

Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

## **FINAL JEE-MAIN EXAMINATION - JUNE, 2022**

(Held On Saturday 25<sup>th</sup>June, 2022)

TIME : 3:00 PM to 6:00 PM

# **PHYSICS**

#### **SECTION-A**

1. Given below are two statements. One is labelled as Assertion A and the other is labelled as Reason R. Assertion A :Two identical balls A and B thrown with same velocity 'u' at two different angles with horizontal attained the same range R. If A and B reached the maximum height h<sub>1</sub> and  $h_2$ respectively, then  $R = 4\sqrt{h_1h_2}$ 

Reason R: Product of said heights.

$$h_1h_2 = \left(\frac{u^2\sin^2\theta}{2g}\right) \cdot \left(\frac{u^2\cos^2\theta}{2g}\right)$$

Choose the CORRECT answer:

- (A) Both A and R are true and R is the correct explanation of A.
- (B) Both A and R are true but R is NOT the correct explanation of A.
- (C) A is true but R is false
- (D) A is false but R is true
- Official Ans. by NTA (A)
- **Sol.** For same range  $\theta_1 + \theta_2 = 90^\circ$



$$h_1h_2 = \frac{u^2\sin^2\theta_1}{2g} \times \frac{u^2\sin^2\theta_2}{2g}$$

TEST PAPER WITH SOLUTION

$$\theta_2 = 90 - \theta$$

$$h_1 h_2 = \frac{u^2 \sin^2 \theta_1}{2g} \cdot \frac{u^2 \cos^2 \theta_1}{2g}$$

$$= \left\lfloor \frac{u \sin \theta_1 \cos \theta_1}{2g} \right\rfloor$$

$$= \left[\frac{u^2 \sin \theta_1 \cos \theta_1}{2g} \times \frac{2}{2}\right]^2 = \frac{R^2}{16}$$
$$R = 4\sqrt{h.h_2}$$

So R is correct explanation of A

Two buses P and Q start from a point at the same time and move in a straight line and their positions  $X_{\rm P}(t) = \alpha t + \beta t^2$  and represented by are  $X_Q(t) = ft - t^2$ . At what time, both the buses have

same velocity ?

2.

(A) 
$$\frac{\alpha - f}{1 + \beta}$$
 (B)  $\frac{\alpha + f}{2(\beta - 1)}$   
(C)  $\frac{\alpha + f}{2(1 + \beta)}$  (D)  $\frac{f - \alpha}{2(1 + \beta)}$ 

Official Ans. by NTA (D)

Sol. 
$$X_{p}(t) = \alpha t + \beta t^{2}$$
  $X_{Q} = ft - t^{2}$   
 $V_{P}(t) = \alpha + 2\beta t$   $V_{Q} = f - 2t$   
 $V_{P} = V_{Q}$   
 $\alpha + 2\beta t = f - 2t$   
 $t = \frac{f - \alpha}{2\beta + 2}$ 



3. A disc with a flat small bottom beaker placed on it at a distance R from its center is revolving about an axis passing through the center and perpendicular to its plane with an angular velocity ω. The coefficient of static friction between the bottom of the beaker and the surface of the disc is μ. The beaker will revolve with the disc if :

(A) 
$$R \le \frac{\mu g}{2\omega^2}$$
 (B)  $R \le \frac{\mu g}{\omega^2}$   
(C)  $R \ge \frac{\mu g}{2\omega^2}$  (D)  $R \ge \frac{\mu g}{\omega^2}$ 

Official Ans. by NTA (B)

Sol. For beaker to move with disc



E YOL

 $f_s = m\omega^2 R$ 

We know that  $f_s \leq f_{s \max}$ 

 $m\omega^2 R \leq \mu mg$ 

$$R \le \frac{\mu g}{\omega^2}$$

4. A solid metallic cube having total surface area 24 m<sup>2</sup> is uniformly heated. If its temperature is increased by 10°C, calculate the increase in volume of the cube (Given : $\alpha = 5.0 \times 10^{-4} \circ C^{-1}$ )

(A) 
$$2.4 \times 10^{6}$$
 cm<sup>3</sup>  
(B)  $1.2 \times 10^{5}$  cm<sup>3</sup>  
(C)  $6.0 \times 10^{4}$  cm<sup>3</sup>  
(D)  $4.8 \times 10^{5}$  cm<sup>3</sup>  
Official Ans. by NTA (B)

Sol. Increase in volume  $\Delta V = \gamma V_0 \Delta T$   $\gamma = 3\alpha$ So  $\Delta V = (3\alpha) V_0 \Delta T$ Total surface area =  $6a^2$ , where a is side length  $24 = 6a^2$  a= 2m Volume  $V_0 = (2)^3 = 8m^3$  $\Delta V = (3 \times 5 \times 10^{-4})(8) \times 10$ 

$$= 1.2 \times 10^{5} \text{ cm}$$

5. A copper block of mass 5.0 kg is heated to a temperature of 500°C and is placed on a large ice block. What is the maximum amount of ice that can melt? [Specific heat of copper:  $0.39 \text{ Jg}^{-1} \circ \text{C}^{-1}$ 

and latent heat of fusion of water : 335 J  $g^{-1}$ ]

(A) 1.5 kg	(B) 5.8 kg
(C) 2.9 kg	(D) 3.8 kg

Official Ans. by NTA (C)

Sol. Heat given by block to get 0°C temperature  $\Delta Q_1 = 5 \times (0.39 \times 10^3) \times (500 - 0)$ 

> =  $975 \times 10^3$ J Heat absorbed by ice to melt m mass

$$\Delta \mathbf{Q}_2 = \mathbf{m} \times \left(335 \times 10^3\right) \mathbf{J}$$

$$\Delta Q_1 = \Delta Q_2$$
  
m×(335×10<sup>3</sup>) = 975×10<sup>3</sup>

$$m = \frac{975}{335} = 2.910 \, \text{kg}$$

6. The ratio of specific heats  $\left(\frac{C_P}{C_V}\right)$  in terms of

degree of freedom (f) is given by:

(A) 
$$\left(1 + \frac{f}{3}\right)$$
  
(B)  $\left(1 + \frac{2}{f}\right)$   
(C)  $\left(1 + \frac{f}{2}\right)$   
(D)  $\left(1 + \frac{1}{f}\right)$ 

Official Ans. by NTA (B)

JEE NEET Class 9 - 12 Scoogle Pile Download App Now 🖸

E-Main Exam June, 2022/25-06-2022/Evening Session

Sol. Molar heat capacity at constant volume  $C_v = \frac{fR}{2}$ 

where f is degree of freedom. Molar heat capacity at constant pressure can be written as  $C_p = R + C_v = R + \frac{fR}{2} = \left(1 + \frac{f}{2}\right)R$ S

So 
$$\frac{C_P}{C_v} = 1 + \frac{2}{f}$$

7. For a particle in uniform circular motion, the acceleration  $\vec{a}$  at any point P(R, $\theta$ ) on the circular path of radius R is (when  $\theta$  is measured from the positive x -axis and v is uniform speed) :

$$(A) - \frac{v^2}{R}\sin\theta \hat{i} + \frac{v^2}{R}\cos\theta \hat{j}$$

$$(B) - \frac{v^2}{R}\cos\theta \hat{i} + \frac{v^2}{R}\sin\theta \hat{j}$$

$$(C) - \frac{v^2}{R}\cos\theta \hat{i} - \frac{v^2}{R}\sin\theta \hat{j}$$

$$(D) - \frac{v^2}{R}\hat{i} + \frac{v^2}{R}\hat{j}$$

Official Ans. by NTA (C)

Sol. 
$$a = |\vec{a}| = \frac{V^2}{R}$$
  
 $\vec{a} = -a \cos \theta \hat{i} - a \sin \theta \hat{j}$   
 $= -\frac{V^2}{R} \cos \theta \hat{i} - \frac{V^2}{R} \sin \theta \hat{j}$   
8. Two metallic plates form a parallel plate capacitor.  
The distance between the plates is 'd'. A metal  
sheet of thickness  $\frac{d}{2}$  and of area equal to area of

each plate is introduced between the plates. What will be the ratio of the new capacitance to the original capacitance of the capacitor ?

(A) 2:1	(B) 1:2
(C) 1:4	(D) 4:1
Official Ans. by I	NTA (A)

Sol. 
$$C_1 = \frac{\epsilon_0 A}{d}$$
  
 $C_2 = \frac{\epsilon_0 A}{\frac{d}{2} + \frac{d/2}{\infty}} = \frac{2}{2}$   
 $\frac{C_2}{C_1} = \frac{2}{1}$ 

9. Two cells of same emf but different internal resistances r<sub>1</sub> and r<sub>2</sub> are connected in series with a resistance R. The value of resistance R, for which the potential difference across second cell is zero,

(D) r<sub>2</sub>

 $z \in_0 A$ 

is  
(A) 
$$r_2 - r_1$$
 (B)  $r_1 - r_2$ 

Official Ans. by NTA (A)

**Sol.** 
$$I = \frac{2E}{R + r_1 + r_2}$$
....(i)

(C) r<sub>1</sub>

But  $V_A - V_B = E - Ir_2 = 0$ 

$$\Rightarrow$$
 I =  $\frac{E}{r_2}$  ....(ii)

Comparing values of I from (i) and (ii)

$$\frac{\mathrm{E}}{\mathrm{r}_{2}} = \frac{2\mathrm{E}}{\mathrm{R} + \mathrm{r}_{1} + \mathrm{r}_{2}}$$
$$\Longrightarrow \mathrm{R} = \mathrm{r}_{2} - \mathrm{r}_{1}$$

Give yourself an extra edge

plate capacitor.



