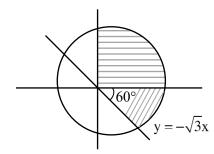


(He	FINAL JEE-MAIN EXAM Id On Friday 05th April, 2024)	IINA	TION – APRIL, 2024 TIME : 3 : 00 PM to 6 : 00 PM
	MATHEMATICS		TEST PAPER WITH SOLUTION
1. Sol.	<b>MATHEMATICS</b> <b>SECTION-A</b> Let $f: [-1, 2] \rightarrow \mathbb{R}$ be given by $f(x) = 2x^2 + x + [x^2] - [x]$ , where [t] denotes the greatest integer less than or equal to t. The number of points, where $f$ is not continuous, is : (1) 6 (2) 3 (3) 4 (4) 5 <b>Ans. (3)</b> Doubtful points : $-1, 0, 1, \sqrt{2}, \sqrt{3}, 2$ at $x = \sqrt{2}, \sqrt{3}$ $f(x) = (2x^2 + x - [x]) + [x^2] = Discount$ $\downarrow_{Cont.}$ at $x = -1$ : $RHL \Rightarrow f(x) = (2 - 1 - (-1)) + 0 = 2$ f(-1) = 2 - 1 - (-1) + 1 = 3 dt x = 2: LHL $\Rightarrow f(x) = 8 + 2 - 1 + 3 = 12$ f(2) = 8 + 2 - 2 + 4 = 12 f(2) = 8 + 2 - 2 + 4 = 12 f(0) = 0 Dis.	3.	$C = x^{2} + y^{2} + gx + gy = 0 \qquad \dots (1)$ 2x + 2yy' + g + gy' = 0 $g = -\left(\frac{2x + 2yy'}{1 + y'}\right)$ Put in (1) $x^{2} + y^{2} - \left(\frac{2x + 2yy'}{1 + y'}\right)(x + y) = 0$ $(x^{2} - y^{2} - 2xy)y' = x^{2} - y^{2} + 2xy$ Let S <sub>1</sub> = {z \in C :  z  \le 5}, S <sub>2</sub> = {z \in C : Im $\left(\frac{z + 1 - \sqrt{3}i}{1 - \sqrt{3}i}\right) \ge 0$ } and S <sub>3</sub> = {z \in C : Re (z) \ge 0}. Then (1) $\frac{125\pi}{6}$ (2) $\frac{125\pi}{24}$ (3) $\frac{125\pi}{4}$ (4) $\frac{125\pi}{12}$ Ans. (4) S <sub>1</sub> : x <sup>2</sup> + y <sup>2</sup> \le 25(1)
2.	f(0) = 0 at x = 1 LHL $\Rightarrow$ 2 + 1 - 0 + 0 = 3 f(1) = 3 - 1 + 1 = 3 RHL $\Rightarrow$ 2 + 1 - 1 + 1 = 3 The differential equation of the family of circles passing the origin and having center at the line y = x is: (1) (x <sup>2</sup> - y <sup>2</sup> + 2xy)dx = (x <sup>2</sup> - y <sup>2</sup> + 2xy)dy (2) (x <sup>2</sup> + y <sup>2</sup> + 2xy)dx = (x <sup>2</sup> + y <sup>2</sup> - 2xy)dy (3) (x <sup>2</sup> - y <sup>2</sup> + 2xy)dx = (x <sup>2</sup> - y <sup>2</sup> - 2xy)dy (4) (x <sup>2</sup> + y <sup>2</sup> - 2xy)dx = (x <sup>2</sup> + y <sup>2</sup> + 2xy)dy Ans. (3)		$S_{2} : \operatorname{Im} \operatorname{of} \frac{z + (1 - \sqrt{3} i)}{(1 - \sqrt{3} i)} \ge 0$ $\operatorname{Im} \operatorname{of} \left( \frac{x + iy}{1 - \sqrt{3} i} + 1 \right) \ge 0$ $\operatorname{Im} \operatorname{of} \left( \frac{(x + iy)(1 + \sqrt{3} i)}{4} \right) \ge 0$ $\Rightarrow \sqrt{3} x + y \ge 0 \qquad \dots \dots (2)$ $S_{3} : x \ge 0 \qquad \dots \dots (3)$ $\operatorname{Area} = \frac{5}{12} (\pi(5)^{2})$

Ans. (3)





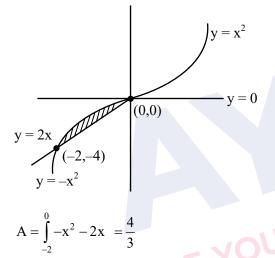


4. The area enclosed between the curves y = x|x| and y = x - |x| is :

(1) 
$$\frac{8}{3}$$
 (2)  $\frac{2}{3}$   
(3) 1 (4)  $\frac{4}{3}$ 

Ans. (4)

Sol.



