

Specific heat capacity of lead = 125J/kg K)

(A) 125 ms^{-1} (B) 500 ms^{-1}

(C) 250 ms^{-1} (D) 600 ms^{-1}

Official Ans. by NTA (B)

Sol.
$$m \times 125 \times 200 + m \times 2.5 \times 10^4 = \frac{1}{2}mv^2 \times \frac{40}{100}$$

$$V = 500 \text{ m/s}$$

The equation of a particle executing simple 10. harmonic motion is given by $x = \sin \pi \left(t + \frac{1}{2} \right) m$. At t = 1s, the speed of particle will be (Given : $\pi = 3.14$) (A) 0 cm s^{-1} (B) 157 cm s^{-1} (C) 272 cm s^{-1} (D) 314 cm s^{-1}

Official Ans. by NTA (B)

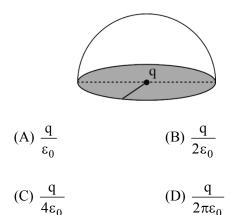
Sol.
$$x = \sin \pi \left(t + \frac{1}{3} \right)$$

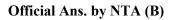
 $x = \sin \left(\pi t + \frac{\pi}{3} \right)$
 $V = \frac{dx}{dt} = \cos \left(\pi t + \frac{\pi}{3} \right) \pi$
 $= -\pi \times \frac{1}{2} = 157 \text{ cm/s}$

Give yourself an extra edge



11. If a charge q is placed at the centre of a closed hemispherical non-conducting surface, the total flux passing through the flat surface would be :





Sol.



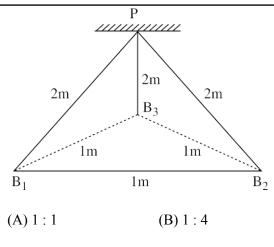
Total flux through complete spherical surface is $\frac{q}{\varepsilon_0}$.

So the flux through curved surface will be $\frac{q}{2\varepsilon_0}$. The flux through flat surface will be zero.

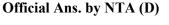
Remark : Electric flux through flat surface is zero but no option is given, option is available for electric flux passing through curved surface.

12. Three identical charged balls each of charge 2C are suspended from a common point P by silk threads of 2m each (as shown in figure). They form an equilateral triangle of side 1m.

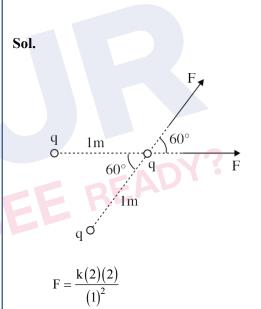
> The ratio of net force on a charged ball to the force between any two charged balls will be :



(D) $\sqrt{3}$:1



(C) $\sqrt{3}:2$



(F = Force between two charges).

F = 4k

$$F_{net} = 2F \cos 30^\circ = 2 \cdot F \cdot \frac{\sqrt{3}}{2} = F \sqrt{3}$$

 $(F_{net} = Net electrostatic force on one charged ball)$

$$\frac{\mathrm{F}_{\mathrm{net}}}{\mathrm{F}} = \frac{\sqrt{3} \mathrm{F}}{\mathrm{F}} = \left(\sqrt{3}\right)$$

Remark: Net force on any one of the ball is zero. But no option given in options.

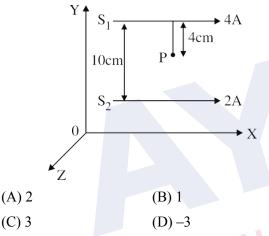
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13. Two long parallel conductors S₁ and S₂ are separated by a distance 10 cm and carrying currents of 4A and 2A respectively. The conductors are placed along x-axis in X-Y plane. There is a point P located between the conductors (as shown in figure).

A charge particle of 3π coulomb is passing through the point P with velocity

 $\vec{v} = (2\hat{i} + 3\hat{j})m/s$; where $\hat{i} \& \hat{j}$ represents unit vector along x & y axis respectively.

The force acting on the charge particle is $4\pi \times 10^{-5} (-x\hat{i} + 2\hat{j})N$. The value of x is :



Official Ans. by NTA (C)

Sol.

$$\vec{B}_{net} = B_1 - B_2 = \frac{\mu_0 \times 4}{2\pi [.04]} - \frac{\mu_0 \times 2}{2\pi [.06]}$$
$$\vec{B}_{net} = \frac{\mu_0}{2\pi} \left[\frac{200}{3} \right] (-\hat{k})$$
$$\vec{F} = q \left[\vec{v} \times \vec{B} \right]$$
$$= \left[3\pi \right] \left[\left(2\hat{i} + 3\hat{j} \right) \times \left(\frac{\mu_0}{2\pi} \right) \left(\frac{200}{3} \right) - \hat{k} \right]$$

Give yourself an extra edge

$$= 3\pi \times \frac{\mu_0}{2\pi} \left(\frac{200}{3}\right) \left[2 \times \hat{j} - 3(\hat{i})\right]$$
$$= (4\pi \times 10^{-7})(100)(-3\hat{i} + 2\hat{j})$$
$$= 4\pi \times 10^{-5} \times \left[-3\hat{i} + 2\hat{j}\right]$$

14. If L, C and R are the self inductance, capacitance and resistance respectively, which of the following does not have the dimension of time ?

(A) RC
(B)
$$\frac{L}{R}$$

(C) \sqrt{LC}
(D) $\frac{L}{C}$

Official Ans. by NTA (D)

Sol. $\left(\frac{L}{C}\right)$ does not have dimension of time. RC, $\frac{L}{P}$ are time constant while \sqrt{LC} is reciprocal

of angular frequency or having dimension of time.

15. Given below are two statements:

Statement I : A time varying electric field is a source of changing magnetic field and vice-versa. Thus a disturbance in electric or magnetic field creates EM waves.

Statement II : In a material medium. The EM wave travels with speed $v = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$.

In the light of the above statements, choose the correct answer from the options given below:

- (A) Both statement I and statement II are true.
- (B) Both statement I and statement II are false.
- (C) Statement I is correct but statement II is false.

(D) Statement I is incorrect but statement II is true. Official Ans. by NTA (C)

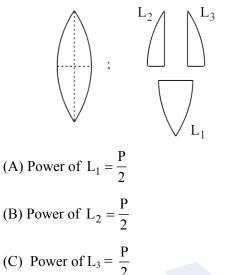
Sol. The statement II is wrong as the velocity of εm

wave in a medium is
$$\frac{1}{\sqrt{\mu\epsilon}} = \frac{1}{\sqrt{\mu_0\mu_r\epsilon_0\epsilon_r}}$$



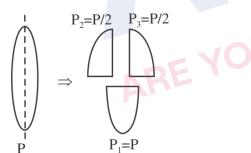


16. A convex lens has power P. It is cut into two halves along its principal axis. Further one piece (out of the two halves) is cut into two halves perpendicular to the principal axis (as shown in figure). Choose the incorrect option for the reported pieces.



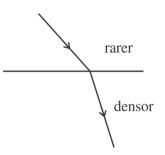
- (D) Power of $L_1 = P$
- Official Ans. by NTA (A)

Sol.



- 17. If a wave gets refracted into a denser medium, then which of the following is true?
 - (A) wavelength speed and frequency decreases.
 - (B) wavelength increases, speed decreases and frequency remains constant.
 - (C) wavelength and speed decreases but frequency remains constant.
 - (D) wavelength, speed and frequency increases.

Official Ans. by NTA (C)



Sol.

No change in frequency but speed and wave-length decreases.

18. Given below are two statements:

Statement I : In hydrogen atom, the frequency of radiation emitted when an electron jumps from lower energy orbit (E₁) to higher energy orbit (E₂), is given as $hf = E_1 - E_2$.

Statement-II : The jumping of electron from higher energy orbit (E₂) to lower energy orbit (E₁) is associated with frequency of radiation given as f = $(E_2 - E_1)/h$

This condition is Bohr's frequency condition.

In the light of the above statements, choose the correct answer from the options given below:

- (A) Both statement I and statement II are true.
- (B) Both statement I and statement II are false
- (C) Statement I is correct but statement II is false
- (D) Statement I is incorrect but statement II is true.

Official Ans. by NTA (D)

Sol. When electron jump from lower to higher energy level, energy absorbed so statement-I incorrect. When electron jump from higher to lower energy level, energy of emitted photon

 $\mathbf{E} = \mathbf{E}_2 - \mathbf{E}_1$

$$hf = E_2 - E_1 \implies f = \frac{E_2 - E_1}{h}$$

so statement-II is correct.

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19. For a transistor to act as a switch, it must be operated in 1. (A) Active region (B) Saturation state only (C) Cut-off state only (D) Saturation and cut-off state Official Ans. by NTA (D) Sol. Transistor act as a switch in saturation and cut of region. 20. We do not transmit low frequency signal to long distances because (a) The size of the antenna should be comparable to signal wavelength which is unreal solution for a signal of longer wavelength. (b) Effective power radiated by a long wavelength baseband signal would be high. (c) We want to avoid mixing up signals transmitted by different transmitter simultaneously. (d) Low frequency signal can be sent to long \Rightarrow distances by superimposing with a high frequency wave as well.

Therefore, the most suitable options will be :

- (A) All statements are true
- (B) (a), (b) and (c) are true only
- (C) (a), (c) and (d) are true only
- (D)(b), (c) and (d) are true only

Official Ans. by NTA (C)

- For low frequency or high wavelength size Sol. (a) of antenna required is high.
 - E P R is low for longer wavelength. (b)
 - yes we want to avoid mixing up signals (c) transmitted by different transmitter simultaneously.
 - Low frequency signals sent to long distance (d) by superimposing with high frequency.