**10.** Given below are two statements:

Statement -I: Susceptibilities of paramagnetic and ferromagnetic substances increase with decrease in temperature.

**Statement – II:** Diamagnetism is a result of orbital motions of electrons developing magnetic moments opposite to the applied magnetic field.

Choose the **CORRECT** answer from the options given below : -

(A) Both statement – I and statement -II are true.

(B) Both statement – I and Statement – II are false.

(C) Statement – I is true but statement – II is false.

(D) Statement-I is false but Statement-II is true.

#### Official Ans. by NTA (A)

Sol. According to curie's law, magnetic susceptibility is inversely proportional to temperature for a fixed value of external magnetic field i.e.  $\chi = \frac{C}{T}$ .

The same is applicable for ferromagnet & the relation is given as  $\chi = \frac{C}{T - T_C}$  (T<sub>c</sub> is curie

temperature)

Diamagnetism is due to non-cooperative behaviour of orbiting electrons when exposed to external magnetic field.

Hence option (A).

11. A long solenoid carrying a current produces a magnetic field B along its axis. If the current is doubled and the number of turns per cm is halved, the new value of magnetic field will be equal to

(A) B	(B) 2 B
	В

(C) 4 B	(D) $\frac{1}{2}$
---------	-------------------

### Official Ans. by NTA (A)

**Sol.**  $B_1 = \mu_0 nI$ 

$$B_2 = \mu_0 \left(\frac{n}{2}\right) (2I)$$
$$\Rightarrow B_1 = B_2$$

12. A sinusoidal voltage V(t) = 210 sin 3000t volt is applied to a series LCR circuit in which L = 10 mH, C = 25  $\mu$ F and R = 100 $\Omega$ . The phase difference ( $\Phi$ ) between the applied voltage and resultant current will be :

(A)  $\tan^{-1}(0.17)$ (B)  $\tan^{-1}(9.46)$ (C)  $\tan^{-1}(0.30)$ (D)  $\tan^{-1}(13.33)$ 

Official Ans. by NTA (A)

**Sol.** 
$$X_L = 10^{-2} \times 3000 = 30\Omega$$

$$X_{\rm C} = \frac{1}{3000 \times 25 \times 10^{-6}} = \frac{40}{3} \Omega$$
$$X = X_{\rm L} - X_{\rm C}$$
$$= 30 - \frac{40}{3} = \frac{50}{3}$$
$$\tan \delta = \frac{X}{\rm R} = \frac{50}{3 \times 100} = \frac{1}{6}$$
$$\delta = \tan^{-1} \left(\frac{1}{6}\right) = \tan^{-1} \left(0.17\right)$$

13. The electromagnetic waves travel in a medium at a speed of  $2.0 \times 10^8$  m/s. The relative permeability of the medium is 1.0. The relative permittivity of the medium will be:

(A) 2.25	(B) 4.25
(C) 6.25	(D) 8.25

Official Ans. by NTA (A)

Sol. 
$$V = 2 \times 10^8 \text{ m/s}$$
  
 $C = 3 \times 10^8 \text{ m/s}$   
 $\frac{C}{V} = \sqrt{\mu_r \epsilon_r}$   
 $\frac{9}{4} = 1 \times \epsilon_r$   
 $\epsilon_r = \frac{9}{4} = 2.25$ 

eedge Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

14. The interference pattern is obtained with two coherent light sources of intensity ratio 4 :1. And the ratio  $\frac{I_{max} + I_{min}}{I_{max} - I_{min}}$  is  $\frac{5}{x}$ . Then, the value of x

will be equal to :

- (A) 3 (B) 4
- (C) 2 (D) 1

Official Ans. by NTA (B)

**Sol.** 
$$\frac{I_1}{I_2} = 4$$

$$\frac{I_{\max}}{I_{\min}} = \left[\frac{\sqrt{I_1} + \sqrt{I_2}}{\sqrt{I_1} - \sqrt{I_2}}\right]^2$$
$$\frac{I_{\max}}{I_{\min}} = \left[\frac{2\sqrt{I_2} + \sqrt{I_2}}{2\sqrt{I_2} - \sqrt{I_2}}\right]^2$$
$$\frac{I_{\max}}{I_{\min}} = 9$$
$$\frac{I_{\max} + I_{\min}}{I_{\max} - I_{\min}} = \frac{10}{8}$$
$$\frac{5}{x} = \frac{10}{8}$$
$$x = 4$$

- A light whose electric field vectors are completely 15. removed by using a good Polaroid, allowed to incident on the surface of the prism at Brewster's angle. Choose the most suitable option for the phenomenon related to the prism.
  - (A) Reflected and refracted rays will be perpendicular to each other
  - (B) Wave will propagate along the surface of prism
  - (C) No refraction, and there will be total reflection of light.
  - (D) No reflection and there will be total transmission of light.

Official Ans. by NTA (D)



But as the incident light electric field vectors are completely removed so there will be no reflection and there will be total transmission of light, explained by an experiment in NCERT.

JEE | NEET | Class 9 - 12 🗾

Download App Now

[Reference NCERT Part-2 Pg-380, (A special case of total transmission)]

Note : Since direction of polarization is not mentioned hence most suitable option (D) corresponding to case in which electric field is absent perpendicular to plane consisting incident and normal.

16. A proton, a neutron, an electron and an  $\alpha$ -particle have same energy. If  $\lambda_p, \lambda_n, \lambda_e$  and  $\lambda_\alpha$  are the de Broglie's wavelengths of proton, neutron, electron and  $\alpha$  particle respectively, then choose the correct relation from the following :

(A) 
$$\lambda_p = \lambda_n > \lambda_e > \lambda_\alpha$$
  
(B)  $\lambda_\alpha < \lambda_n < \lambda_p < \lambda_e$   
(C)  $\lambda_e < \lambda_p = \lambda_n > \lambda_\alpha$   
(D)  $\lambda_e = \lambda_p = \lambda_n = \lambda_\alpha$ 

Official Ans. by NTA (B)

Sol. 
$$\lambda = \frac{h}{\sqrt{2Em}}$$
  
 $\lambda \propto \frac{1}{\sqrt{m}}$   
 $\therefore \quad \lambda_e > \lambda_p > \lambda_n > \lambda_\alpha$ 



JEE | NEET | Class 9 - 12 Stroot Play www.eedge.in Download App Now 🖸 Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

17. Which of the following figure represents the  $(\mathbf{p})$ va

ariation of 
$$\ln\left(\frac{R}{R_0}\right)$$
 with  $\ln A(\text{If } R = \text{radius of a})$ 

nucleus and A = its mass number)



Official Ans. by NTA (B)

**Sol.** 
$$R = R_0 A^{\frac{1}{3}}$$



18. Identify the logic operation performed by the given circuit :



- (A) AND gate (C) NOR gate
- (B) OR gate (D) NAND gate

Official Ans. by NTA (A)

**Sol.** = 
$$\left[\overline{\left[\overline{A+A}\right] + \left[\overline{B+B}\right]}\right]$$

$$Y = \overline{\overline{A} + \overline{B}} (D' \text{ MORGAN LAW})$$
$$Y = \Delta B$$

19. Match List I with List II

List -I		List – II	
A	Facsimile	I.	Static Document Image
В.	Guided media Channel	II.	Local Broadcast Radio
C.	Frequency Modulation	III.	Rectangular wave
D.	Digital Signal	IV.	Optical Fiber

Choose the correct answer from the following options :

(A) A –IV, B-III, C-II, D-I (B)A-I, B-IV, C-II, D-III (C) A –IV, B-II, C-III, D-I (D) A-I, B-II, C-III, D-IV Official Ans. by NTA (B)

- Question based on the theory given in NCERT. Sol.
- 20. If n represents the actual number of deflections in a converted galvanometer of resistance G and shunt resistance S. Then the total current I when its figure of merit is K will be :

(A) 
$$\frac{KS}{(S+G)}$$
 (B)  $\frac{(G+S)}{nKS}$   
(C)  $\frac{nKS}{(G+S)}$  (D)  $\frac{nK(G+S)}{S}$ 

Official Ans. by NTA (D)

Sol.

www.eedge.in

JEE | NEET | Class 9 - 12 Download App Now

DEE-Main Exam June, 2022/25-06-2022/Evening Session

$$I = \frac{I_g}{I - I_g} (G + S)$$

$$I = \frac{nK}{S} (G + S)$$

#### **SECTION-B**

1. For  $z = a^2 x^3 y^{\frac{1}{2}}$ , where 'a' is a constant. If percentage error in measurement of 'x' and 'y' are 4% and 12%, respectively, then the percentage error for 'z' will be %.