5. 60 words can be made using all the letters of the word BHBJO, with or without meaning. If these words are written as in a dictionary, then the 50<sup>th</sup> word is :

(1) OBBHJ	(2) HBBJO
(3) OBBJH	(4) JBBOH
Ans. (3)	

Sol. B B H J O

B \_\_\_\_\_4! = 24  
H \_\_\_\_\_
$$\frac{4!}{2!} = 12$$
  
J \_\_\_\_\_ $\frac{4!}{2!} = 12$   
O B B H J  
O B B J H → 50<sup>th</sup> rank

Let  $\vec{a} = 2\hat{i} + 5\hat{j} - \hat{k}$ ,  $\vec{b} = 2\hat{i} - 2\hat{j} + 2\hat{k}$ 6. and  $\vec{c}$  be three vectors such that  $(\vec{c}+\hat{i})\times(\vec{a}+\vec{b}+\hat{i})=\vec{a}\times(\vec{c}+\hat{i})$ .  $\vec{a}.\vec{c}=-29$ , then  $\vec{c} \cdot \left(-2\hat{i} + \hat{j} + \hat{k}\right)$  is equal to : (1) 10(2)5(3) 15 (4) 12 Ans. (2) **Sol.** Let's assume  $\vec{v} = \vec{a} + \vec{b} + \hat{i}$  $=5\hat{i}+3\hat{j}+\hat{k}$ and  $\vec{c} + \hat{i} = \vec{p}$ So,  $\vec{p} \times \vec{v} = \vec{a} \times \vec{p}$  $\vec{\mathbf{p}} \times \vec{\mathbf{v}} + \vec{\mathbf{p}} \times \vec{\mathbf{a}} = \vec{\mathbf{0}}$  $\vec{p} \times (\vec{v} + \vec{a}) = \vec{0}$  $\Rightarrow \vec{p} = \lambda (\vec{v} + \vec{a})$  $\vec{c} + i = \lambda \left( 7\hat{i} + 8\hat{j} \right)$  $\overline{a}.\overline{c} + \overline{a}.\hat{i} = \lambda \overline{a}.(7\hat{i} + 8\hat{j})$  $-29+2=\lambda(14+40)$  $\lambda = -\frac{1}{2}$ 

$$\vec{c} \cdot \left(-2\hat{i} + \hat{j} + \hat{k}\right) + \hat{i} \cdot \left(-2\hat{i} + \hat{j} + \hat{k}\right) = \lambda \left(7\hat{i} + 8\hat{j}\right) \cdot \left(-2\hat{i} + \hat{j} + \hat{k}\right)$$
$$= -\frac{1}{2}(-14 + 8) + 2 = 5$$

Consider three vectors  $\vec{a}, \vec{b}, \vec{c}$ . Let  $|\vec{a}| = 2, |\vec{b}| = 3$ 7. and  $\vec{a} = \vec{b} \times \vec{c}$ . If  $\alpha \in \left[0, \frac{\pi}{3}\right]$  is the angle between the vectors  $\vec{b}$  and  $\vec{c}$ , then the minimum value of  $27\left|\vec{c}-\vec{a}\right|^2$  is equal to : (1) 110(2) 105(3) 124(4) 121

## Give yourself an extra edge





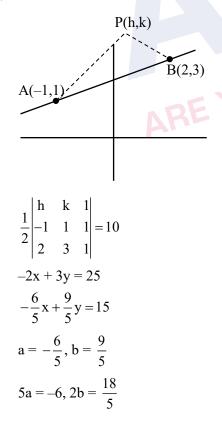
Sol. 
$$|\vec{c} - \vec{a}| = |\vec{c}|^2 + |\vec{a}|^2 - 2\bar{a}.\bar{c}$$
  