SECTION-B

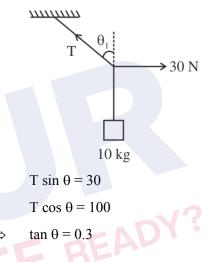
A mass of 10 kg is suspended vertically by a rope of length 5m from the roof. A force of 30 N is applied at the middle point of rope in horizontal direction. The angle made by upper half of the rope with vertical is $\theta = \tan^{-1} (x \times 10^{-1})$. The value of x is .

(Given $g = 10 \text{ m/s}^2$)

Official Ans. by NTA (3)

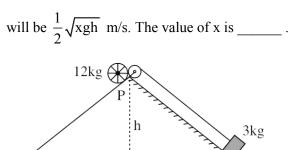
Sol.

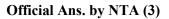
2.



A rolling wheel of 12 kg is on an inclined plane at position P and connected to a mass of 3 kg through a string of fixed length and pulley as shown in figure. Consider PR as friction free surface.

The velocity of centre of mass of the wheel when it reaches at the bottom Q of the inclined plane PQ







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Sol. Net loss in PE = Gain in KE

$$12 \text{ gh} - 3\text{gh} = \frac{1}{2}3v^{2} + \frac{1}{2}12v^{2} + \frac{1}{2}\left[12r^{2}\right]\left(\frac{v}{r}\right)^{2}$$

$$9\text{gh} = \frac{1}{2}\left[3 + 12 + 12\right]v^{2}$$

$$v^{2} = \frac{2\text{gh}}{3} \implies v = \frac{1}{2}\sqrt{\frac{8}{3}}\text{gh}$$

$$x = \frac{8}{3} \approx 3$$

3. A diatomic gas ($\gamma = 1.4$) does 400 J of work when it is expanded isobarically. The heat given to the gas in the process is _____ J.

Official Ans. by NTA (1400)

Sol.
$$Q = nC_p \Delta T = \frac{nv}{v-1} R\Delta T$$
$$Q = \frac{v}{v-1} \omega = \frac{1.4}{0.4} \times 400 = 1400 \text{ J}$$

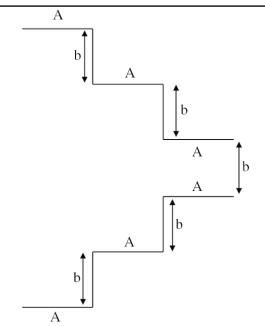
4. A particle executes simple harmonic motion. Its amplitude is 8 cm and time period is 6s. The time it will take to travel from its position of maximum displacement to the point corresponding to half of its amplitude, is ______ s.

Official Ans. by NTA (1)

Sol.
$$t = \frac{\Delta \phi}{\omega} = \frac{\pi/2 - \pi/6}{2\pi/6} = \frac{\pi/3}{\pi/3} = 1 \sec^{10}{100}$$

5. A paralle plate capacitor is made up of stair like structure with a palte area A of each stair and that is connected with a wire of length b, as shown in the figure. The capacitance of the arrangement is

$$\frac{x}{15} \frac{\varepsilon_0 A}{b}$$
. The value of x is _____



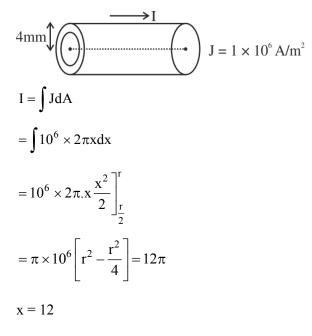
Official Ans. by NTA (23)

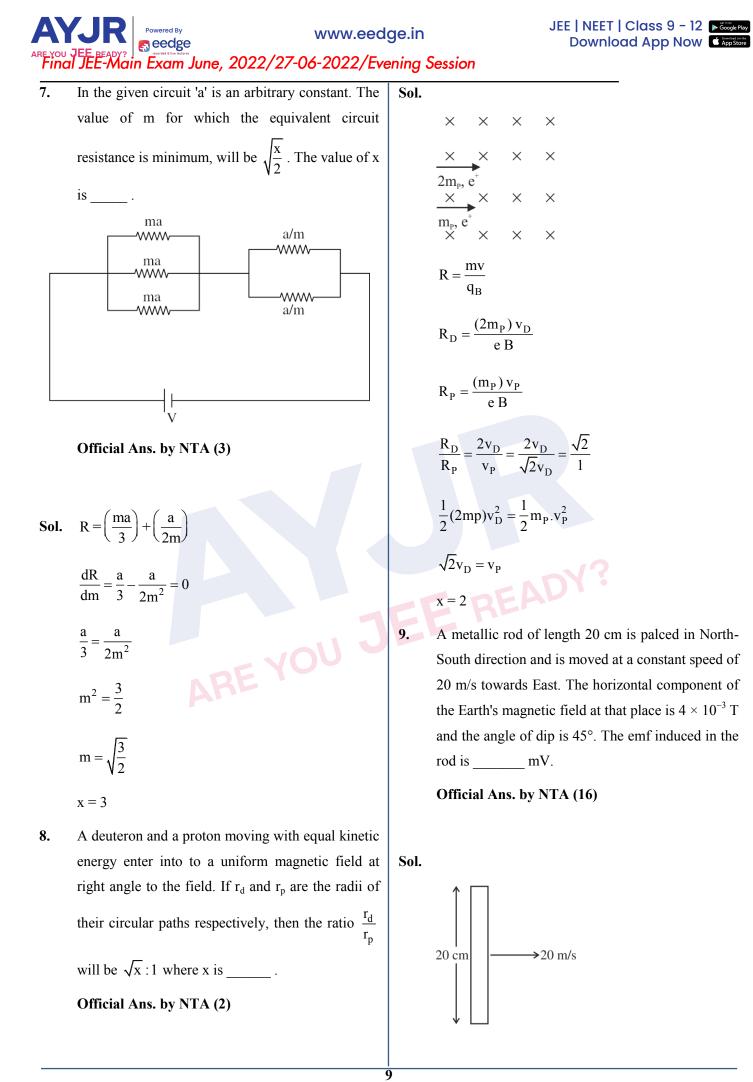
Sol. Parallel combination

$$\mathbf{c}_{eq} = \varepsilon_0 \mathbf{A} \left[\frac{1}{5b} + \frac{1}{3b} + \frac{1}{b} \right] = \frac{23}{15} \frac{\varepsilon_0 \mathbf{A}}{b}$$

6. The current density in a cylindrical wire of radius $r = 4.0 \text{ mm} \text{ is } 1.0 \times 10^6 \text{ A/m}^2$. The current through the outer portion of the wire between radial distances r/2 and r is x π A; where x is _____. Official Ans. by NTA (12)

Sol.

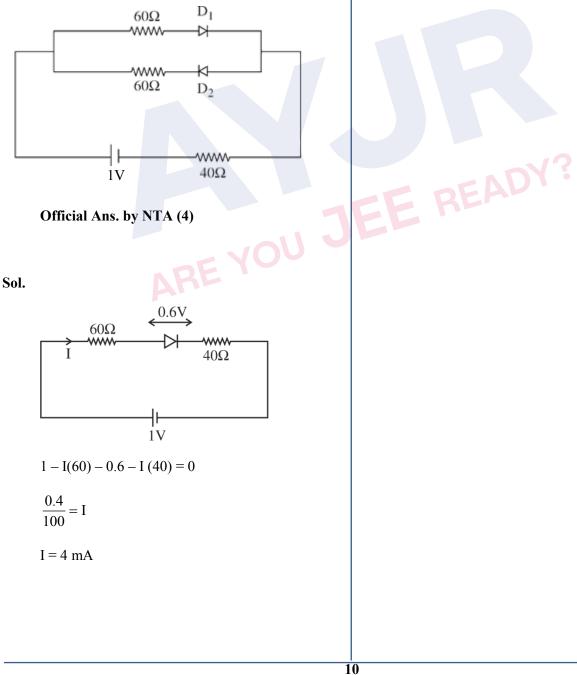




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- B_H = 4 × 10⁻³ T θ → 45° B_V = B_H ∈= (V × B) · ℓ = ((4 × 10⁻³)(20)) $\frac{20}{100}$ = 16 × 10⁻³ V = 16 mV
- 10. The cut-off voltage of the diodes (shown in figure) in forward bias is 0.6 V. The current through the resister of 40 Ω is _____ mA.