Official Ans. by NTA (18)

**Sol.**  $z = a^2 x^3 y^{1/2}$ 

$$\frac{\Delta z}{z} = \frac{2\Delta a}{a} + \frac{3\Delta x}{x} + \frac{1}{2}\frac{\Delta y}{y}$$

a is constant

$$\frac{\Delta z}{z} \times 100 = 3(4\%) + \frac{1}{2}(12\%) = 18\%$$

2. A curved in a level road has a radius 75m. The maximum speed of a car turning this curved road can be 30 m/s without skidding. If radius of curved road is changed to 48 m and the coefficient of friction between the tyres and the road remains same, then maximum allowed speed would be\_\_\_\_\_\_m/s.

#### Official Ans. by NTA (24)

Sol.  $f_{s max} = \frac{mv^2}{R}$  $\mu mg = \frac{mv^2}{R}$ 

$$v = \sqrt{\mu Rg}$$
$$\frac{v_2}{v_1} = \sqrt{\frac{R_2}{R_1}}$$
$$\frac{v_2}{30} = \sqrt{\frac{48}{75}}$$
$$v_2 = 24 \text{ m/s}$$

3. A block of mass 200 g is kept stationary on a smooth inclined plane by applying a minimum horizontal force  $F = \sqrt{x}N$  as shown in figure. The value of x = \_\_\_\_\_.



Official Ans. by NTA (12)



4. Moment of Inertia (M.I.) of four bodies having same mass 'M' and radius '2R' are as follows:
I<sub>1</sub>= M.I. of solid sphere about its diameter
I<sub>2</sub> = M.I. of solid cylinder about its axis
I<sub>3</sub> = M.I. of solid circular disc about its diameter
I<sub>4</sub> = M.I. of thin circular ring about its diameter
If 2(I<sub>2</sub> + I<sub>3</sub>) + I<sub>4</sub> = x. I<sub>1</sub> then the value of x will be

Official Ans. by NTA (5)



Sol. 
$$I_1 = \frac{2}{5}M(2R)^2 = \frac{8}{5}MR^2$$
  
 $I_1 = \frac{1}{2}M(2R)^2 = 2MR^2$   
 $I_3 = \frac{M(2R)^2}{4} = MR^2$   
 $I_4 = \frac{M(2R)^2}{2} = 2MR^2$   
 $2(I_2 + I_3) + I_4 = x I_1$   
 $8MR^2 = x\frac{8}{5}MR^2$   
 $x = 5$ 

5. Two satellites  $S_1$  and  $S_2$  are revolving in circular orbits around a planet with radius  $R_1 = 3200$  km and  $R_2 = 800$  km respectively. The ratio of speed of satellite  $S_1$  to the speed of satellite  $S_2$  in their respective orbits would be  $\frac{1}{x}$  where x =

Official Ans. by NTA (2)

- **Sol.**  $V = \frac{GM}{r} \Rightarrow \frac{V_1}{V_2} = \sqrt{\frac{800}{3200}} = \frac{1}{2}$
- 6. When a gas filled in a closed vessel is heated by raising the temperature by 1°C, its pressure increase by 0.4%. The initial temperature of the gas is\_\_\_\_\_K.

Official Ans. by NTA (250)

**Sol.** pV = nRT $\Delta P.V = nR\Delta T$  $\frac{\Delta P}{P} = \frac{\Delta T}{T} = \frac{0.4}{100}$ 

$$\Rightarrow T = \frac{100 \times 1}{0.4} = 250 \text{K}$$

7. 27 identical drops are charged at 22V each. They combine to form a bigger drop. The potential of the bigger drop will be \_\_\_\_\_ V.

Official Ans. by NTA (198)

Sol. 
$$q \rightarrow nq$$

$$n\frac{4}{3}\pi r^{3} = \frac{4}{3}\pi (r')^{3}$$
$$\implies r' = n^{\frac{1}{3}}r$$

$$V = \frac{kq}{r} \propto \frac{n}{n^{1/3}} \propto n^{2/3} \propto 27^{2/3} \Longrightarrow v' = 9V = 9 \times 22 = 198$$

8. The length of a given cylindrical wire is increased to double of its original length. The percentage increase in the resistance of the wire will be %.

Official Ans. by NTA (300)

Sol. V' = V  

$$\ell'A = \ell A$$
  
 $2\ell A' = \ell A$   
 $A' = \frac{A}{2}$   
 $R = \rho \frac{\ell}{A} \dots (i)$   
 $\ell' = 2\ell$   
 $A' = \frac{A}{2}$   
 $R' = \frac{\rho \ell'}{A'} = \frac{\rho 2\ell}{\frac{A}{2}}$   
 $R' = \frac{4\rho \ell}{A}$   
 $R' = 4R$  from equation (i)  
% increase in resistance  
 $= \frac{R'-R}{R} \times 100 = \frac{4R-R}{R} \times 100$   
 $= 300 \%$ 

### Give yourself an extra edge

8 www.ayjr.in

# AYJR Powered By www.eedge.in ARE YOU JEE READY? Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

9. In a series LCR circuit, the inductance, capacitance and resistance are L = 100mH,  $C = 100\mu$ F and  $R = 10\Omega$  respectively. They are connected to an AC source of voltage 220V and frequency of 50 Hz. The approximate value of current in the circuit will be\_\_\_\_\_A.



Official Ans. by NTA (22)

**Sol.** 
$$X_L = \omega L = 2\pi \times 50 \times 10^{-1} = 10\pi$$

$$X_{\rm X} = \frac{1}{\omega C} = \frac{1}{2\pi \times 50} \times 10^4 = \frac{100}{\pi}$$
  
R = 10 $\Omega$ 

$$Z = \sqrt{\left(10\pi - \frac{100}{\pi}\right)^2 + 10^2} \approx 10\Omega$$
  
Sol. Volt  
i =  $\frac{E}{2} \approx \frac{220}{10} \approx 22$ Amp

**10.** In an experiment of CE configuration of n-p-n transistor, the transfer characteristics are observed as given in figure.



If the input resistance is  $200\Omega$  and output resistance is  $60 \Omega$  the voltage gain in this experiment will be \_\_\_\_\_

Official Ans. by NTA (15)

Sol. Voltage Gain =  $\frac{I_C}{I_B} \times \frac{R_0}{R_I} = \frac{10 \times 10^{-3}}{200 \times 10^{-6}} \times \frac{60}{200} = 15$ 



# FINAL JEE-MAIN EXAMINATION - JUNE, 2022

(Held On Saturday 25<sup>th</sup> June, 2022)

TIME: 3:00 PM to 6:00 PM

#### **CHEMISTRY SECTION-A** Official Ans. by NTA (D) 1. The minimum energy that must be possessed by photons in order to produce the photoelectric effect **Sol.** $\Delta T = i k_f \times m$ with platinum metal is: $0.2 = i \times 1.86 \times \frac{0.7}{93} \times \frac{1000}{42}$ [Given: The threshold frequency of platinum is 1.3 $\times 10^{15} \text{ s}^{-1}$ and h = 6.6 $\times 10^{-34} \text{ J s.}$ ] $i = \frac{0.2 \times 93 \times 6}{1.86 \times 100}$ (A) $3.21 \times 10^{-14}$ J (B) $6.24 \times 10^{-16}$ J i = 0.60(D) $9.76 \times 10^{-20}$ J (C) $8.58 \times 10^{-19}$ J $2A \rightleftharpoons A_2$ Official Ans. by NTA (C) $1 - \alpha$ **Sol.** W = hv $i = 1 - \alpha + \frac{\alpha}{2}$ $= 6.6 \times 10^{-34} \times 1.3 \times 10^{15}$ $= 8.58 \times 10^{-19} \text{ J}$ $i=1-\frac{\alpha}{2}$ At 25°C and 1 atm pressure, the enthalpy of 2. combustion of benzene (1) and acetylene (g) are $1 - \frac{\alpha}{2} = 0.60$ -3268 kJ mol<sup>-1</sup> and -1300 kJ mol<sup>-1</sup>, respectively. The change in enthalpy for the reaction $1 - 0.60 = \frac{\alpha}{2}$ $3 C_2 H_2(g) \rightarrow C_6 H_6(l)$ , is $\alpha = 0.80$ $(A) + 324 \text{ kJ mol}^{-1}$ (B) $+632 \text{ kJ mol}^{-1}$ $(D) - 732 \text{ kJ mol}^{-1}$ 4. $(C) - 632 \text{ kJ mol}^{-1}$ Official Ans. by NTA (C) 298 K is

**Sol.**  $\Delta H = \sum \Delta H_{Combustion}$  (Reactant) -  $\sum \Delta H_{Combustion}$ (Product)  $= 3 \times (-1300) - [-3268]$ 

 $= -632 \text{ kJ mol}^{-1}$ 

Solute A associates in water. When 0.7 g of solute 3. A is dissolved in 42.0 g of water, it depresses the freezing point by  $0.2^{\circ}$ C. The percentage association of solute A in water, is [Given : Molar mass of A = 93 g mol<sup>-1</sup>. Molal depression constant of water is 1.86 K kg mol<sup>-1</sup>] (A) 50 % (B) 60 % (C) 70 % (D) 80 %

#### **TEST PAPER WITH SOLUTION**

- The  $K_{sp}$  for bismuth sulphide  $(Bi_2S_3)$  is  $1.08 \times 10^{-73}$ . The solubility of Bi<sub>2</sub>S<sub>3</sub> in mol L<sup>-1</sup> at
  - (A)  $1.0 \times 10^{-15}$ (B)  $2.7 \times 10^{-12}$  $\sim 10^{-8}$  $a = 10^{-10}$