 $= |\vec{c}|^2 + 4 - 0$   
 $\because \vec{a} = \vec{b} \times \vec{c}$   
 $|\vec{a}| = |\vec{b} \times \vec{c}|$   
 $2 = 3|\vec{c}|\sin\alpha$   
 $|\vec{c}| = \frac{2}{3}\cos ec\alpha$   $\alpha \in \left[0, \frac{\pi}{3}\right]$   
 $|\vec{c}|_{\min} = \frac{2}{3} \times \frac{2}{\sqrt{3}}$   $\cos ec\alpha \in \left[\frac{2}{\sqrt{3}}, \infty\right)$   
 $\Rightarrow 27|\vec{c} - \vec{a}|_{\min}^2 = 27\left(\frac{16}{27} + 4\right) = 124$ 

Let A(-1, 1) and B(2, 3) be two points and P be a 8. variable point above the line AB such that the area of  $\triangle PAB$  is 10. If the locus of P is ax + by = 15, then 5a + 2b is :

(4) 6

(1) 
$$-\frac{12}{5}$$
 (2)  $-\frac{6}{5}$   
(3) 4 (4) 6  
Ans. (1)

Sol.



Let  $(\alpha, \beta, \gamma)$  be the point (8, 5, 7) in the line 9.  $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-2}{5}$ . Then  $\alpha + \beta + \gamma$  is equal to (1) 16(2) 18 (3) 14 (4) 20Ans. (3)

Sol.

$$A = (8, 5, 7)$$

$$2\hat{i} + 3\hat{j} + 5\hat{k}$$

$$M = (2\lambda + 1, 3\lambda - 1, 5\lambda + 2)$$

$$A'$$

$$\overline{AM} \cdot (2\hat{i} + 3\hat{j} + 5\hat{k}) = 0$$
  
(2\lambda - 7)(2) + (3\lambda - 6)(3) + (5\lambda - 5)(5) = 0  
38\lambda = 57

$$\lambda = \frac{1}{2}$$
$$M\left(4, \frac{7}{2}, \frac{19}{2}\right)$$

3

r = 6

A'(0,2,12) If the constant term in the expansion of 10.  $\left(\frac{\sqrt[5]{3}}{x} + \frac{2x}{\sqrt[3]{5}}\right)^{12}$ ,  $x \neq 0$ , is  $\alpha \times 2^8 \times \sqrt[5]{3}$ , then 25 $\alpha$  is

Sol. 
$$T_{r+1} = {}^{12}C_r \left(\frac{3^{1/5}}{x}\right)^{12-r} \left(\frac{2x}{5^{1/3}}\right)^r$$
  
 $T_{r+1} = \frac{{}^{12}C_r \left(3\right)^{\frac{12-r}{5}} \left(2\right)^r \left(x\right)^{2r-12}}{\left(5\right)^{r/3}}$ 

$$T_{7} = \frac{{}^{12}C_{6}(3)^{6/5}(2)^{6}}{5^{2}} = \left(\frac{9 \times 11 \times 7}{25}\right) 2^{8} \cdot 3^{1/5}$$
  
25\alpha = 693



11. Let 
$$f, g : \mathbb{R} \to \mathbb{R}$$
 be defined as  $: f(x) = |x - 1|$  and

~

$$g(x) = \begin{cases} e^x, & x \ge 0\\ x+1, & x \le 0 \end{cases}$$
. Then the function  $f(g(x))$  is

(2) one-one but not onto.

( v

- (3) both one-one and onto.
- (4) onto but not one-one.