FINAL JEE-MAIN EXAMINATION - JUNE, 2022 (Held On Monday 27th June, 2022) TIME: 3:00 PM to 6:00 PM **TEST PAPER WITH SOLUTIONS** CHEMISTRY **SECTION-A** 2. Identify the **incorrect** statement for PCl₅ from the following. 1. Which amongst the given plots is the correct plot for pressure (p) vs density (d) for an ideal gas? (A) In this molecule, orbitals of phosphorous are $T_3 > T_2 > T_1$ assumed to undergo sp³d hybridization. (A) (B) The geometry of PCl₅ is trigonal bipyramidal. (C) PCl₅ has two axial bonds stronger than three р (atm) equatorial bonds. (D) The three equatorial bonds of PCl₅ lie in a $d(g \text{ cm}^{-3})$ plane. $T_3 > T_2 > T_1$ (B) y. Official Ans. by NTA (C) р (atm) In PCl₅, axial bonds are weaker than equatorial. Sol. $d(g \text{ cm}^{-3})$ 3. Statement I : Leaching of gold with cyanide ion $T_3 > T_2 > T_1$ (C) in absence of air $/ O_2$ leads to cyano complex of y Au(III). р Statement II : Zinc is oxidized during the (atm) displacement reaction carried out for gold $d(g \text{ cm}^{-3})$ extraction. $T_3 > T_2 > T$ (D) In the light of the above statements, choose the У correct answer from the options given below. р (A) Both Statement I and Statement II are correct (atm) (B) Both Statement I and Statement II are incorrect (C) Statement I is correct but Statement II is d(g cmincorrect Official Ans. by NTA (B) (D) Statement I is incorrect but Statement II is Sol. P vs d : correct $\mathbf{P} = \left(\frac{\mathbf{RT}}{\mathbf{M}}\right) \mathbf{d}$ Official Ans. by NTA (D) Statement-1 : wrong, Au⁺ is correct, not Au⁺³ Sol. Statement-2 : correct $T_3 > T_2 > T_1$



4.	The correct order of increasing intermolecular	7.	Given below are two statements: one is labelled as
	hydrogen bond strength is		Assertion A and the other is labelled as Reason R.
	(A) HCN $<$ H ₂ O $<$ NH ₃		Assertion A : Flourine forms one oxoacid.
	(B) HCN $<$ CH ₄ $<$ NH ₃		Reason R : Flourine has smallest size amongst all halogens and is highly electronegative
	(C) $CH_4 < HCN < NH_3$		In the light of the above statements, choose the
	(D) $CH_4 < NH_3 < HCN$		most appropriate answer from the options given
	Official Ans. by NTA (C)		below.(A) Both A and R are correct and R is the correct explanation of A.
Sol.	Order of H-Bonding		(B) Both A and R are correct but R is NOT the
	$CH_4 < HCN < NH_3$		correct explanation of A.
	NCH NCH		(C) A is correct but R is not correct.
	$H_2NH \dots NH_3$		(D) A is not correct but R is correct
5.	The correct order of increasing ionic radii is		Official Ans. by NTA (A)
	(A) $Mg^{2+} < Na^+ < F^- < O^{2-} < N^{3-}$	Sal	Both A and R are correct and R is the correct
		Sol.	explanation of A.
	(B) $N^{3-} < O^{2-} < F^- < Na^+ < Mg^{2+}$		
	(C) $F^- < Na^+ < O^{2-} < Mg^{2+} < N^{3-}$	8.	In 3d series, the metal having the highest M^{2+}/M
	(D) $Na^+ < F^- < Mg^{2+} < O^{2-} < N^{3-}$		standard electrode potential is
	Official Ans. by NTA (A)	2	(A) Cr (B) Fe
			(C) Cu (D) Zn Official Ans. by NTA (C)
Sol.	$N^{-3} > O^{-2} > F^{-} > Na^{+} > Mg^{+2}$ (Radii)		
	(Isoelectronic species)	Sol.	$Cr^{+2}/Cr \rightarrow -0.90 V$
($\mathrm{Fe}^{+2}/\mathrm{Fe} \rightarrow -0.44 \mathrm{V}$
6.	The gas produced by treating an aqueous solution		$Cu^{+2}/Cu \rightarrow +0.34 V$
	of ammonium chloride with sodium nitrite is		$Zn^{+2}/Zn \rightarrow -0.76 V$
	(A) NH_3 (B) N_2		So Ans. Cu ⁺² /Cu
	(C) N_2O (D) Cl_2	9.	The 'f' orbitals are half and completely filled, respectively in lanthanide ions
	Official Ans. by NTA (B)		(Given: Atomic no. Eu, 63; Sm, 62; Tm, 69; Tb,
			65; Yb, 70; Dy, 66]
Sol.	$NH_4Cl + NaNO_2 \rightarrow NH_4NO_2 + NaCl$		(A) Eu^{2+} and Tm^{2+} (B) Sm^{2+} and Tm^{3+}
~ • • •			(C) Tb^{4+} and Yb^{2+} (D) Dy^{3+} and Yb^{3+}
			Official Ans. by NTA (C)
	$N_2 + 2H_2O$		

ARE YOU JEE READY?

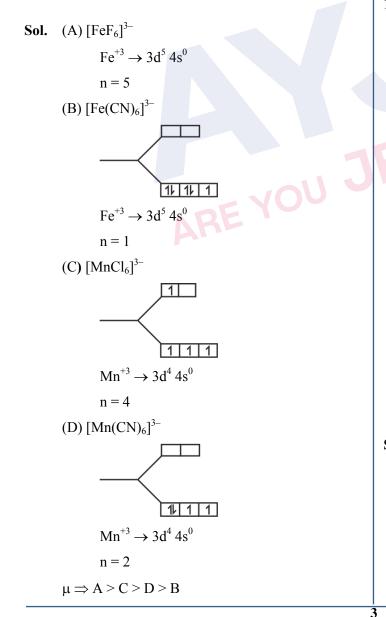
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Sol. $Tb \rightarrow 4f^{9}6s^{2}$ $Tb^{+4} \rightarrow 4f^{7}$ $Yb \rightarrow 4f^{14}6s^{2}$ $Yb^{+2} \rightarrow 4f^{14}$

- 10. Arrange the following coordination compounds in the increasing order of magnetic moments. (Atomic numbers: Mn = 25; Fe = 26)
 (A) [FeF₆]³⁻
 (B) [Fe(CN)₆]³⁻
 (C) [MnCl₆]³⁻ (high spin)
 - (D) $[Mn(CN)_6]^{3-}$

(A) A < B < D < C
(B) B < D < C < A
(C) A < C < D < B
(D) B < D < A < C
Official Ans. by NTA (B)

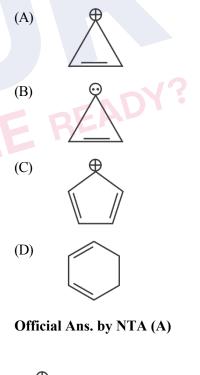


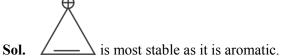
11. On the surface of polar stratospheric clouds, hydrolysis of chlorine nitrate gives A and B while its reaction with HCl produces B and C. A, B and C are, respectively
(A) HOCl, HNO₃, Cl₂
(B) Cl₂, HNO₃, HOCl
(C) HClO₂, HNO₂, HOCl
(D) HOCl, HNO₂, Cl₂O

Sol. O_{μ} N - O - Cl + H₂O \longrightarrow O_{μ} N - OH + HOCl OH (B) (A) O_{μ} N - O - Cl + HCl \longrightarrow O_{μ} N - OH + Cl₂ OH (B) (C)

12. Which of the following is most stable?

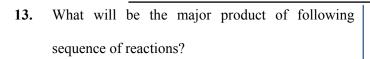
Official Ans. by NTA (A)

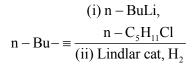


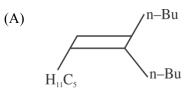


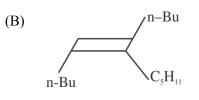


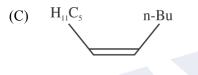
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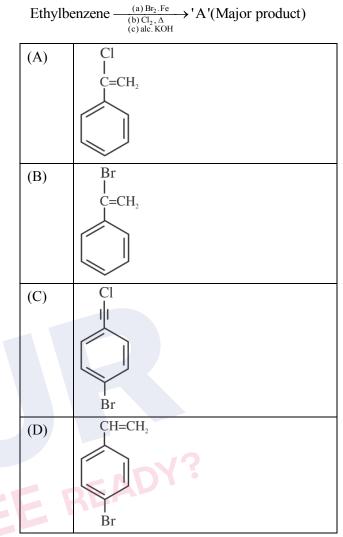


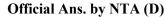


(D) C_3H_{11}



14. Product 'A' of following sequence of reactions is



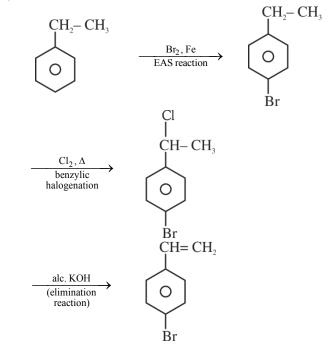


Sol.

nBuLi

(acid base

reaction)



Sol. $n - Bu - C \equiv CH$

 $n - Bu - C \equiv C^- Li^+$

$$n - C_5 H_{11} Cl \downarrow (SN reaction)$$

$$\overset{n-Bu}{\swarrow} \overset{C_{5}H_{11}}{\longleftarrow} \overset{H_{2}}{\underset{Catalyst}{\overset{H_{2}}{\leftarrow}}} n - Bu - C \equiv C - C_{5}H_{11}$$

Give yourself an extra edge

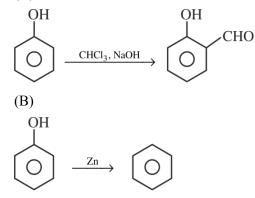
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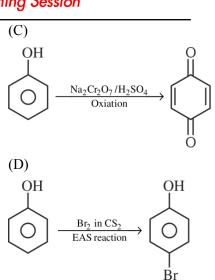
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- List I List II A. I. Br₂ in CS₂ OH OН CHO B. II. Na₂Cr₂O₇/H₂SO₄ OH C. III. Zn IV. CHCl₃/NaOH D. OH Choose the correct answer from the options given below: (A) A-IV, B-III, C-II, D-I
 - (B) A-IV, B-III, C-I, D-II (C) A-II, B-III, C-I, D-IV
 - (D) A-IV, B-II, C-III, D-I

Official Ans. by NTA (A)







- 16. Decarboxylation of all six possible forms of diaminobenzoic acids C₆H₃(NH₂)₂COOH yields three products A, B and C. Three acids give a product 'A', two acids gives a product 'B' and one acid give a product 'C'. The melting point of product 'C' is
 - (A) 63°C
 (B) 90°C

 (C) 104°C
 (D) 142°C

Official Ans. by NTA (D)



17. Which is true about Buna-N?

(A) It is a linear polymer of 1, 3-butadiene.