(C) 
$$3.2 \times 10^{-10}$$
 (D)  $4.2 \times 10^{-10}$ 

Official Ans. by NTA (A)

Sol. 
$$Bi_2S_3 = 2Bi^{3+} + 3S^{2-}$$
  
 $2s \quad 3s$   
 $k_{sp} = (2s)^2 (3s)^3$   
 $= 4s^2 \times 27 (s)^3$   
 $= 108 (s)^5$   
 $(s)^5 = \frac{1.08 \times 10^{-73}}{108}$   
 $\Rightarrow s = 10^{-15}$ 



www.eedge.inJEE | NEET | Class 9 - 12Download App NowImage: ComparisonFinal JEE-Main Exam June, 2022/25-06-2022/Evening Session

Match List I with List II. 5. In the light of the above statements, choose the List I List II correct answer from the options given below. I. Stomach (A) Both Statement I and Statement II are true. A. Zymase B. Diastase II. Yeast (B) Both Statement I and Statement II are false. C. Urease III. Malt (C) Statement I is true but Statement II is false. (D) Statement I is false but Statement II is true. D. Pepsin IV. Soyabean Choose the correct answer from the options given Official Ans. by NTA (A) below: In the electro-refining, impure metal (here blister (A) A-II, B-III, C-I, D-IV Sol. (B) A-II, B-III, C-IV, D-I copper) is used as an anode while precious metal like Au, Pt get deposited as anode mud. (C) A-III, B-II, C-IV, D-I (D) A-III, B-II, C-I, D-IV 8. Given below are two statements one is labelled as Assertion A and the other is labelled as **Reason R**: Official Ans. by NTA (B) Assertion A : The amphoteric nature of water is explained by using Lewis acid/base concept. Sol. Zymase naturally occurs in yeast. **Reason R** : Water acts as an acid with NH<sub>3</sub> and as Diastase is found in malt. a base with H<sub>2</sub>S. Urease is found in soyabean In the light of the above statements choose the correct answer from the options given below : Pepsin is found in stomach (A) Both A and R are true and R is the correct The correct order of electron gain enthalpies of Cl, 6. explanation of A. F, Te and Po is (B) Both A and R are true but R is NOT the correct (A) F < Cl < Te < Po(B) Po < Te < F < Clexplanation of A. (D) Cl < F < Te < Po(C) Te < Po < Cl < F(C) A is true but R is false. Official Ans. by NTA (D) (D) A is false but R is true. Official Ans. by NTA (D) Sol. As Cl has maximum electron affinity among all elements.  $H_{2}S + H_{2}O \Longrightarrow H_{3}O^{+} + HS^{-}$ Acid Base Sol. Element  $\Delta_{eg}H$  (kJ/mol)  $H_2O + NH_3 \longrightarrow NH_4OH$ F -328Cl -349 9. The correct order of reduction potentials of the Те -190following pairs is Po -174A. Cl<sub>2</sub>/Cl<sup>-</sup> 7. Given below are two statements. B.  $I_2/I^-$ Statement I: During electrolytic refining, blister C.  $Ag^{+}/Ag$ copper deposits precious metals D. Na<sup>+</sup>/Na Statement II: In the process of obtaining pure E. Li<sup>+</sup>/Li copper by electrolysis method, copper blister is

Choose the correct answer from the options given below.

used to make the anode.

# Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

(A) A > C > B > D > E
(B) A > B > C > D > E
(C) A > C > B > E > D
(D) A > B > C > E > D
Official Ans. by NTA (A)

👩 eedge

Sol. 
$$E_{Cl_2/Cl^-}^{\circ} = +1.36 V$$
  
 $E_{I_2/I^-}^{\circ} = +0.54 V$   
 $E_{Ag^+/Ag}^{\circ} = +0.80 V$   
 $E_{Na^+/Na}^{\circ} = -2.71 V$   
 $E_{Li^+/Li}^{\circ} = -3.05 V$ 

**10.** The number of bridged oxygen atoms present in compound B formed from the following reactions is

(B) 1

 $Pb(NO_3)_2 \xrightarrow{673 \text{ K}} A + PbO + O_2$ 

 $A \xrightarrow{\text{Dimerise}} B$ 

(A) 0

Official Ans. by NTA (A)

Sol.

 $Pb(NO_3)_2 \xrightarrow{\Delta} PbO + NO_2 + O_2$ (A)

 $2 \underset{A}{\text{NO}_2} \xrightarrow{\text{Dimerise}} N_2 \underset{B}{O_4}$ 



(no bridged oxygen)

 The metal ion (in gaseous state) with lowest spinonly magnetic moment value is

(A) $V^{2+}$	(B) Ni <sup>2+</sup>
(C) $Cr^{2+}$	(D) Fe <sup>2+</sup>
Official Ans. by N	TA (B)



Ni<sup>2+</sup>: 
$$1s^{2} 2s^{2} 2p^{6} 3s^{2} 3p^{6} 3d^{8}$$
  
 $\boxed{12}121211 (3d) \text{ (unpaired } e^{-} = 2)$   
Cr<sup>2+</sup>:  $1s^{2} 2s^{2} 2p^{6} 3s^{2} 3p^{6} 3d^{4}$   
 $\boxed{111111} (3d) \text{ (unpaired } e^{-} = 4)$   
Fe<sup>2+</sup>:  $1s^{2} 2s^{2} 2p^{6} 3s^{2} 3p^{6} 3d^{6}$   
 $\boxed{12}11111 (3d) \text{ (unpaired } e^{-} = 4)$   
Civen below on two statements, one is labelled

12. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R Assertion A: Polluted water may have a value of BOD of the order of 17 ppm.

**Reason R:** BOD is a measure of oxygen required to oxidise both the biodegradable and nonbiodegradable organic material in water.

In the light of the above statements, choose the most appropriate answer from the options given below.

(A) Both A and R are correct and R is the correct explanation of A.

(B) Both A and R are correct but R is NOT the correct explanation of A.

- (C) A is correct but R is not correct.
- (D) A is not correct but R is correct.

Official Ans. by NTA (C)

**Sol.** Clean water have BOD less than 5 ppm while highly polluted water has BOD greater or equal to 17 ppm. So, assertion is correct.

BOD is measure of oxygen required to oxidise only bio-degradable organic matter. So, reason is false.

13. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R. Assertion A: A mixture contains benzoic acid and napthalene. The pure benzoic acid can be separated out by the use of benzene.

Reason R: Benzoic acid is soluble in hot water.



JEE | NEET | Class 9 - 12 Download App Now 
€ App Stor

Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

In the light of the above statements, choose the most appropriate answer from the options given below.

(A) Both A and R are true and R is the correct explanation of A.

(B) Both A and R are true but R is NOT the correct explanation of A.

- (C) A is true but R is false.
- (D) A is false but R is true.

Official Ans. by NTA (D)

**Sol.** Benzoic acid and Napthalene can be effectively separated by crystallization. Benzoic acid is soluble in hot water whereas Napthalene is insoluble.

Hence assertion is incorrect but reason is correct

- During halogen test, sodium fusion extract is boiled with concentrated HNO<sub>3</sub> to
  - (A) remove unreacted sodium
  - (B) decompose cyanide or sulphide of sodium
  - (C) extract halogen from organic compound
  - (D) maintain the pH of extract

Official Ans. by NTA (B)

- **Sol.** Sodium fusion extract is boiled with concentrated HNO<sub>3</sub> to remove sodium cyanide and sodium sulphide
- **15.** Amongst the following, the major product of the given chemical reaction is







Sol.



**16.** In the given reaction



(A) benzyl bromide (B) bromobenzene

- (C) cyclohexyl bromide (D) methyl bromide
- Official Ans. by NTA (B)







# Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

17. Which of the following conditions or reaction sequence will NOT give acetophenone as the major product ? (A) (a)  $C_6H_5$   $H + CH_3MgBr$  (b)  $Na_2Cr_2O_7$ ,  $H^+$ (B) (a)  $H_3C$   $H + C_6H_3MgBr$  (b) PCC, DCM (C)  $C_6H_5$   $OC_2H_5 + 2CH_3MgBr$ 

s eedge

(D)  $C_{6}H_{5}$   $Cl + CH_{3}MgBr + CdCl_{2}$ 

Official Ans. by NTA (C)

Sol.



**18.** The major product formed in the following reaction, is





Official Ans. by NTA (D)

Sol.



19. Which of the following ketone will NOT give enamine on treatment with secondary amines? [where t-Bu is -C(CH<sub>3</sub>)<sub>3</sub>]



- Official Ans. by NTA (C)
- **Sol.** Enamine formation is an example of nucleophilic addition elimination reaction

Since in ketone  $\begin{array}{c} H_3C & \bigcap \\ I & C \\ H_3C & C \\ H_3C & C \\ CH_3 & CH_3 \end{array}$  Carbonyl

Group is highly sterically hindered hence attack of nucleophile will not be possible.