Sol. f(g(x)) = |g(x) - 1|  $fog \begin{bmatrix} |e^{x} - 1| & x \ge 0 \\ |x + 1 - 1| & x \le 0 \end{bmatrix}$  $fog \begin{bmatrix} e^{x} - 1 & x \ge 0 \\ -x & x \le 0 \end{bmatrix}$ 

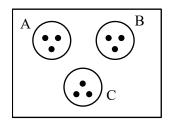
12. Let the circle  $C_1 : x^2 + y^2 - 2(x + y) + 1 = 0$  and  $C_2$ be a circle having centre at (-1, 0) and radius 2. If the line of the common chord of  $C_1$  and  $C_2$ intersects the y-axis at the point P, then the square of the distance of P from the centre of  $C_1$  is :

	(1) 2	(2) 1
	(3) 6	(4) 4
	Ans. (1)	
Sol.	$S_1: x^2 + y^2 - 2x - 2y - 2y$	+ 1 = 0
	$S_2: x^2 + y^2 + 2x - 3 =$	0
	Common chord = $S_1$ –	$-S_2 = 0$
	-4x - 2y + 4 = 0	
	$2x + y = 2 \Longrightarrow P(0, 2)$	
	$d_{(c,p)}^2 = (1-0)^2 + (2-1)^2$	$(-1)^2 = 2$

13. Let the set  $S = \{2, 4, 8, 16, \dots, 512\}$  be partitioned into 3 sets A, B, C with equal number of elements such that  $A \cup B \cup C = S$  and  $A \cap B = B \cap C = A \cap C = \phi$ . The maximum number of such possible partitions of S is equal to :

Sol.

Ans. (1)



$$\frac{9!}{(3!3!3!)3!} \times 3!$$

**14.** The values of m, n, for which the system of equations

$$x + y + z = 4,$$
  

$$2x + 5y + 5z = 17,$$
  

$$x + 2y + mz = n$$
  
has infinitely many solutions, satisfy the equation :  
(1) m<sup>2</sup> + n<sup>2</sup> - m - n = 46  
(2) m<sup>2</sup> + n<sup>2</sup> + m + n = 64  
(3) m<sup>2</sup> + n<sup>2</sup> + m n = 68  
(4) m<sup>2</sup> + n<sup>2</sup> - mn = 39  
**Ans. (4)**  
**Sol.**  $D = \begin{vmatrix} 1 & 1 & 1 \\ 2 & 5 & 5 \\ 1 & 2 & m \end{vmatrix} = 0 \Rightarrow m = 2$   
 $D_3 = \begin{vmatrix} 1 & 1 & 4 \\ 2 & 5 & 17 \\ 1 & 2 & n \end{vmatrix} = 0 \Rightarrow n = 7$ 

15. The coefficients a, b, c in the quadratic equation  $ax^2 + bx + c = 0$  are from the set {1, 2, 3, 4, 5, 6}. If the probability of this equation having one real root bigger than the other is p, then 216p equals : (1) 57 (2) 38

76

(3) 19	(4)
Ans. (2)	



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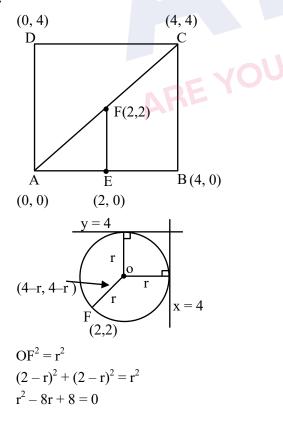
Sol. 
$$D > 0$$
  
 $b^2 > 4ac$   
 $b = 3 : (a, c) = (1, 1)(1, 2)(2, 1)$   
 $b = 4 : (a, c) = (1, 1)(1, 2)(2, 1)(1, 3)(3, 1)$   
 $b = 5 : (a, c) = (1, 1)(1, 2)(2, 1)(1, 3)(3, 1)(1, 4)(4, 1)$   
 $(1,5)(5, 1)(1, 6)(6, 1)(2, 3)(3, 2)(2, 2)$   
 $b = 6 : (a, c) = (1, 1)(1, 2)(2, 1)(1, 3)(3, 1)(1, 4)(4, 1)$   
 $(1,5)(5, 1)(1, 6)(6, 1)(2, 3)(3, 2)(2, 4)(4, 2)(2, 2)$   
fav. cases = 38  
Prob. :  $\frac{38}{6 \times 6 \times 6}$ 

16. Let ABCD and AEFG be squares of side 4 and 2 units, respectively. The point E is on the line segment AB and the point F is on the diagonal AC. Then the radius r of the circle passing through the point F and touching the line segments BC and CD satisfies :

> (2)  $r^2 - 8r + 8 = 0$ (1) r = 1 $(4) 2r^2 - 8r + 7 = 0$  $(3) 2r^2 - 4r + 1 = 0$ Ans. (2)

 $6 \times 6 \times 6$ 

Sol.