(B) It is obtained by copolymerization of 1, 3butadiene and styrene.

(C) It is obtained by copolymerization of 1, 3butadiene and acrylonitrile.

(D) The suffix N in Buna-N stands for its natural occurrence

Official Ans. by NTA (C)

15. Match List I with List II



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- Sol. It is copolymerization of 1, 3-butadiene and acrylonitrile.
- 18. Given below are two statements.

Statuents I: Maltose has two α -D-glucose units linked at C_1 and C_4 and is a reducing sugar.

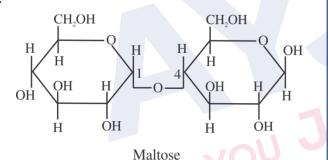
Statement II: Maltose has two monosaccharides: α -D-glucose and β -D-glucose linked at C₁ and C₆ and it is a non-reducing sugar.

In the light of the above statements, choose the correct answer from the options given below.

- (A) Both Statement I and Statement II are true
- (B) Both Statement I and Statement II are false
- (C) Statement I is true but Statement II is false
- (D) Statement I is false but Statement II is true

Official Ans. by NTA (C)

Sol.



19. Match List I with List Ii

List I	List II
A. Antipyretic	I. Reduces pain
B. Analgesic	II. Reduces stress
C. Tranquilizer	III. Reduces fever
D. Antacid	IV. Reduces acidity
	(Stomach)

Choose the correct answer from the options given below:

- (A) A-III, B-I, C-II, D-IV
- (B) A-III, B-I, C-IV, D-II
- (C) A-I, B-IV, C-II, D-III
- (D) A-I, B-III, C-II, D-IV

Official Ans. by NTA (A)

Sol.

A. Antipyretic	Reduces fever
B. Analgesic	Reduces pain
C. Tranquilizer	Reduces stress
D. Antacid	Reduces acidity (Stomach)

20. Match List I with List II

List I	List II
(Anion)	(Gas evolved on reaction with dil.
	$H_2SO_4)$
A. CO_3^{2-}	I. Colourless gas which turns lead
	acetate paper black
B. S ²⁻	II. Colourless gas which turns
	acidified potassium dichromate
	solution green.
C. SO_3^{2-}	III. Brown fumes which turns
	acidified KI solution containing
	starch blue.
D. NO ₂ ⁻	IV. Colourless gas evolved with
	brisk effervescence, which turns
E REA	lime water milky.

Choose the correct answer from the options given below:

(A) A-III, B-I, C-II, D-IV (B) A-II, B-I, C-IV, D-III (C) A-IV, B-I, C-III, D-II (D) A-IV, B-I, C-II, D-III Official Ans. by NTA (D)

 CO_3^{2-} will give $CO_2(g)$ which will turns lime water Sol. milky.

> S^{2-} will give H_2S (g), will turns lead acetate paper black

> SO_3^{2-} will give SO_2 (g), which will turns acidified potassium dichromate solution green.

> NO₂⁻ will give brown NO₂(g) will turn KI solution blue.

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116 g of a substance upon dissociation reaction, 1. yields 7.5 g of hydrogen, 60g of oxygen and 48.5 g of carbon. Given that the atomic masses of H, O and C are 1, 16 and 12 respectively. The data agrees with how many formulae of the following?

SECTION-B

(B) HCHO (A) CH₃COOH (C) CH₃OOCH₃ (D) CH₃CHO

Official Ans. by NTA (2)

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Sol. %H =
$$\frac{7.5}{116} \times 100 = 6.5$$

%O = $\frac{60}{116} \times 100 = 51.7$
%C = $\frac{48.5}{116} \times 100 = 41.8$

Relative atomicities = $H \Rightarrow 6.5$

$$O \Rightarrow \frac{51.7}{16} = 3.25$$
$$C \Rightarrow \frac{41.8}{12} = 3.5$$

Emperically formula is approx.. CH₂O (A) $C_2H_4O_2$ (B) CH_2O relate to this formula. Consider the following set of quantum numbers

	n	1	ml
A.	3	3	-3
B.	3	2	-2
C.	2	1	+1
D.	2	2	+2

2.

The number of correct sets of quantum numbers is

Official Ans. by NTA (2)

Sol. Quantum no. of set (B) and (C) can be correct. (A) and (D) are wrong as $n = \ell$ is not possible.

3. BeO reacts with HF in presence of ammonia to give [A] which on thermal decomposition produces [B] and ammonium fluoride. Oxidation state of Be in [A] is

Official Ans. by NTA (2)

Sol.

4. When 5 moles of He gas expand isothermally and reversibly at 300 K from 10 litre to 20 litre, the magnitude of the maximum work obtained is _____ J. [nearest integer] (Given: $R = 8.3 \text{ J K}^{-1} \text{mol}^{-1}$ and $\log 2 = 0.3010$)

Official Ans. by NTA (8630)

Sol. n = 5 mol
T = 300 K
V₁ = 10 L
V₂ = 20 L
w = -nRT
$$\ell n \frac{V_2}{V_1}$$

= -5 × 8.3 × 300 × $\ell n \frac{20}{10}$
= -8630.38 J

A solution containing 2.5×10^{-3} kg of a solute 5. dissolved in 75×10^{-3} kg of water boils at 373.535 K. The molar mass of the solute is $_____g mol^{-1}$. [nearest integer] (Given: K_b (H₂O) = 0.52 K Kg mol^{-1} , boiling point of water = 373.15K)

Official Ans. by NTA (45)



9.

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Sol. w = 2.5 g $K_b = 0.52$ $w_{solvent} = 75 \text{ g}$ M = Mol. Wt. of solute $T'_B = 373.535 \text{ K}$ $T^o_B = 373.15 \text{ K}$ $\Delta T_B = 0.385 = K_b \text{ molality}$ $0.385 = 0.52 \times \left(\frac{2.5}{M} \times \frac{1000}{75}\right)$

 $M = 45 \text{ g mol}^{-1}$

- 6. pH value of 0.001 M NaOH solution is _____ Official Ans. by NTA (11)
- **Sol.** 0.001 M NaOH $[OH^-] = 10^{-3}$ pOH = 3pH = 11
- 7. For the reaction taking place in the cell: Pt(s) | H₂(g) | H⁺(aq) || Ag⁺(aq) | Ag(s) $E^{o}_{Cell} = +0.5332 \text{ V.}$ The value of $\Delta_{f}G^{0}$ is _____ kJ mol⁻¹. (in nearest integer) Official Ans. by NTA (51)

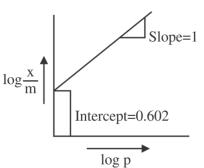
Sol.
$$\frac{1}{2}H_2 + Ag^+ \rightarrow H^+ + Ag$$
$$\Delta G^\circ = -nE^\circ F$$
$$= -1 \times 0.5332 \times 96500 J$$
$$= -51.35 kJ$$
$$(n = 2 \text{ for } H_2 + 2Ag^+ \rightarrow 2H^+ + 2Ag$$

It has been found that for a chemical reaction with rise in temperature by 9K the rate constant gets doubled. Assuming a reaction to be occurring at 300 K, the value of activation energy is found to be kJ mol⁻¹. [nearest integer]

(Given $\ln 10 = 2.3$, $R = 8.3 \text{ JK}^{-1}\text{mol}^{-1}$, $\log 2 = 0.30$) Official Ans. by NTA (59)

Sol.
$$\log_{10} \frac{K_2}{K_1} = \frac{E_a}{2.303R} \left(\frac{1}{300} - \frac{1}{309} \right)$$

 $0.3 = \frac{E_a}{2.303 \times 8.3} \left(\frac{9}{300 \times 309} \right)$
 $E_a = \frac{0.3 \times 2.303 \times 8.3 \times 300 \times 309}{9}$
 $= 59065.04 J$
 $E_a = 59.06 kJ$



If the initial pressure of a gas is 0.03 atm, the mass of the gas adsorbed per gram of the adsorbent is $___ \times 10^{-2}$ g.