#### Give yourself an extra edge

5 www.ayjr.in



www.eedge.inJEE | NEET | Class 9 - 12Download App NowDownload App NowFinal JEE-Main Exam June, 2022/25-06-2022/Evening Session

20. An antiseptic dettol is a mixture of two compounds 'A' and 'B' where A has 6π electrons and B has 2π electrons. What is 'B'?
(A) Bithionol

- (B) Terpineol
- (C) Chloroxylenol
- (D) Chloramphenicol

Official Ans. by NTA (B)

Sol. Dettol is mixture of



Chloroxylenol (Compound A) It has  $6\pi e^-$  Terpineol (Compound B) It has  $2\pi e^-$ 

Hence compound 'B' is Terpineol.

#### **SECTION-B**

 A protein 'A' contains 0.30% of glycine (molecular weight 75). The minimum molar mass of the protein 'A' is \_\_\_\_\_ × 10<sup>3</sup> g mol<sup>-1</sup> [nearest integer]

Official Ans. by NTA (25)

**Sol.** 0.30 % glycine is equal to 75

$$1 \% \longrightarrow \frac{75}{0.30}$$
$$100 \% \longrightarrow \frac{75}{0.30} \times 100$$
$$= 25000 \text{ g}$$

2. A rigid nitrogen tank stored inside a laboratory has a pressure of 30 atm at 06:00 am when the temperature is 27 °C. At 03:00 pm, when the temperature is 45°C, the pressure in the tank will be \_\_\_\_\_\_atm. [nearest integer]

Official Ans. by NTA (32)

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$
$$\frac{30}{300} = \frac{P_2}{318}$$
$$P_2 = \frac{30}{300} \times 318$$
$$= \frac{1}{10} \times 318$$
$$= 32$$

Sol.

**3.** Amongst BeF<sub>2</sub>, BF<sub>3</sub>, H<sub>2</sub>O, NH<sub>3</sub>, CCl<sub>4</sub> and HCl, the number of molecules with non-zero net dipole moment is \_\_\_\_\_.

Official Ans. by NTA (3)

**Sol.** BeF<sub>2</sub>, BF<sub>3</sub> and CCl<sub>4</sub>  $\Rightarrow \mu_{net} = 0$ H<sub>2</sub>O, NH<sub>3</sub> and HCl  $\Rightarrow \mu_{net} \neq 0$ 

4. At 345 K, the half life for the decomposition of a sample of a gaseous compound initially at 55.5 kPa was 340 s. When the pressure was 27.8 kPa, the half life was fund to be 170 s. The order of the reaction is \_\_\_\_\_. [integer answer]

Official Ans. by NTA (0)

Sol. 
$$t_{1/2} \times \frac{1}{[P_0]^{n-1}}$$
  
 $\frac{t_1}{t_2} = \frac{(P_2)^{n-1}}{(P_1)^{n-1}}$   
 $\frac{340}{170} = \left(\frac{27.8}{55.5}\right)^{n-1}$   
 $\Rightarrow 2 = \frac{1}{(2)^{n-1}}$   
 $n = 0$ 

5. A solution of  $Fe_2(SO_4)_3$  is electrolyzed for 'x' min with a current of 1.5 A to deposit 0.3482 g of Fe. The value of x is\_\_\_\_\_. [nearest integer] Given : 1 F = 96500 C mol<sup>-1</sup> Atomic mass of Fe = 56 g mol<sup>-1</sup> Official Ans. by NTA (20)

Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

**Sol.**  $Fe^{3+} + 3e^{-} \longrightarrow Fe$  $3F \longrightarrow 1$  mole Fe is deposited For 56 g  $\longrightarrow$  3 × 96500 (required charge) For 1g  $\longrightarrow \frac{3 \times 96500}{56}$  (required charge) For 0.3482 g  $\longrightarrow \frac{3 \times 96500}{56} \times 0.3482$ = 1800.06Q = it1800.06 = 1.5 t $t = 20 \min$ 6. Consider the following reactions :  $PCl_3 + H_2O \longrightarrow A + HCl$  $A + H_2O \longrightarrow B + HCl$ number of ionisable protons present in the product B\_\_\_\_\_ . Official Ans. by NTA (2) **Sol.**  $PCl_3+H_2O \xrightarrow{Partial} PCl_2(OH)$  (or)  $PCl(OH)_2 +$ HCl PCl<sub>2</sub>(OH) (or) PCl(OH)<sub>2</sub> water no. of ionisable protons in B = 27. Amongst FeCl<sub>3</sub>.3H<sub>2</sub>O,  $K_3[Fe(CN)_6]$ and [Co(NH<sub>3</sub>)<sub>6</sub>]Cl<sub>3</sub>, the spin-only magnetic moment value of the inner-orbital complex that absorbs light at shortest wavelength is \_\_\_\_\_ B.M. [nearest integer] Official Ans. by NTA (2) Sol.  $[Fe(H_2O)_3Cl_3], \underbrace{K_3[Fe(CN)_6], [Co(NH_3)_6]Cl_3}_{inner orbital complexes}$ 

 $K_3[Fe(CN)_6]$  has more value of  $\Delta_0$  than that of [Co(NH<sub>3</sub>)<sub>6</sub>]Cl<sub>3</sub>; as  $\overline{C}N$  is stronger ligand. More  $\Delta_0 \Rightarrow$  smaller value of absorbed  $\lambda$ 

$$\begin{array}{cccc} K_{3}[Fe(CN)_{6}]: \ Fe^{3+} & : \ 3d^{5} & 4s^{0} & 4p^{0} \\ & & & \\ \hline 1 \ unpaired \ e^{-} & d^{2}sp^{3} \end{array}$$

Spin only magnetic moment ( $\mu$ ) =  $\sqrt{3}$  BM = 1.732 BM

Rounding off  $\Rightarrow 2$ 

The Novolac polymer has mass of 963 g. The number of monomer units present in it are Official Ans. by NTA (9)

Sol. Monomer unit of Novolac is  $\bigcirc$  CH<sub>2</sub>OH its

molecular mass is 124 amu.

Upon considering molecular weight of polymer as 963 amu (In question its given as 963 gram) Now if during formation of Novolac, (n–1) unit of water are removed then

 $n \times 124 = 963 + [18 \times (n-1)]$ 

n = 9

9. How many of the given compounds will give a positive Biuret test \_\_\_\_\_? Glycine, Glycylalanine, Tripeptide, Biuret Official Ans. by NTA (2)

- Sol. Biuret test is given by all proteins and peptides having atleast two peptide linkages.Hence positive test must be given by tripeptide and Biuret.
- 10. The neutralization occurs when 10 mL of 0.1 M acid 'A' is allowed to react with 30 mL of 0.05 M base M(OH)<sub>2</sub>. The basicity of the acid 'A' is\_\_\_\_\_. [M is a metal]
  Official Ans. by NTA (3)

Sol.	Acid	+ Base	$\longrightarrow$	Salt + $H_2O$
	0.1 M	M(OH) <sub>2</sub>		
	10ml	0.05 M		
		30 ml		
	at equivalence point equivalent of acid = equivalent of base			
	0.1 × 10 >	$< n = 30 \times 0.05$	$5 \times 2$	
		n = 3		



## **FINAL JEE-MAIN EXAMINATION - JUNE, 2022**

3.

# (Held On Saturday 25<sup>th</sup>June, 2022)

TIME: 3:00 PM to 6:00 PM

Let  $z_1$  and  $z_2$  be two complex numbers such that

# MATHEMATICS

#### SECTION-A

1. Let  $A = \{x \in R : |x+1| < 2\}$  and

 $B = \{x \in R : |x - 1| \ge 2\}.$  Then which one of the

following statements is **NOT** true ?

- (A) A B = (-1, 1) (B) B A = R (-3, 1)
- (C)  $A \cap B = (-3, -1]$  (D)  $A \cup B = R [1, 3)$
- Official Ans. by NTA (B)

Sol. 
$$A: x \in (-3, 1)$$
  $B: x \in (-\infty, -1] \cup [3, \infty)$   
 $B - A = (-\infty, -3] \cup [3, \infty) = R - (-3, 3)$ 

- 2. Let  $a, b \in R$  be such that the equation  $ax^2 - 2bx + 15 = 0$  has a repeated root  $\alpha$ . If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 - 2bx + 21 = 0$ , then  $\alpha^2 + \beta^2$  is equal to:
  - (A) 37
    (B) 58
    (C) 68
    (D) 92

Official Ans. by NTA (B)

**Sol.**  $ax^2 - 2bx + 15 = 0$ 

$$2\alpha = \frac{2b}{a}, \alpha^2 = \frac{15}{a}$$
$$\frac{\alpha}{2} = \frac{15}{2b}$$
$$\alpha = \frac{15}{b}$$
$$x^2 - 2bx + 21 = 0$$
$$\left(\frac{15}{b}\right)^2 - 2b\left(\frac{15}{b}\right) + 21 = 0$$
$$b^2 = 25$$
$$\alpha + \beta = 2b, \ \alpha\beta = 21$$
$$\alpha^2 + \beta^2 = 4b^2 - 42$$
$$= 58$$

$$\overline{z}_1 = i\overline{z}_2 \text{ and } \arg\left(\frac{z_1}{\overline{z}_2}\right) = \pi$$
. Then  
(A)  $\arg z_2 = \frac{\pi}{4}$  (B)  $\arg z_2 = -\frac{3\pi}{4}$ 

**TEST PAPER WITH SOLUTION** 

(C) 
$$\arg z_1 = \frac{\pi}{4}$$
 (D)  $\arg z_1 = -\frac{3\pi}{4}$ 

Official Ans. by NTA (C)