17. Let 
$$\beta(m, n) = \int_{0}^{1} x^{m-1} (1-x)^{n-1} dx$$
, m,  $n > 0$ . If  

$$\int_{0}^{1} (1-x^{10})^{20} dx = a \times \beta(b,c), \text{ then } 100(a + b + x)$$
equals  
(1) 1021 (2) 1120  
(3) 2012 (4) 2120  
Ans. (4)  
Sol.  $I = \int_{0}^{1} 1.(1-x^{10})^{20} dx$   
 $x^{10} = t$   
 $x = t^{1/10}$   
 $dx = \frac{1}{10}(t)^{-9/10} dt$   
 $I = \frac{1}{0}\int_{0}^{1} t^{-9/10} (1-t)^{20} dt$   
 $a = \frac{1}{10}$   $b = \frac{1}{10}$   $c = 21$   
18. Let  $\alpha\beta \neq 0$  and  $A = \begin{bmatrix} \beta & \alpha & 3 \\ \alpha & \alpha & \beta \\ -\beta & \alpha & 2\alpha \end{bmatrix}$ .  
If  $B = \begin{bmatrix} 3\alpha & -9 & 3\alpha \\ -\alpha & 7 & -2\alpha \\ -2\alpha & 5 & -2\beta \end{bmatrix}$  is the matrix of cofactors  
of the elements of A, then det(AB) is equal to :  
(1) 343 (2) 125  
(3) 64 (4) 216  
Ans. (4)  
Sol. Equating co-factor fo  $A_{21}$   
 $(2\alpha^{2} - 3\alpha) = \alpha$   
 $\alpha = 0, 2 (accept)$   
Now,  $2\alpha^{2} - \alpha\beta = 3\alpha$   
 $\alpha = 2$   $\beta = 1$   
 $|AB| = |A \cot (A)| = |A|^{3}$   
 $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 2 & 1 \\ -1 & 2 & 4 \end{bmatrix} = 6 - 2(9) + 3(6) = 6$ 





19. If 
$$y(\theta) = \frac{2\cos\theta + \cos 2\theta}{\cos 3\theta + 4\cos 2\theta + 5\cos\theta + 2}$$
  
then at  $\theta = \frac{\pi}{2}$ ,  $y'' + y' + y$  is equal to:  
(1)  $\frac{3}{2}$  (2) 1  
(3)  $\frac{1}{2}$  (4) 2

Ans. (4)

Sol. 
$$y = \frac{2\cos\theta + 2\cos^2\theta - 1}{4\cos^3\theta - 3\cos\theta + 8\cos^2\theta - 4 + 5\cos\theta + 2}$$
$$y = \frac{(2\cos^2\theta + 2\cos\theta - 1)}{(2\cos^2\theta + 2\cos\theta - 1)(2\cos\theta + 2)}$$
$$y = \frac{1}{2}\left(\frac{1}{1 + \cos\theta}\right)$$
$$\Rightarrow \theta = \frac{\pi}{2} \quad y = \frac{1}{2}$$
$$y' = \frac{1}{2}\left(\frac{-1}{(1 + \cos\theta)^2} \times (-\sin\theta)\right)$$
$$\Rightarrow \theta = \frac{\pi}{2} \quad y = \frac{1}{2}$$
$$y'' = \frac{1}{2}\left[\frac{\cos\theta(1 + \cos\theta)^2 - \sin\theta(2)(1 + \cos\theta)(-\sin\theta)}{(1 + \cos\theta)^4}\right]$$
$$\Rightarrow \theta = \frac{\pi}{2} \qquad y = 1$$
20 For x > 0 the least value of K for which  $4^{1+x} + 4^{1-x}$ 

20. For  $x \ge 0$ , the least value of K, for which  $4^{1+x} + 4^{1-x}$ ,  $\frac{K}{2}$ ,  $16^x + 16^{-x}$  are three consecutive terms of an A.P. is equal to : (1) 10 (2) 4 (3) 8 (4) 16

 $+\frac{1}{4^{2x}}$ 

Ans. (1)

Sol. 
$$k = 4\left(4^x + \frac{1}{4^x}\right) + \left(4^{2x} + \frac{1}{2^x}\right)$$
  
 $\geq 2 \qquad \geq 2$ 

$$k \ge 10$$

## **SECTION-B**

**21.** Let the mean and the standard deviation of the probability distribution

Х	α	1	0	-3
P(X)	$\frac{1}{3}$	K	$\frac{1}{6}$	$\frac{1}{4}$

be  $\mu$  and  $\sigma$ , respectively. If  $\sigma - \mu = 2$ , then  $\sigma + \mu$  is equal to \_\_\_\_\_.