Official Ans. by NTA (12)

Sol.
$$\frac{x}{m} = kP^{\frac{1}{n}}$$

 $\log \frac{x}{m} = \log k + \frac{1}{n} \log P$
From graph
 $Slope = \frac{1}{n} = 1 \Longrightarrow n = 1$
Intercept = log k = 0.602
k = 4
 $\frac{x}{m} = 4 \times (0.03)^{\frac{1}{1}}$
 $\frac{x}{m} = 12 \times 10^{-2}$

- 10. 0.25 g of an organic compound containing chlorine gave 0.40 g of silver chloride in Carius estimation. The percentage of chlorine present in the compound is ______. [in nearest integer] (Given: Molar mass of Ag is 108 g mol⁻¹ and that of Cl is 35.5 g mol⁻¹)
 Official Ans. by NTA (40)
- **Sol.** wt. of organic compound = 0.25 g

mass of Cl =
$$\frac{35.5}{143.5} \times 0.4$$
g

mass % of Cl in the organic compound

$$=\frac{35.5\times0.4}{143.5\times0.25}\times100$$

= 39.58%



FINAL JEE-MAIN EXAMINATION – JUNE, 2022(Held On Monday 27th June, 2022)TIME : 3 : 00 PM to 6 : 00 PMMATHEMATICSTEST PAPER WITH SOLUTIONSECTION-AI. The number of points of intersection of
$$|7-(4+3i)|=2$$
 and $|2|+|7-4|=6$, $z \in C$ is :
 $(A) 0$ (B) 1
 $(C) 2$ (D) 3Official Ans. by NTA (C)Sol. $C: (x-4)^2 + (y-3)^2 = 4$
 $E: $\frac{(x-2)^2}{9} + \frac{y^2}{5} = 1$ $- \frac{1}{(-1,0)} + \frac{(2,0)}{(2,0)} + \frac{(2,0)}{(5,0)}$ Lower Extremity of vertical diameter of
circle $\rightarrow (4,1)$ Put in clipse $= \frac{(4-2)^2}{95} + \frac{1}{5} = 1$ $= \frac{4}{9} + \frac{1}{5} = 1$ $= \frac{1}{295} - 1 < 0$ Two Solutions
Answer (C)Answer (C)2.Let $f(x) = \begin{vmatrix} a & -1 & 0 \\ ax^2 & ax & a \end{vmatrix}$ which the squares of all the values of a for
 $2f'(10) - f'(5) + 100 = 0$ is:
 $(A) 117$ (A) 117(B) 106
(C) 125(C) $2+\sqrt{3}$ (Dificial Ans. by NTA (B)$



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- Sol. $a = \alpha i\beta$; $\alpha \in \mathbb{R}$; $\beta \in \mathbb{R}$ 4ix + (1 + i) y = 0 and $8\left(\cos\frac{2\pi}{3} + i\sin\frac{2\pi}{3}\right)x + \overline{a}y = 0$ $\begin{vmatrix} 4i & 1+i \\ 8e^{i2\pi/3} & \overline{a} \end{vmatrix} = 0$ $\Rightarrow 4i \overline{a} - (1 + i) 8e^{i2\pi/3} = 0$ $\Rightarrow 4i (\alpha + i\beta) - 8 (1 + i) \left(\frac{-1 + i\sqrt{3}}{2}\right) = 0$ $\Rightarrow i\alpha - \beta + 1 + \sqrt{3} + i (1 - \sqrt{3}) = 0$ $\Rightarrow \beta = \sqrt{3} + 1$ $\alpha = \sqrt{3} - 1$ So, $\frac{\alpha}{\beta} = \frac{\sqrt{3} - 1}{\sqrt{3} + 1} = 2 - \sqrt{3}$
- 4. Let A and B be two 3×3 matrices such that AB= I and $|A| = \frac{1}{8}$ then |adj(Badj(2A))| is equal to (A) 16 (B) 32 (C) 64 (D) 128

Official Ans. by NTA (C)

Sol. AB = i

$$|adj (B adj (2A)| = |B adj (2A)|^{2}$$

$$= |B|^{2} |adj (2A)|^{2}$$

$$= |B|^{2} (|2A|^{2})^{2} = |B|^{2} (2^{6} |A|^{2})^{2}$$

$$|A| = \frac{1}{8} and |AB| = 1 \implies |A| |B| = 1$$

$$\implies \frac{1}{8} |B| = 1$$

$$\implies |B| = 8$$
required value = 64
5. Let $S = 2 + \frac{6}{7} + \frac{12}{7^{2}} + \frac{20}{7^{3}} + \frac{30}{7^{4}} + \dots$ then 4S is equal to

$$(A) \left(\frac{7}{3}\right)^{2} \qquad (B) \frac{7^{3}}{3^{2}}$$

$$(C) \left(\frac{7}{3}\right)^{3} \qquad (D) \frac{7^{2}}{3^{3}}$$
Official Ans. by NTA (C)

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Sol.	S = 2 + $\frac{6}{7}$ + $\frac{12}{7^2}$ + $\frac{20}{7^3}$ + $\frac{30}{7^4}$ +
	Considering infinite sequence,
	$S = 2 + \frac{6}{7} + \frac{12}{7^2} + \frac{20}{7^3} + \frac{30}{7^4} + \dots$
	$\frac{S}{7} = \frac{2}{7} + \frac{6}{7^2} + \frac{12}{7^3} + \frac{20}{7^4} + \dots$
\Rightarrow	$\frac{6S}{7} = 2 + \frac{4}{7} + \frac{6}{7^2} + \frac{8}{7^3} + \frac{10}{7^4} + \dots$
\Rightarrow	$\frac{6S}{7^2} = \frac{2}{7} + \frac{4}{7^2} + \frac{6}{7^3} + \frac{8}{7^4} + \dots$
	$\frac{6S}{7}\left(1-\frac{1}{7}\right) = 2 + \frac{2}{7} + \frac{2}{7^2} + \frac{2}{7^3} + \dots$
\Rightarrow	$\frac{6^2 S}{7^2} = \frac{2}{1 - \frac{1}{7}} = \frac{2}{6} \times 7$
\Rightarrow	$\mathbf{S} = \frac{2 \times 7^3}{6^3} \Longrightarrow 4\mathbf{S} = \frac{7^3}{3^3} = \left(\frac{7}{3}\right)^3$
6.	If $a_1, a_2, a_3 \dots$ and $b_1, b_2, b_3 \dots$ are A.P. and
	$a_1 = 2$, $a_{10} = 3$, $a_1b_1 = 1 = a_{10}b_{10}$ then a_4b_4 is equal to
	(A) $\frac{35}{27}$ (B) 1
	27 28
	(C) $\frac{27}{-1}$ (D) $\frac{26}{-1}$
	(C) $\frac{27}{28}$ (D) $\frac{28}{27}$ Official Ans. by NTA (D)
	(C) $\frac{27}{28}$ (D) $\frac{23}{27}$ Official Ans. by NTA (D)
Sol.	20
Sol.	Official Ans. by NTA (D) $a_1, a_2, a_3 \dots A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots, A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$
Sol.	Official Ans. by NTA (D) $a_1, a_2, a_3, \dots, A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots, A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}; d_1 \& d_2$ are common differences respectively]
Sol.	Official Ans. by NTA (D) $a_1, a_2, a_3, \dots, A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots, A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}; d_1 \& d_2$ are common differences respectively] $a_4.b_4 = (2+3d_1)(\frac{1}{2}+3d_2)$
Sol.	Official Ans. by NTA (D) $a_1, a_2, a_3, \dots, A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots, A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}; d_1 \& d_2$ are common differences respectively]
Sol.	Official Ans. by NTA (D) $a_1, a_2, a_3, \dots, A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots, A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}; d_1 \& d_2$ are common differences respectively] $a_4.b_4 = (2+3d_1)(\frac{1}{2}+3d_2)$
Sol. 7.	Official Ans. by NTA (D) $a_1, a_2, a_3 \dots A.P.$; $a_1 = 2$; $a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots A.P.$; $b_1 = \frac{1}{2}$; $b_{10} = \frac{1}{3}$; $d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}$; d_1 & d_2 are common differences respectively] $a_4.b_4 = (2+3d_1)(\frac{1}{2}+3d_2)$ $= (2+\frac{1}{3})(\frac{1}{2}-\frac{1}{18})$
	Official Ans. by NTA (D) $a_1, a_2, a_3 \dots A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}; d_1 \& d_2$ are common differences respectively] $a_4.b_4 = (2 + 3d_1)(\frac{1}{2} + 3d_2)$ $= (2 + \frac{1}{3})(\frac{1}{2} - \frac{1}{18})$ $= (\frac{7}{3})(\frac{8}{18}) = \frac{28}{27}$
	Official Ans. by NTA (D) $a_1, a_2, a_3 \dots A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}; d_1 \& d_2$ are common differences respectively] $a_4.b_4 = (2+3d_1)(\frac{1}{2}+3d_2)$ $= (2+\frac{1}{3})(\frac{1}{2}-\frac{1}{18})$ $= (\frac{7}{3})(\frac{8}{18}) = \frac{28}{27}$ If m and n respectively are the number of local
	Official Ans. by NTA (D) $a_1, a_2, a_3 \dots A.P.; a_1 = 2; a_{10} = 3; d_1 = \frac{1}{9}$ $b_1, b_2, b_3, \dots, A.P.; b_1 = \frac{1}{2}; b_{10} = \frac{1}{3}; d_2 = \frac{-1}{54}$ [Using $a_1b_1 = 1 = a_{10}b_{10}; d_1 \& d_2$ are common differences respectively] $a_4.b_4 = (2+3d_1)(\frac{1}{2}+3d_2)$ $= (2+\frac{1}{3})(\frac{1}{2}-\frac{1}{18})$ $= (\frac{7}{3})(\frac{8}{18}) = \frac{28}{27}$ If m and n respectively are the number of local maximum and local minimum points of the

(C) (2, 2) (D) (3, 4)

Official Ans. by NTA (B)

9.