Sol. 
$$\overline{z}_1 = i\overline{z}_2$$
  
 $z_1 = -iz_2$   
 $arg\left(\frac{z_1}{z_2}\right) = \pi$   
 $arg\left(-i\frac{z_2}{\overline{z}_2}\right) = \pi$   $arg(z_2) = \theta$   
 $-\frac{\pi}{2} + \theta + \theta = \pi$   
 $2\theta = \frac{3\pi}{2}$   
 $arg(z_2) = \theta = \frac{3\pi}{4}$ ,  $arg z_1 = \frac{\pi}{4}$   
4. The system of equations  
 $-kx + 3y - 14z = 25$   
 $-15x + 4y - kz = 3$   
 $-4x + y + 3z = 4$   
is consistent for all k in the set  
(A) R (B) R - {-11,13}  
(C) R - {13} (D) R - {-11,11}

Official Ans. by NTA (D)



www.eedge.inJEE | NEET | Class 9 - 12Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

Sol. 
$$\Delta = \begin{vmatrix} -k & 3 & -14 \\ -15 & 4 & -k \\ -4 & 1 & 3 \end{vmatrix} = 121 - k^2$$
$$\Delta \neq 0 \qquad k \in \mathbb{R} - \{11, -11\} \text{ (Unique sol.)}$$
If k = 11
$$\Delta_z = \begin{vmatrix} -11 & 3 & 25 \\ -15 & 4 & 3 \\ -4 & 1 & 4 \end{vmatrix} \neq 0$$
No colution

No solution

If k = -11

$$\Delta_z = \begin{vmatrix} 11 & 3 & 25 \\ -15 & 4 & 3 \\ -4 & 1 & 4 \end{vmatrix} \neq 0$$

No solution

5. 
$$\lim_{x \to \frac{\pi}{2}} \left( \tan^2 x \left( \left( 2\sin^2 x + 3\sin x + 4 \right)^{\frac{1}{2}} - \left( \sin^2 x + 6\sin x + 2 \right)^{\frac{1}{2}} \right) \right)$$

is equal to

(A) 
$$\frac{1}{12}$$
 (B)  $-\frac{1}{18}$   
(C)  $-\frac{1}{12}$  (D)  $-\frac{1}{6}$ 

Official Ans. by NTA (A)

Sol.

 $\lim_{x \to \frac{\pi}{2}} \tan^2 x \left[ \sqrt{2\sin^2 x + 3\sin x + 4} - \sqrt{\sin^2 x + 6\sin x + 2} \right] =$ 

$$\lim_{x \to \frac{\pi}{2}} \frac{\tan^2 x \, [\sin^2 x - 3\sin x + 2]}{\sqrt{9} + \sqrt{9}}$$
  
= 
$$\lim_{x \to \frac{\pi}{2}} \frac{\tan^2 x (\sin x - 1)(\sin x - 2)}{6}$$
  
= 
$$\frac{1}{6} \lim_{x \to \frac{\pi}{2}} \tan^2 x (1 - \sin x)$$
  
= 
$$\frac{1}{6} \lim_{x \to \frac{\pi}{2}} \frac{\sin^2 x \, (1 - \sin x)}{(1 - \sin x)(1 + \sin x)} = \frac{1}{12}$$

6. The area of the region enclosed between the parabolas  $y^2 = 2x - 1$  and  $y^2 = 4x - 3$  is

(A) 
$$\frac{1}{3}$$
 (B)  $\frac{1}{6}$   
(C)  $\frac{2}{3}$  (D)  $\frac{3}{4}$ 

Official Ans. by NTA (A)

**Sol.** Required area =  $2 \int_{0}^{1} \left( \frac{y^2 + 3}{4} - \frac{y^2 + 1}{2} \right) dy$ 



7. The coefficient of  $x^{101}$  in the expression  $(5+x)^{500} + x(5+x)^{499} + x^2(5+x)^{498} + \dots x^{500}$ ,

x > 0, is

(A) 
$${}^{501}C_{101}(5){}^{399}$$
 (B)  ${}^{501}C_{101}(5){}^{400}$ 

(C)  ${}^{501}C_{100}(5){}^{400}$  (D)  ${}^{500}C_{101}(5){}^{399}$ 

Official Ans. by NTA (A)

**Sol.**  $(5+x)^{500} + x(5+x)^{499} + x^2(5+x)^{498} + \dots + x^{500}$ 

$$=\frac{(5+x)^{501}-x^{501}}{(5+x)-x}=\frac{(5+x)^{501}-x^{501}}{5}$$

 $\Rightarrow$  coefficient  $x^{101}$  in given expression

$$=\frac{{}^{501}\mathrm{C}_{101}5^{400}}{5}={}^{501}\mathrm{C}_{101}5^{399}$$

Give yourself an extra edge

2 www.ayjr.in

EE-Main Exam June, 2022/25-06-2022/Evening Session

8. The sum 
$$1 + 2 \cdot 3 + 3 \cdot 3^2 + \dots + 10 \cdot 3^9$$
 is equal to

(A)  $\frac{2 \cdot 3^{12} + 10}{4}$ (B)  $\frac{19 \cdot 3^{10} + 1}{4}$ (D)  $\frac{9\cdot 3^{10}+1}{2}$ (C)  $5 \cdot 3^{10} - 2$ 

Official Ans. by NTA (B)

Sol. 
$$S = 1 \cdot 3^{0} + 2 \cdot 3^{1} + 3 \cdot 3^{2} + \dots + 10 \cdot 3^{9}$$
  
 $3S = 1 \cdot 3^{1} + 2 \cdot 3^{2} \dots + 9 \times 3^{9} + 10 \times 3^{10}$   
 $-2S = (1 \cdot 3^{0} + 3^{1} + 3^{2} \dots 3^{9}) - 10 \cdot 3^{10}$   
 $S = 5 \times 3^{10} - \left(\frac{3^{10} - 1}{4}\right)$   
 $S = \frac{20 \cdot 3^{10} - 3^{10} + 1}{4} = \frac{19 \cdot 3^{10} + 1}{4}$ 

Let P be the plane passing through the intersection 9. of the planes

> $\vec{r} \cdot (\hat{i} + 3\hat{j} - \hat{k}) = 5$  and  $\vec{r} \cdot (2\hat{i} - \hat{j} + \hat{k}) = 3$ , and the point (2,1,-2). Let the position vectors of the points X and Y be  $\hat{i} - 2\hat{j} + 4\hat{k}$  and  $5\hat{i} - \hat{j} + 2\hat{k}$ respectively. Then the points (A) X and X + Y are on the same side of P

(B) Y and Y - X are on the opposite sides of P

(C) X and Y are on the opposite sides of P

(D) X + Y and X - Y are on the same side of P Official Ans. by NTA (C)

**Sol.**  $P_1 + \lambda P_2 = 0$  $\Rightarrow (x+3y-z-5)+\lambda(2x-y+z-3)=0$ (2,1,-2) lies on this plane

 $\therefore \lambda = 1 \implies$  plane is 3x + 2y - 8 = 0

10. A circle touches both the y-axis and the line x + y = 0. Then the locus of its center is

(A) 
$$y = \sqrt{2}x$$
 (B)  $x = \sqrt{2}y$ 

(C) 
$$y^2 - x^2 = 2xy$$
 (D)  $x^2 - y^2 = 2xy$ 

Official Ans. by NTA (D)

**Sol.** Let (h, k) is centre of circle

$$\left|\frac{\mathbf{h}-\mathbf{k}}{\sqrt{2}}\right| = \left|\mathbf{h}\right|$$

 $k^{2} - h^{2} + 2hk = 0$ 

 $\therefore$  Equation of locus is  $y^2 - x^2 + 2xy = 0$ 



Water is being filled at the rate of  $1 \text{ cm}^3 / \text{sec}$  in a 11. right circular conical vessel (vertex downwards) of height 35 cm and diameter 14 cm. When the height of the water level is 10 cm, the rate  $(in \text{ cm}^2 / \text{sec})$ at which the wet conical surface area of the vessel increases is

(A) 5 (B) 
$$\frac{\sqrt{21}}{5}$$
  
(C)  $\frac{\sqrt{26}}{5}$  (D)  $\frac{\sqrt{26}}{10}$   
Official Ans. by NTA (C)

**Sol.** From figure 
$$\frac{r}{h} = \frac{7}{35} \Rightarrow h = 5r$$

Given 
$$\frac{dV}{dt} = 1 \Rightarrow \frac{d}{dt} \left( \frac{\pi r^2 h}{3} \right) = 1$$

$$\Rightarrow \frac{\mathrm{d}}{\mathrm{dt}} \left( \frac{5\pi}{3} r^3 \right) = 1 \Rightarrow r^2 \frac{\mathrm{d}r}{\mathrm{dt}} = \frac{1}{5\pi}$$

Let wet conical surface area = S

$$= \pi r \ell = \pi r \sqrt{h^2 + r^2}$$
$$= \sqrt{26}\pi r^2 \Rightarrow \frac{dS}{dt} = 2\sqrt{26}\pi r \frac{dr}{dt}$$
When h = 10 then r = 2  $\Rightarrow \frac{dS}{dt} = \frac{2\sqrt{2}}{10}$ 

/26



www.eedge.inJEE | NEET | Class 9 - 12Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