Ans. (5)  
Sol. 
$$\frac{1}{3} + k + \frac{1}{6} + \frac{1}{4} = 1 \qquad \Rightarrow k = \frac{1}{4}$$
  
 $\mu = \frac{\alpha}{3} + \frac{1}{4} - \frac{3}{4}$   
 $\boxed{\mu = \frac{\alpha}{3} - \frac{1}{2}}$   
 $\sigma = \sqrt{\left(\alpha^2 \frac{1}{3} + \frac{1}{4} + 9\frac{1}{4}\right) - \left(\frac{\alpha}{3} - \frac{1}{2}\right)^2}$   
 $\sigma = \sqrt{\frac{2\alpha^2}{9} + \frac{\alpha}{3} + \frac{9}{4}}$   
 $\sigma = \mu + 2$   
 $\sigma^2 = (\mu + 2)^2 \Rightarrow \frac{2\alpha^2}{9} + \frac{\alpha}{3} + \frac{9}{4} = \frac{\alpha^2}{9} + \frac{9}{4} + \alpha$   
 $\frac{\alpha^2}{9} - \frac{2\alpha}{3} = 0$   
 $\alpha = 0, \text{ (reject) or } \alpha = 6$   
 $(\because x = 0 \text{ is already given)}$   
 $\Rightarrow \sigma + \mu = 2\mu + 2$   
 $= 5$ 

22. Let 
$$y = y(x)$$
 be the solution of the differential  
equation  $\frac{dy}{dx} + \frac{2x}{(1+x^2)^2}y = xe^{\frac{1}{(1+x^2)}}$ ;  $y(0) = 0$ .  
Then the area enclosed by the curve  
 $f(x) = y(x)e^{-\frac{1}{(1+x^2)}}$  and the line  $y - x = 4$  is \_\_\_\_.  
Ans. (18)



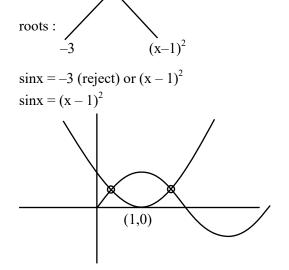
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Sol. IF = 
$$e^{\int \frac{2x}{(1+x^2)^2} dx} = e^{\frac{-1}{1+x^2}}$$
  
 $y \cdot e^{\frac{-1}{1+x^2}} = \int x \cdot e^{\frac{1}{1+x^2}} \cdot e^{\frac{-1}{1+x^2} dx}$   
 $y \cdot e^{\frac{-1}{1+x^2}} = \frac{x^2}{2} + c$   
 $(0, 0) \Rightarrow \boxed{C=0}$   
 $y(x) = \frac{x^2}{2} e^{\frac{1}{1+x^2}}$   
 $f(x) = \frac{x^2}{2}$   
 $y = x^2/2$   
 $(-2, 2)$   
 $(4, 8)$ 

$$A = \int_{-2}^{4} (x+4) - \frac{x^2}{2} dx = 18$$

23. The number of solutions of  $\sin^2 x + (2 + 2x - x^2)\sin x - 3(x - 1)^2 = 0$ , where  $-\pi \le x \le \pi$ , is Ans. (2)