Sol. $m = L \cdot max$ $N = L \cdot min$ $f(x) = \int_{-\infty}^{x^2} \frac{t^2 - 5t + 4}{2 + e^t} dt$ $f'(x) = \frac{\left(x^4 - 5x^2 + 4\right)2x}{2 + e^{x^2}} = \frac{2x\left(x^2 - 1\right)\left(x^2 - 4\right)}{2 + e^{x^2}}$ $=\frac{2x(x-1)(x+1)(x-2)(x+2)}{2+e^{x^2}}$ 2 L.min L.max min max min so, m = 2and n = 3Let f be a differentiable function in $\left(0, \frac{\pi}{2}\right)$. 8. If $\int_{-\infty}^{1} t^2 f(t) dt = \sin^3 x + \cos x$ then $\frac{1}{\sqrt{3}} f'\left(\frac{1}{\sqrt{3}}\right)$ is equal to : (A) $6 - 9\sqrt{2}$ (B) $6 - \frac{9}{\sqrt{2}}$ (C) $\frac{9}{2} - 6\sqrt{2}$ (D) $\frac{9}{\sqrt{2}} - 6$ Official Ans. by NTA (B) **Sol.** At right hand vicinity of x = 0 given equation does not satisfy :: LHS = $\int_{t^{-}}^{1} t^{2} f(t) dt = 0$, RHS = $\lim_{x \to 0^{+}} (\sin^{3} x + \cos x) = 1$

LHS \neq RHS hence data given in question is wrong hence BONUS

Correct data should have been

$$\int_{\cos x}^{1} t^{2} f(t) dt = \sin^{3} x + \cos x - 1$$

Calculation for option
differentiating both sides
 $-\cos^{2} x f(\cos x).(-\sin x) = 3\sin^{2} x.\cos x - \sin x$

 $\Rightarrow f(\cos x) = 3 \tan x - \sec^2 x$ $\Rightarrow f'(\cos x)(-\sin x) = 3\sec^2 x - 2\sec^2 x \tan x$ $\Rightarrow f'(\cos x)\cos x = \frac{2}{\cos^2 x} - \frac{3}{\sin x \cdot \cos x}$ When $\cos x = \frac{1}{\sqrt{3}}$; $\sin x = \frac{\sqrt{2}}{\sqrt{3}}$

$$\therefore f'\left(\frac{1}{\sqrt{3}}\right)\frac{1}{\sqrt{3}} = 6 - \frac{9}{\sqrt{2}}.$$

The integral $\int_{0}^{1} \frac{1}{\gamma^{\left\lfloor \frac{1}{x} \right\rfloor}} dx$, where [.] denotes the greatest integer function is equal to

(A)
$$1+6\log_{e}\left(\frac{6}{7}\right)$$
 (B) $1-6\log_{e}\left(\frac{6}{7}\right)$
(C) $\log_{e}\left(\frac{7}{6}\right)$ (D) $1-7\log_{e}\left(\frac{6}{7}\right)$

Official Ans. by NTA (A)

Sol.

$$\int_{0}^{1} \frac{1}{7^{\left[\frac{1}{x}\right]}} dx = -\int_{1}^{0} \frac{1}{7^{\left[\frac{1}{x}\right]}} dx$$

$$= (-1) \left[\int_{1}^{1/2} \frac{1}{7} dx + \int_{1/2}^{1/2} \frac{1}{7^{2}} dx + \int_{1/3}^{1/4} \frac{1}{7^{3}} dx + \dots \infty \right]$$

$$= \left(\frac{1}{7} + \frac{1}{2.7^{2}} + \frac{1}{3.7^{3}} + \dots \infty \right) - \left(\frac{1}{7.2} + \frac{1}{7^{2}.3} + \frac{1}{7^{2}.4} \dots \infty \right)$$

$$= -\ln \left(1 - \frac{1}{7} \right) - 7 \left(\frac{1}{7^{2}.2} + \frac{1}{7^{3}.3} + \frac{1}{7^{4}.4} + \dots \infty \right)$$

$$\left[as \ln(1 + x) = x - \frac{x^{2}}{2} + \frac{x^{3}}{3} - \frac{x^{4}}{4} \dots \infty \right]$$

$$= -\ln \frac{6}{7} - 7 \left(-\ln \left(1 - \frac{1}{7} \right) - \frac{1}{7} \right)$$

$$= 6 \ln \frac{6}{7} + 1$$

10. If the solution curve of the differential equation $((\tan^{-1} y) - x)dy = (1+y^2)dx$ passes through the point (1, 0) then the abscissa of the point on the curve whose ordinate is tan (1) is :

(A) 2e (B)
$$\frac{2}{e}$$

(C) 2 (D) $\frac{1}{e}$

Official Ans. by NTA (B)

Sol.
$$\frac{dx}{dy} + \frac{x}{1+y^2} = \frac{\tan^{-1} y}{1+y^2}$$

I.f = $e^{\int \frac{1}{1+y^2} dy} = e^{\tan^{-1} y}$
 $xe^{\tan^{-1} y} = \int \frac{\tan^{-1} y}{1+y^2} e^{\tan^{-1} y} dy$

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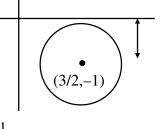
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$$x \cdot e^{\tan^{-1}y} = (\tan^{-1}y - 1)e^{\tan^{-1}y} + c$$

$$\therefore (1, 0) \text{ lise exit } c = 2.$$
For $y = \tan 1 \Rightarrow x = \frac{2}{c}$
11. If the equation of the parabola, whose vertex is at (5, 4) and the directrix is $3x + y - 29 = 0$, is $x^2 + ay^2 + bxy + cx + dy + k = 0$ then $a + b + c + d + k$ is equal to (A) 575 (B) -575 (C) 576 (D) -576 Official Ans. by NTA (D)
Sol. Vertex (5,4)
Directrix : $3x + y - 29 = 0$
Co-ordinates of B (foot of directrix)
 $\frac{x-5}{3} = \frac{y-4}{1} = -(\frac{15+4-29}{10}) = 1$
Directrix
 $a = 8, y = 5$
 $S = (2, 3)$ (focus)
Equation of parabola
 $PS = PM$
so equation is $x^2 + 9y^2 - 6xy + 134x - 2y - 711 = 0$
 $a + b + c + d + k = 9 - 6 + 134 - 2 - 711 = -576$
12. The set of values of k for which the circle
 $C : 4x^2 + 4y^2 - 12x + 8y + k = 0$ lies inside the fourth quadrant and the point $(1, -\frac{1}{3})$ lies on or inside the circle C is :
(A) An empty set (B) $(6, \frac{95}{9}]$
(C) $\left[\frac{80}{9}, 10\right]$ (D) $(9, \frac{92}{9}]$
Official Ans. by NTA (D)
Sol. C : $4x^2 + 4y^2 - 12x + 8y + k = 0$
 $\Rightarrow x^2 + y^2 - 3x + 2y + (\frac{k}{4}) = 0$
 $Centre (\frac{3}{2}, -1); r = \sqrt{\frac{13-k}{2}} \Rightarrow k \le 13 ... (1)$

(i) Point
$$\left(1, \frac{-1}{3}\right)$$
 lies on or inside circle C
 $\Rightarrow S_1 \le 0 \Rightarrow k \le \frac{92}{9} \dots (2)$

(ii) C lies in 4^{th} quadrant



r < 1
⇒
$$\frac{\sqrt{13-k}}{2}$$
 < 1
⇒ k < 9 (3)
Hence (1) ∩ (2) ∩ (3) ⇒ k ∈ $\left(9, \frac{92}{9}\right)$

13. Let the foot of the perpendicular from the point (1, 2, 4) on the line $\frac{x+2}{4} = \frac{y-1}{2} = \frac{z+1}{3}$ be P. Then the distance of P from the plane 3x+4y+12z+23=0

(A) 5
(C) 4 READ (B)
$$\frac{50}{13}$$

(D) $\frac{63}{13}$

Official Ans. by NTA (A)

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Sol.

$$P(4\lambda-2, 2\lambda+1, 3\lambda+1) = 4, 2, 3$$

$$(1, 2, 4)$$

$$\frac{x+2}{4} = \frac{y-1}{2} = \frac{z+1}{3} = \lambda$$

$$(x, y, z) = (4\lambda - 2, 2\lambda + 1, 3\lambda - 1)$$

$$\overline{AP} = (4\lambda - 3) \hat{i} + (2\lambda - 1) \hat{j} + (3\lambda - 5) \hat{k}$$

$$\overline{b} = 4\hat{i} + 2\hat{j} + 3\hat{k}$$

$$\overline{AP} \cdot \overline{b} = 0$$

$$4(4\lambda - 3) + 2(2\lambda - 1) + 3(3\lambda - 5) = 0$$

$$29\lambda = 12 + 2 + 15 = 29$$

$$\lambda = 1$$

$$P = (2, 3, 2)$$

$$3x + 4y + 12z + 23 = 0$$

$$d = \left|\frac{6+12+24+23}{\sqrt{9+16+144}}\right|$$

$$d = \left|\frac{65}{13}\right| = 5$$
14. The shortest distance between the lines

$$\frac{x-3}{2} = \frac{y-2}{3} = \frac{z-1}{-1} \text{ and } \frac{x+3}{2} = \frac{y-6}{1} = \frac{z-5}{3} \text{ is :}$$

$$(A) \frac{18}{\sqrt{5}} \qquad (B) \frac{22}{3\sqrt{5}}$$

$$(C) \frac{46}{3\sqrt{5}} \qquad (D) 6\sqrt{3}$$
Official Ans. by NTA (A)
Sol.