12. If 
$$b_n = \int_0^{\frac{\pi}{2}} \frac{\cos^2 nx}{\sin x} dx$$
,  $n \in N$ , then  
(A)  $b_3 - b_2$ ,  $b_4 - b_3$ ,  $b_5 - b_4$  are in an A.P. with  
common difference -2  
(B)  $\frac{1}{b_3 - b_2}$ ,  $\frac{1}{b_4 - b_3}$ ,  $\frac{1}{b_5 - b_4}$  are in an A.P. with  
common difference 2  
(C)  $b_3 - b_2$ ,  $b_4 - b_3$ ,  $b_5 - b_4$  are in a G.P.  
(D)  $\frac{1}{b_3 - b_2}$ ,  $\frac{1}{b_4 - b_3}$ ,  $\frac{1}{b_5 - b_4}$  are in an A.P. with  
common difference -2  
Official Ans. by NTA (D)  
Sol.  $b_n = \int_0^{\frac{\pi}{2}} \frac{1 + \cos 2nx}{\sin x} dx$   
 $b_{n+1} - b_n = \int_0^{\frac{\pi}{2}} \frac{\cos^2(n+1)x - \cos^2 nx}{\sin x} dx$   
 $= \int_0^{\frac{\pi}{2}} \frac{-\sin(2n+1)x}{\sin x} dx$   
 $= \left(\frac{\cos(2n+1)x}{2n+1}\right)^{\frac{\pi}{2}} = \frac{-1}{2n+1}$ 

$$\frac{1}{b_3 - b_2}, \frac{1}{b_4 - b_3}, \frac{1}{b_5 - b_4}$$
 are in A.P. with c.d.= -2

13. If y = y(x) is the solution of the differential equation  $2x^2 \frac{dy}{dx} - 2xy + 3y^2 = 0$  such that

y(e) = 
$$\frac{e}{3}$$
, then y(1) is equal to  
(A)  $\frac{1}{3}$  (B)  $\frac{2}{3}$   
(C)  $\frac{3}{2}$  (D) 3

Official Ans. by NTA (B)

Sol. 
$$\frac{dy}{dx} - \frac{y}{x} = -\frac{3}{2} \left(\frac{y}{x}\right)^2 \qquad y = vx$$
$$\frac{dv}{v^2} = -\frac{3dx}{2x}$$
$$-\frac{1}{v} = -\frac{3}{2} \ln |x| + C$$
$$-\frac{x}{y} = \frac{-3}{2} \ln |x| + C$$
$$x = e, \ y = \frac{e}{3}$$
$$C = -\frac{3}{2}$$
When  $x = 1, \ y = \frac{2}{3}$ 

14. If the angle made by the tangent at the point  $(x_0, y_0)$  on the curve  $x = 12(t + \sin t \cos t)$ ,

 $y = 12(1 + \sin t)^2, 0 < t < \frac{\pi}{2}$ , with the positive x-axis

1s 
$$\frac{1}{3}$$
, then  $y_0$  is equal to  
(A)  $6(3+2\sqrt{2})$  (B)  $3(7+4\sqrt{3})$   
(C) 27 (D) 48

Official Ans. by NTA (C)

π

Sol. 
$$\frac{dy}{dx} = \frac{2(1+\sin t) \times \cos t}{1+\cos 2t}$$
$$\Rightarrow \frac{2(1+\sin t)\cos t}{2\cos^2 t} = \sqrt{3}$$
$$\Rightarrow t = \frac{\pi}{6}, y_0 = 27$$

**15.** The value of  $2\sin(12^\circ) - \sin(72^\circ)$  is :

(A) 
$$\frac{\sqrt{5}(1-\sqrt{3})}{4}$$
 (B)  $\frac{1-\sqrt{5}}{8}$   
(C)  $\frac{\sqrt{3}(1-\sqrt{5})}{2}$  (D)  $\frac{\sqrt{3}(1-\sqrt{5})}{4}$ 

Official Ans. by NTA (D)

JEE | NEET | Class 9 - 12 Download App Now

Sol.  $\sin 12^{\circ} + \sin 12^{\circ} - \sin 72^{\circ}$ =  $\sin 12^{\circ} - 2\cos 42^{\circ}\sin 30^{\circ}$ =  $\sin 12^{\circ} - \sin 48^{\circ}$ =  $-2\cos 30^{\circ}\sin 18^{\circ}$ =  $-2 \times \frac{\sqrt{3}}{2} \times \frac{\sqrt{5} - 1}{4}$ 

$$=\frac{\sqrt{3}}{4}(1\!-\!\sqrt{5})$$

16. A biased die is marked with numbers 2,4, 8, 16, 32, 32 on its faces and the probability of getting a face with mark n is  $\frac{1}{n}$ . If the die is thrown thrice, then the probability, that the sum of the numbers obtained is 48, is

(A) 
$$\frac{7}{2^{11}}$$
 (B)  $\frac{7}{2^{12}}$   
(C)  $\frac{3}{2^{10}}$  (D)  $\frac{13}{2^{12}}$ 

Official Ans. by NTA (D)

# **Sol.** $P(n) = \frac{1}{n}$

P(2) = 
$$\frac{1}{2}$$
 P(8) =  $\frac{1}{8}$   
P(4) =  $\frac{1}{4}$  P(16) =  $\frac{1}{16}$ 

 $P(32) = \frac{2}{32}$ 

Possible cases

16, 16, 16 and 32, 8, 8

Probability = 
$$\frac{1}{16^3} + \frac{2}{32} \times \frac{1}{8} \times \frac{1}{8} \times 3 = \frac{13}{16^3}$$

17. The negation of the Boolean expression  $((\sim q) \land p) \Rightarrow ((\sim p) \lor q)$  is logically equivalent to

(A) 
$$p \Rightarrow q$$
 (B)  $q \Rightarrow p$ 

(C) 
$$\sim (p \Rightarrow q)$$
 (D)  $\sim (q \Rightarrow p)$ 

Official Ans. by NTA (C)

Sol.  $\sim p \lor q \equiv p \rightarrow q$   $\sim q \land p \equiv \sim (p \rightarrow q)$ Negation of  $\sim (p \rightarrow q) \rightarrow (p \rightarrow q)$ is  $\sim (p \rightarrow q) \land (\sim (p \rightarrow q))$  i.e.  $\sim (p \rightarrow q)$ 

18. If the line y = 4 + kx, k > 0, is the tangent to the parabola  $y = x - x^2$  at the point P and V is the vertex of the parabola, then the slope of the line through P and V is :

(A) 
$$\frac{3}{2}$$
 (B)  $\frac{26}{9}$   
(C)  $\frac{5}{2}$  (D)  $\frac{23}{6}$ 

Official Ans. by NTA (C)

**Sol.** Slope of tangent at P = Slope of line AP

$$y'|_{P} = 1 - 2\alpha = \frac{\alpha - \alpha^2 - 4}{\alpha}$$

Solving  $\alpha = -2 \Rightarrow P(-2, -6)$ 

Slope of PV = 
$$\frac{5}{2}$$



**19.** The value of  $\tan^{-1}\left(\frac{\cos\left(\frac{15\pi}{4}\right) - 1}{\sin\left(\frac{\pi}{4}\right)}\right)$  is equal to

(A) 
$$-\frac{\pi}{4}$$
 (B)  $-\frac{\pi}{8}$ 

(C) 
$$-\frac{5\pi}{12}$$
 (D)  $-\frac{4\pi}{9}$ 

Official Ans. by NTA (B)



www.eedge.in Download Ap

JEE | NEET | Class 9 - 12 Download App Now € AppStor

Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

Sol. 
$$\tan^{-1}\left[\frac{\cos\left(4\pi - \frac{\pi}{4}\right) - 1}{\sin\frac{\pi}{4}}\right] \Rightarrow \tan^{-1}\left(\frac{\cos\frac{\pi}{4} - 1}{\sin\frac{\pi}{4}}\right)$$
  
 $\tan^{-1}\left(\frac{1 - \sqrt{2}}{1}\right) = -\frac{\pi}{8}$ 

20. The line 
$$y = x + 1$$
 meets the ellipse  $\frac{x^2}{4} + \frac{y^2}{2} = 1$  at  
two points P and Q. If r is the radius of the circle  
with PQ as diameter then  $(3r)^2$  is equal to  
(A) 20 (B) 12

(C) 11 (D) 8

Official Ans. by NTA (A)

**Sol.** Ellipse  $x^2 + 2y^2 = 4$ 

Line y = x + 1Point of intersection

 $x^{2} + 2(x+1)^{2} = 4$   $3x^{2} + 4x - 2 = 0$  $|x_{1} - x_{2}| = \frac{\sqrt{40}}{3}$ 

$$AB = 2r = |x_1 - x_2| \sqrt{1 + m^2}$$

m is slope of given line

$$AB = \frac{\sqrt{40}}{3} \sqrt{1+1}$$

$$2r = \frac{\sqrt{80}}{3} \Rightarrow r = \frac{\sqrt{80}}{6}$$

$$(3r)^{2} = \left(3 \times \frac{\sqrt{80}}{6}\right)^{2} = \frac{80}{4} = 20$$

$$(0,\overline{2})$$

$$AB = 2r$$

$$AB = 2r$$

1

**SECTION-B** 

1. Let 
$$A = \begin{pmatrix} 2 & -2 \\ 1 & -1 \end{pmatrix}$$
 and  $B = \begin{pmatrix} -1 & 2 \\ -1 & 2 \end{pmatrix}$ . Then the

number of elements in the set

$$\label{eq:and_states} \begin{split} &\{(n,m):n,m\in\{1,2,....,10\} \ \ and \ \ \ nA^n+mB^m=I\} \\ & \text{is } \_\_\_ \end{split}$$