Sol. 
$$\sin^2 x - (x^2 - 2x - 2)\sin x - 3(x - 1)^2 = 0$$
  
 $\sin^2 x - (x - 1)^2)\sin x - 3(x - 1)^2 = 0$ 



24. Let the point  $(-1, \alpha, \beta)$  lie on the line of the shortest distance between the lines  $\frac{x+2}{-3} = \frac{y-2}{4} = \frac{z-5}{2}$  and  $\frac{x+2}{-1} = \frac{y+6}{2} = \frac{z-1}{0}$ . Then  $(\alpha - \beta)^2$  is equal to \_\_\_\_\_. Ans. (25)

$$\begin{array}{c} Q & (-2,-6,1) & \overbrace{(-1,+2)}^{(-1,+2)} \\ \hline & (-3\hat{i}+4\hat{j}+2\hat{k}) \end{array}$$

$$P(-3\lambda-2,4\lambda+2,2\lambda+5) \\ Q(-\mu-2,2\mu-6,1) \\ DRS \text{ of } PQ = (3\lambda-\mu,2\mu-4\lambda-8,-2\lambda-4) \\ DRS \text{ of } PQ = (3\lambda-\mu,2\mu-4\lambda-8,-2\lambda-4) \\ DRS \text{ of } PQ = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -1 & 2 & 0 \\ -3 & 4 & 2 \end{vmatrix}$$

$$= (4\hat{i}+2\hat{j}+2\hat{k}) \\ OR \\ (2,1,1) \\ \frac{3\lambda-\mu}{2} = \frac{2\mu-4\lambda-8}{1} = \frac{-2\lambda-4}{1} \\ \Rightarrow \mu = \lambda+2 \& 7\lambda = \mu-8 \\ \hline \lambda = -1 & \boxed{\mu = 1} \\ Q: (-3,-4,1) \\ L_{PQ} = \frac{x+3}{2} = \frac{y+4}{1} = \frac{z-1}{1} \\ (-1,\alpha,\beta) \Rightarrow 1 = \frac{\alpha+4}{1} = \frac{\beta-1}{1} \\ \Rightarrow \alpha = -3, \beta = 2 \\ (\alpha-\beta)^2 = 25 \end{array}$$



25. If  

$$1 + \frac{\sqrt{3} - \sqrt{2}}{2\sqrt{3}} + \frac{5 - 2\sqrt{6}}{18} + \frac{9\sqrt{3} - 11\sqrt{2}}{36\sqrt{3}} + \frac{49 - 20\sqrt{6}}{180} + \dots$$
upto  $\infty = 2\left(\sqrt{\frac{b}{a}} + 1\right)\log_{e}\left(\frac{a}{b}\right)$ , where a and b are

integers with gcd(a, b) = 1, then 11a + 18b is equal to \_\_\_\_\_.

Sol. 
$$S = 1 + \frac{x}{2\sqrt{3}} + \frac{x^2}{18} + \frac{x^3}{36\sqrt{3}} + \frac{x^4}{180} + \dots \infty$$
  
Put  $\frac{x}{\sqrt{3}} = t$ , where  $x = \sqrt{3} - \sqrt{2}$   
$$S = 1 + \frac{t}{2} + \frac{t^2}{6} + \frac{t^3}{12} + \frac{t^4}{20} + \dots$$
  
$$S = 1 + t\left(1 - \frac{1}{2}\right) + t^2\left(\frac{1}{2} - \frac{1}{3}\right) + t^3\left(\frac{1}{3} - \frac{1}{4}\right) + t^4\left(\frac{1}{4} - \frac{1}{5}\right)$$
  
$$S = \left(1 + t + \frac{t^2}{2} + \frac{t^3}{3} + \frac{t^3}{4} + \dots\right) - \left(\frac{t}{2} + \frac{t^2}{3} + \frac{t^3}{4} + \frac{t^4}{5} + \dots\right)$$
  
$$S = \left(t + \frac{t^2}{2} + \dots\right) - \frac{1}{t}\left(t + \frac{t^2}{2} + \frac{t^3}{3} + \dots\right) + 2$$
  
$$S = 2 + \left(1 - \frac{1}{t}\right)\left(-\log(1 - t)\right) = \left(\frac{1}{t} - 1\right)\log(1 - t) + 2$$
  
$$S = 2 + \left(\frac{\sqrt{3}}{\sqrt{3} - \sqrt{2}} - 1\right)\log\left(1 - \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3}}\right)$$
  
$$S = 2 + \left(\frac{\sqrt{2}}{\sqrt{3} - \sqrt{2}}\right)\log \frac{\sqrt{2}}{\sqrt{3}}$$
  
$$S = 2 + \left(\frac{\sqrt{6} + 2}{2}\right)\log \frac{2}{3} = 2 + \left(\sqrt{\frac{3}{2}} + 1\right)\log\frac{2}{3}$$
  