$$\frac{x-3}{2} = \frac{y-2}{-1} = \frac{z-5}{-3}$$

$$A = (3, 2, 1) \qquad B = (-3, 6, 5)$$

$$\overrightarrow{n_1} = 2\hat{i} + 3\hat{j} - \hat{k}$$

$$\overrightarrow{n_2} = 2\hat{i} + \hat{j} - 3\hat{k}$$

$$\overrightarrow{BA} = 6\hat{i} - 4\hat{j} - 4\hat{k}$$
SHORTEST DISTANCE =
$$\frac{\overrightarrow{BA} \cdot \overrightarrow{n_1} \cdot \overrightarrow{n_2}}{\overrightarrow{n_1} \times \overrightarrow{n_2}}$$

$$= 10\hat{i} - 8\hat{j} - 4\hat{k}$$

$$(\overrightarrow{BA} \cdot \overrightarrow{n_1} \cdot \overrightarrow{n_2}) = 60 + 32 + 16 = 108$$

$$|\overrightarrow{n_1} \times \overrightarrow{n_2}| = \sqrt{100+64+16} = \sqrt{180}$$

$$S.D = \frac{108}{\sqrt{180}} = \frac{108}{6\sqrt{5}} = \frac{18}{\sqrt{5}}$$

15. Let \vec{a} and \vec{b} be the vectors along the diagonal of a parallelogram having area $2\sqrt{2}$. Let the angle between \vec{a} and \vec{b} be acute. $|\vec{a}|=1$ and $|\vec{a}.\vec{b}|=|\vec{a}\times\vec{b}|$. If $\vec{c}=2\sqrt{2}(\vec{a}\times\vec{b})-2\vec{b}$, then an angle between \vec{b} and \vec{c} is :

(A)
$$\frac{\pi}{4}$$
 (B) $-\frac{\pi}{4}$

C)
$$\frac{5\pi}{6}$$
 (D) $\frac{3\pi}{4}$

Official Ans. by NTA (D)

a Sol. Area = $\frac{1}{2} |\vec{a} \times \vec{b}| = 2\sqrt{2} \Rightarrow |\vec{a} \times \vec{b}| = 4\sqrt{2}$ $\vec{a} = 1$ and $\vec{a} \cdot \vec{b} = \vec{a} \times \vec{b}$ $\Rightarrow \cos \theta = \sin \theta$ $\Rightarrow \theta = \frac{\pi}{4}$ $\therefore \left| \vec{a} \times \vec{b} \right| = 4\sqrt{2} \implies \left| \vec{a} \right| \left| \vec{b} \right| \sin \frac{\pi}{4} = 4\sqrt{2}$ $\Rightarrow \left| \vec{b} \right| = 8$ Now, $\vec{c} = 2\sqrt{2} \left(\vec{a} \times \vec{b} \right) - 2\vec{b}$ $|\vec{c}| = \sqrt{(2\sqrt{2})^2 |\vec{a} \times \vec{b}|^2 + (2|\vec{b}|)^2} = 16\sqrt{2}$ Now, $\vec{\mathbf{b}}.\vec{\mathbf{c}} = -2\left|\vec{\mathbf{b}}\right|^2$ $\Rightarrow 8 \times 16\sqrt{2} \times \cos \alpha = -2.64$ $\Rightarrow \cos \alpha = -\frac{1}{\sqrt{2}} \Rightarrow \alpha = \frac{3\pi}{4}$



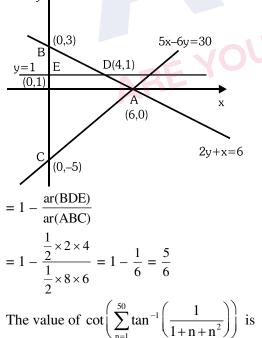
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- 16. The mean and variance of the data4, 5, 6, 6, 7, 8, x, y where x < y are 6, and $\frac{9}{4}$ respectively. Then $x^4 + y^2$ is equal to (A) 162 (B) 320 (C) 674 (D) 420 Official Ans. by NTA (B) Sol. mean $\overline{x} = \frac{4+5+6+6+7+8+x+y}{8} = 6$ $\Rightarrow x + y = 48 - 36 = 12$ Variance $= \frac{1}{8} (16+25+36+36+49+64+x^2+y^2) - 36 = \frac{9}{4}$ $\Rightarrow x^2 + y^2 = 80$
 - :. x = 4; y = 8 $x^4 + y^2 = 256 + 64 = 320$ If a point A(x, y) lies in the region
- 17. If a point A(x, y) lies in the region bounded by the y-axis, straight lines 2y + x = 6 and 5x 6y = 30, then the probability that y < 1 is :

$(A) \frac{1}{6}$	(B) $\frac{5}{6}$
(C) $\frac{2}{3}$	(D) $\frac{6}{7}$

Official Ans. by NTA (B)

Sol. Required probability = $\frac{ar(ADEC)}{ar(ABC)}$



(A) $\frac{26}{25}$ (C) $\frac{50}{51}$ (A) $\frac{26}{25}$ (B) $\frac{25}{26}$ (C) $\frac{50}{51}$ (D) $\frac{52}{51}$ Official Ans. by NTA (A)

Sol.
$$\tan^{-1} \frac{1}{1+n+n^2} = \tan^{-1} \left(\frac{(n+1)-n}{1+n(n+1)} \right)$$

$$= \tan^{-1} (n+1) - \tan^{-1} n$$
so, $\sum_{n=1}^{50} (\tan^{-1}(n+1) - \tan^{-1} n)$

$$= \tan^{-1} 51 - \tan^{-1} 1$$
cot $\left(\sum_{n=1}^{50} \tan^{-1} \left(\frac{1}{1+n+n^2} \right) \right) = \cot (\tan^{-1} 51 + \tan^{-1} 1)$

$$= \frac{1}{\tan(\tan^{-1} 51 - \tan^{-1} 1)} = \frac{1+51 \times 1}{51-1} = \frac{52}{50} = \frac{26}{25}$$

19. $\alpha = \sin 36^{\circ}$ is a root of which of the following equation

(A)
$$10x^4 - 10x^2 - 5 = 0$$
 (B) $16x^4 + 20x^2 - 5 = 0$
(C) $16x^4 - 20x^2 + 5 = 0$ (D) $16x^4 - 10x^2 + 5 = 0$
Official Ans. by NTA (C)

Sol.
$$\cos 72^\circ = \frac{\sqrt{5} - 1}{4}$$

 $\Rightarrow 1 - 2 \sin^2 36^\circ = \frac{\sqrt{5} - 1}{4}$
 $\Rightarrow 4 - 8\alpha^2 = \sqrt{5} - 1$
 $\Rightarrow 5 - 8\alpha^2 = \sqrt{5}$
 $\Rightarrow (5 - 8\alpha^2)^2 = 5$
 $\Rightarrow 25 + 64\alpha^4 - 80\alpha^2 = 5$
 $\Rightarrow 64\alpha^4 - 80\alpha^2 + 20 = 0$
 $\Rightarrow 16\alpha^4 - 20\alpha^2 + 5 = 0$

20. Which of the following statement is a tautology?
(A) ((~q) ∧ p) ∧ q
(B) ((~q) ∧ p) ∧ (p ∧ (~ p))
(C) ((~q) ∧ p) ∨ (p ∨ (~ p))
(D) (p ∧ q) ∧ (~ (p ∧ q))

Sol. (A)
$$(\sim q \land p) \land q = (\sim q \land q) \land p = f$$

(B) $(\sim q \land p) \land (p \land \sim p) = \sim q \land (p \land \sim p) = f$
(C) $(\sim q \land p) \lor (p \lor \sim p) = (\sim q \land p) \lor (t) = t$
(D) $(p \land q) \land (\sim (p \land q)) = f$

18.

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SECTION-B

1. Let $S = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$. Define

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f: S
$$\rightarrow$$
 S as f(n) =
 $\begin{cases} 2n, & \text{if } n = 1, 2, 3, 4, 5 \\ 2n - 11 & \text{if } n = 6, 7, 8, 9, 10 \end{cases}$

Let $g : S \rightarrow S$ be a function such that $fog(n) = \begin{cases} n+1 & \text{, if } n \text{ is odd} \\ n-1 & \text{, if } n \text{ is even} \end{cases}$, then

g(10) ((g(1) + g(2) + g(3) + g(4) + g(5))) is equal to:

Official Ans. by NTA (190)

Sol.
$$f^{-1}(n) = \begin{cases} \frac{n}{2} & ; n = 2, 4, 6, 8, 10 \\ \frac{n+11}{2} & ; n = 1, 3, 5, 7, 9 \end{cases}$$

 $f(g(n)) = \begin{cases} n+1 & ; n \in odd \\ n-1 & ; n \in even \end{cases}$
 $\Rightarrow g(n) = \begin{cases} f^{-1}(n+1) & ; n \in odd \\ f^{-1}(n-1) & ; n \in even \end{cases}$
 $\therefore g(n) = \begin{cases} \frac{n+1}{2} & ; n \in odd \\ \frac{n+10}{2} & ; n \in even \end{cases}$
 $g(10) \cdot [g(1) + g(2) + g(3) + g(4) + g) = 10 \cdot [1 + 6 + 2 + 7 + 3] = 190$

2. Let α , β be the roots of the equation $x^2 - 4\lambda x + 5 = 0$ and α , γ be the roots of the equation $x^2 - (3\sqrt{2} + 2\sqrt{3})x + 7 + 3\lambda\sqrt{3} = 0$. If $\beta + \gamma = 3\sqrt{2}$, then $(\alpha + 2\beta + \gamma)^2$ is equal to :

(5)

Official Ans. by NTA (98)