Official Ans. by NTA (1)

**Sol.** 
$$A^2 = A$$
 and  $B^2 = B$ 

Therefore equation  $nA^n + mB^m = I$  becomes

nA + mB = I, which gives m = n = 1

Only one set possible

2. Let  $f(x) = [2x^2 + 1]$  and  $g(x) = \begin{cases} 2x - 3, & x < 0 \\ 2x + 3, & x \ge 0 \end{cases}$ 

where [t] is the greatest integer  $\leq t$ . Then, in the open interval (-1, 1), the number of points where fog is discontinuous is equal to \_\_\_\_\_

Official Ans. by NTA (62)

**Sol.** 
$$f(g(x)) = [2g^2(x)]$$

$$= \begin{cases} \left[ 2(2x-3)^2 \right] + 1; \ x < 0 \\ \left[ 2(2x+3)^2 \right] + 1; \ x \ge 0 \end{cases}$$

∴ fog is discontinuous whenever  $2(2x-3)^2$  or  $2(2x+3)^2$  belongs to integer except x = 0.

+1

 $\therefore$  62 points of discontinuity.

3. The value of b > 3 for which

$$12\int_{3}^{b} \frac{1}{(x^{2}-1)(x^{2}-4)} dx = \log_{e}\left(\frac{49}{40}\right), \text{ is equal to}$$

Official Ans. by NTA (6)

JEE | NEET | Class 9 - 12 Download App Now

ain Exam June, 2022/25-06-2022/Evening Session

Sol. 
$$\frac{12}{3} \left[ \int_{3}^{b} \left( \frac{1}{x^{2} - 4} - \frac{1}{x^{2} - 1} \right) dx \right] = \log \frac{49}{40}$$
$$\frac{12}{3} \left[ \frac{1}{4} \ell n \left| \frac{x - 2}{x + 2} \right| - \frac{1}{2} \ell n \left| \frac{x - 1}{x + 1} \right| \right]_{3}^{b} = \log \frac{49}{40}$$
$$\ell n \frac{(b - 2)(b + 1)^{2}}{(b + 2)(b - 1)^{2}} = \ell n \frac{49}{50}$$
$$h = 6$$

4. If the sum of the coefficients of all the positive even powers of x in the binomial expansion of

$$\left(2x^3+\frac{3}{x}\right)^{10}$$
 is  $5^{10}-\beta\cdot3^9$ , then  $\beta$  is equal to \_\_\_\_\_

#### Official Ans. by NTA (83)

- Sol.  $T_{r+1} = {}^{10} C_r (2x^3)^{10-r} \left(\frac{3}{x}\right)^r$ =  ${}^{10} C_r 2^{10-r} 3^r x^{30-4r}$ Put r = 0, 1, 2, .... 7 and we get  $\beta = 83$ 5. If the mean deviation about the mean of the
- numbers 1, 2, 3, ...., n, where n is odd, is  $\frac{5(n+1)}{n}$ , then n is equal to \_\_\_\_\_\_

#### Official Ans. by NTA (21)

- Sol. Mean deviation about mean of first n natural numbers is  $\frac{n^2 - 1}{4n}$  $\therefore$  n = 21
- 6. Let  $\vec{b} = \hat{i} + \hat{j} + \lambda \hat{k}, \lambda \in \mathbb{R}$ . If  $\vec{a}$  is a vector such that  $\vec{a} \times \vec{b} = 13\hat{i} - \hat{j} - 4\hat{k}$  and  $\vec{a} \cdot \vec{b} + 21 = 0$ , then  $(\vec{b} - \vec{a}) \cdot (\hat{k} - \hat{j}) + (\vec{b} + \vec{a}) \cdot (\hat{i} - \hat{k})$  is equal to Official Ans. by NTA (14)

Sol. 
$$(\vec{a} \times \vec{b}).\vec{b} = 0$$
  
 $\Rightarrow 13 - 1 - 4\lambda = 0 \Rightarrow \lambda = 3$   
 $\Rightarrow \vec{b} = \hat{i} + \hat{j} + 3\hat{k} \Rightarrow \vec{a} \times \vec{b} = 13\hat{i} - \hat{j} - 4\hat{k}$   
 $\Rightarrow (\vec{a} \times \vec{b}) \times \vec{b} = (13\hat{i} - \hat{j} - 4\hat{k}) \times (\hat{i} + \hat{j} + 3\hat{k})$   
 $\Rightarrow -21\vec{b} - 11\vec{a} = \hat{i} - 43\hat{j} + 14\hat{k}$   
 $\Rightarrow \vec{a} = -2\hat{i} + 2\hat{j} - 7\hat{k}$ 

Now  $(\vec{b} - \vec{a}) \cdot (\hat{k} - \hat{j}) + (\vec{b} + \vec{a}) \cdot (\hat{i} - \hat{k}) = 14$ 

 The total number of three-digit numbers, with one digit repeated exactly two times, is

Official Ans. by NTA (243)

- Sol. If 0 taken twice then ways = 9 If 0 taken once then  ${}^{9}C_{1} \times 2 = 18$ If 0 not taken then  ${}^{9}C_{1} {}^{8}C_{1} \cdot 3 = 216$ Total = 243
  - Let  $f(x) = |(x-1)(x^2 2x 3)| + x 3$ ,  $x \in \mathbb{R}$ . If m and M are respectively the number of points of local minimum and local maximum of f in the interval (0, 4), then m + M is equal to \_\_\_\_\_

Official Ans. by NTA (3)

Sol. 
$$f(x) = \begin{cases} (x^2 - 1)(x - 3) + (x - 3), x \in (0, 1] \cup [3, 4) \\ -(x^2 - 1)(x - 3) + (x - 3), x \in [1, 3] \end{cases}$$
  
$$\Rightarrow f'(x) = \begin{cases} 3x^2 - 6x, x \in (0, 1) \cup (3, 4) \\ -3x^2 + 6x + 2, x \in (1, 3) \end{cases}$$

f(x) is non-derivable at x = 1 and x = 3

also f'(x) = 0 at x = 1 + 
$$\sqrt{\frac{5}{3}} \implies m + M = 3$$

### Give yourself an extra edge

8.



www.eedge.inJEE | NEET | Class 9 - 12Final JEE-Main Exam June, 2022/25-06-2022/Evening Session

 $8x + 4\sqrt{2}y = 1, z = 0$ Let the eccentricity of the hyperbola  $\frac{x^2}{x^2} - \frac{y^2}{b^2} = 1$ Sol. 9.  $\Rightarrow \frac{x - \frac{1}{8}}{1} = \frac{y - 0}{\sqrt{2}} = \frac{z - 0}{0} = \lambda$ be  $\frac{5}{4}$ . If the equation of the normal at the point  $-8x - 6\sqrt{3}z = 1, y = 0$  $\left(\frac{8}{\sqrt{5}},\frac{12}{5}\right)$  on the hyperbola is  $8\sqrt{5}x + \beta y = \lambda$ , then  $\Rightarrow \frac{x+\frac{1}{8}}{2\sqrt{2}} = \frac{y-0}{0} = \frac{z-0}{-4}$  $\lambda - \beta$  is equal to  $\begin{vmatrix} \frac{1}{4} & 0 & 0\\ 1 & -\sqrt{2} & 0\\ 3\sqrt{3} & 0 & -4 \end{vmatrix} = \sqrt{2}$ Official Ans. by NTA (85)  $e^{2} = 1 + \frac{b^{2}}{a^{2}} = \frac{25}{16} \Rightarrow \frac{b^{2}}{a^{2}} = \frac{9}{16}$  .....(1) Sol.  $d = \frac{1}{\sqrt{51}}$  $A\left(\frac{8}{\sqrt{5}},\frac{12}{5}\right)$  satisfies  $\frac{x^2}{a^2}-\frac{y^2}{b^2}=1$  $\frac{1}{d^2} = 51$  $\Rightarrow \frac{64}{5a^2} - \frac{144}{25b^2} = 1$  .....(2) Solving (1) & (2)  $b = \frac{6}{5} a = \frac{8}{5}$ JEE READY? Normal at A is  $\frac{\sqrt{5}a^2x}{8} + \frac{5b^2y}{12} = a^2 + b^2$ Comparing it  $8\sqrt{5}x + \beta y = \lambda$ Gives  $\lambda = 100$ ,  $\beta = 15$  $\lambda - \beta = 85$ Let  $l_1$  be the line in xy-plane with x and y 10. intercepts  $\frac{1}{8}$  and  $\frac{1}{4\sqrt{2}}$  respectively, and  $l_2$  be the line in zx-plane with x and z intercepts  $-\frac{1}{8}$  and  $-\frac{1}{6\sqrt{2}}$  respectively. If d is the shortest distance between the line  $l_1$  and  $l_2$ , then  $d^{-2}$  is equal to Official Ans. by NTA (51)