Sol.
$$x^2 - 4\lambda x + 5 = 0 \Big\langle_{\beta}^{\alpha} \\ x^2 - (3\sqrt{2} + 2\sqrt{3})x + (7 + 3\lambda\sqrt{3}) = 0 \Big\langle_{\gamma}^{\alpha} \\ \alpha + \beta = 4\lambda \\ \alpha + \gamma = 3\sqrt{2} + 2\sqrt{3}$$

- $\beta + \lambda = 3\sqrt{2} \qquad \alpha\gamma = 7 + 3\lambda\sqrt{3}$ $\therefore \qquad \alpha = 2\lambda + \sqrt{3} \qquad \alpha\beta = 5$ $\beta = 2\lambda - \sqrt{3} \qquad 4\lambda^2 = 8 \implies \lambda = \sqrt{2}$ $\therefore \qquad (\alpha + 2\beta + \lambda)^2 = (4\alpha + 3\sqrt{2})^2 = (7\sqrt{2})^2 = 98$
- Let A be a matrix of order 2 × 2, whose entries are from the set {0, 1, 2, 3, 4, 5}. If the sum of all the entries of A is a prime number p, 2

Official Ans. by NTA (180)

Sol. Let
$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$
; a, b, c, $d \in \{0, 1, 2, 3, 4, 5\}$
 $a + b + c + d = p, p \in \{3, 5, 7\}$
Case-(i)
 $a + b + c + d = 3$; a, b, c, $d \in \{0, 1, 2, 3\}$
No. of ways = ${}^{3+4-1}C_{4-1} = {}^{6}C_{3} = 56$ (1)
Case-(ii)
 $a + b + c + d = 5$; a, b, c, $d \in \{0, 1, 2, 3, 4, 5\}$
No. of ways = ${}^{5+4-1}C_{4-1} = {}^{8}C_{3} = 56$ (2)
Case-(iii)
 $a + b + c + d = 7$
No. of ways = total ways when a, b, c, $d \in \{0, 1, 2, 3, 4, 5, 6, 7\}$ - total ways when a, b, c, $d \in \{0, 1, 2, 3, 4, 5, 6, 7\}$ - total ways when a, b, c, $d \notin \{6, 7\}$
No of ways = ${}^{7+4-1}C_{4-1} = \left(\frac{|4|}{|3|} + \frac{|4|}{|2|}\right)$
 $= {}^{10}C_{3} - 16 = 104$ (3)
Hence total no. of ways = 180
4. If the sum of the coefficients of all the positive powers of x, in the binomial expansion of $\left(x^{n} + \frac{2}{x^{5}}\right)^{7}$ is 939, then the sum of all the possible integral values of n is :
Official Ans. by NTA (57)
Sol. coefficients and there cumulative sum are :



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region

-1 < x < 1

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$$\frac{\operatorname{Coefficient}}{x^{10} \to 1^{10}} \frac{\operatorname{Commutative sum}}{1}$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1}$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1}$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1}$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1}$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1}$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1} + 14 + 84 + 280$$

$$x^{20} \to 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1} + 14 + 84 + 280$$

$$x^{20} \to 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1} + 14 + 84 + 280$$

$$x^{20} \to 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1} + 14 + 84 + 280 + 560 = 939$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1} + 4 + 84 + 280 + 560 = 939$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 2^{10} \cdot 1^{10} \frac{1}{1} + 4 + 84 + 280 + 560 = 939$$

$$x^{10} \to 2^{10} \cdot 2^{10} \cdot 2^{10} + 11 + 12 = 57$$
5. Let [1] denote the greatest integer ≤ 1 and [1]
denote the fractional part of 1. Then integral value
of α for which the fiel hand limit of the function
f(x) = [1 + x] + \frac{a^{2(1)}(1^{10} + [x]^{-1}}{2[x]^{1} + [x]}
$$x + y \ge 0$$
Sol. $f(x) = [1 + x] + \frac{a^{2(1)}(1^{10} + [x]^{-1}}{2[x]^{1} + [x]}$

$$x + y \ge 0$$
Sol. $f(x) = [1 + x] + \frac{a^{2(1)}(1^{10} + [x]^{-1}}{2[x]^{1} + [x]}$

$$x + y \ge 0$$

$$x = 3^{10} = -\frac{a^{2}}{3}$$

$$x = 3; \alpha \in 1$$
6. If $y(x) = (x^{1^{1}})$

$$x = x^{1} = \frac{10}{3}$$

$$\Rightarrow \alpha = 3; \alpha \in 1$$
6. If $y(x) = (x^{1^{1}})$

$$x = x^{1} + 2x \cdot \ln x$$

$$y'(x) = y(x) = (x^{1^{1}})$$

$$hy(x) = x^{1} \cdot \ln x$$

$$\frac{1}{y(x)} - y'(x) = \frac{x^{2}}{x} + 2x \cdot \ln x$$

$$y'(x) = y(x) = (x^{1^{1}})$$

$$x = \frac{1}{2} \frac{2}{2} \frac{1}{2} \frac{1}{1} - \frac{1}{2} \frac{3}{2} \frac{2}{2} \frac{1}{2} \frac{1}{1} - \frac{1}{2} \frac{3}{2} \frac{2}{2} \frac{1}{2} \frac{1}{2} \frac{1}{1} - \frac{1}{2} \frac{1}{$$

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Sol.
$$(1 - x^2) \frac{dy}{dx} = xy + (x^3 + 2) \sqrt{1 - x^2}$$

$$\Rightarrow \frac{dy}{dx} + \left(\frac{-x}{1 - x^2}\right) y = \frac{x^3 + 2}{\sqrt{1 - x^2}}$$

$$IF = e^{\int \frac{-x}{1 - x^2} dx} = \sqrt{1 - x^2}$$

$$y(x) \cdot \sqrt{1 - x^2} = \frac{x^4}{4} + 2x + c$$

$$y(0) = 0 \Rightarrow c = 0$$

$$\sqrt{1 - x^2} y(x) = \frac{x^4}{4} + 2x$$

$$required value = \int_{-1/2}^{1/2} \left(\frac{x^4}{4} + 2x\right) dx - \frac{1}{4} \cdot 2\int_{0}^{1/2} x^4 dx$$

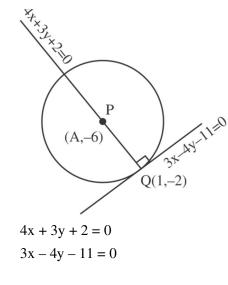
$$= \frac{1}{10} \left(x^5\right)_{0}^{1/2} = \frac{1}{320}$$

$$k^{-1} = 320$$

9. Let a circle C of radius 5 lie below the x-axis. The line $L_1=4x+3y-2$ passes through the centre P of the circle C and intersects the line $L_2:3x-4y-11=0$ at Q. The line L_2 touches C at the point Q. Then the distance of P from the line 5x-12y+51=0 is

Official Ans. by NTA (11)

Sol.



$$4 \frac{5}{\theta}$$

$$\frac{x}{-25} = \frac{y}{50} = \frac{1}{-25}$$

$$\frac{x-1}{\cos\theta} = \frac{y+2}{\sin\theta} = \pm 5$$

$$y = -2 + 5\left(-\frac{4}{5}\right) = -6$$

$$x = 1 + 5\left(\frac{3}{5}\right) = 4$$

Req. distance

$$\frac{5(4) - 12(-6) + 51}{13}$$
$$= \left| \frac{20 + 72 + 51}{13} \right|$$
$$= \frac{143}{13} = 11$$

10. Let $S = \{E, E_2, ..., E_8\}$ be a sample space of random

experiment such that $P(E_n) = \frac{n}{36}$ for every n = 1, 2...8. Then the number of elements in the set $\left\{A \subset S: P(A) \ge \frac{4}{5}\right\}$ is _____

Official Ans. by NTA (19)

Sol.
$$P(A') < \frac{1}{5} = \frac{36}{180}$$

5 times the sum of missing number should be less than 36.

If 1 digit is missing = 7 If 2 digit is missing = 9 If 3 digit is missing = 2 If 0 digit is missing = 1 **Alternate** A is subset of S hence A can have elements: type 1 : { }



Final JEE-Main Exam June, 2022/27-06-2022/Evening Session

EE READY?

Note : Type 1 to Type 4 elements can not be in set A as maximum probability of type 4 elements.

{E₅, E₆, E₇, E₈} is
$$\frac{5}{36} + \frac{6}{36} + \frac{7}{36} + \frac{8}{36} = \frac{13}{18} < \frac{4}{5}$$

Now for Type 5 acceptable elements let's call probability as P₅

$$\begin{split} P_{5} &= \frac{n_{1} + n_{2} + n_{3} + n_{4} + n_{5}}{36} \leq \frac{4}{5} \\ &\Rightarrow n_{1} + n_{2} + n_{3} + n_{4} + n_{5} \geq 28.8 \\ \text{Hence, 2 possible ways } \{E_{5}, E_{6}, E_{7}, E_{8}, E_{3} \text{ or } E_{4}\} \\ P_{6} &= n_{1} + n_{2} + n_{3} + n_{4} + n_{5} + n_{6} \geq 28.8 \\ &\Rightarrow 9 \text{ possible ways} \\ P_{7} &\Rightarrow n_{1} + n_{2} + \dots + n_{7} \geq 288 \\ &\Rightarrow 7 \text{ possible ways} \\ P_{8} &\Rightarrow n_{1} + n_{2} + \dots + n_{8} \geq 28.8 \\ &\Rightarrow 1 \text{ possible way} \\ \text{Total} &= 19 \end{split}$$