$$a = 2, b = 3$$
  
$$11a + 18b = 11 \times 2 + 18 \times 3 = 76$$

**26.** Let a > 0 be a root of the equation  $2x^2 + x - 2 = 0$ .

If 
$$\lim_{x \to \frac{1}{a}} \frac{16(1 - \cos(2 + x - 2x^2))}{(1 - ax^2)} = \alpha + \beta \sqrt{17}$$
, where

$$\alpha, \beta \in \mathbb{Z}$$
 then  $\alpha + \beta$  is equal to \_\_\_\_\_

Ans. (170)

Sol. 
$$2x^{2} + x - 2 = 0$$
  
 $2x^{2} - x - 2 = 0$   
 $\frac{1}{a}$   
 $2x^{2} - x - 2 = 0$   
 $\frac{1}{a}$   
 $\frac{1}{b}$   
 $\lim_{x \to \frac{1}{a}} 16 \cdot \frac{\left(1 - \cos 2\left(x - \frac{1}{a}\right)\left(x - \frac{1}{b}\right)\right)}{4\left(x - \frac{1}{b}\right)^{2}} \times \frac{4\left(x - \frac{1}{b}\right)^{2}}{a^{2}\left(x - \frac{1}{a}\right)^{2}}$   
 $= 16 \times \frac{2}{a^{2}}\left(\frac{1}{a} - \frac{1}{b}\right)^{2}$   
 $= 16 \times \frac{2}{a^{2}}\left(\frac{1}{a} - \frac{1}{b}\right)^{2}$   
 $= \frac{32}{a^{2}}\left(\frac{17}{4}\right) = \frac{17.8}{a^{2}} = \frac{17 \times 8 \times 16}{(-1 + \sqrt{117})^{2}}$   
 $= \frac{136.16}{18.2\sqrt{7}} \times \frac{18 + 2\sqrt{7}}{18 + 2\sqrt{7}}$   
 $= \frac{136}{256}(18 + 2\sqrt{7}) \cdot 16$   
 $= 153 + 17\sqrt{17} = \alpha + \beta\sqrt{17}$ 

$$\alpha + \beta = 153 + 17 = 170$$

27. If  $f(t) = \int_{0}^{\pi} \frac{2xdx}{1 - \cos^2 t \sin^2 x}$ ,  $0 < t < \pi$ , then the value

of 
$$\int_{0}^{\frac{\pi}{2}} \frac{\pi^2 dt}{f(t)}$$
 equals \_\_\_\_\_.

Ans. (1)

**Sol.** 
$$f(t) = \int_{0}^{\pi} \frac{2x}{1 - \cos^2 t \sin^2 x} dx$$
 .....(1)





$$= 2\int_{0}^{\pi} \frac{(\pi - x)dx}{1 - \cos^{2} t \sin^{2} x} \qquad \dots(2)$$

$$2f(t) = 2\int_{0}^{\pi} \frac{\pi}{1 - \cos^{2} t \sin^{2} x} dx$$

$$f(t) = \int_{0}^{\pi} \frac{\pi}{1 - \cos^{2} t \sin^{2} x} dx$$
divide & by cos<sup>2</sup>x
$$f(t) = \pi\int_{0}^{\pi} \frac{\sec^{2} x dx}{\sec^{2} x - \cos^{2} t \tan^{2} x}$$

$$f(t) = 2\pi\int_{0}^{\pi/2} \frac{\sec^{2} x dx}{\sec^{2} x - \cos^{2} t \tan^{2} x}$$

$$\tan x = z$$

$$\sec^{2} x dx = dz$$

$$f(t) = 2\pi\int_{0}^{\infty} \frac{dz}{1 + \sin^{2} t \cdot z^{2}}$$

$$= \frac{\pi^{2}}{\sin t}$$
Then 
$$\int_{0}^{\pi/2} \frac{\pi^{2}}{f(t)} dt$$

$$= 1$$
28. Let the maximum and minimum values of  $(\sqrt{8x - x^{2} - 12} - 4)^{2} + (x - 7)^{2}, x \in R \text{ be M and m}$ 
respectively. Then M<sup>2</sup> - m<sup>2</sup> is equal to \_\_\_\_\_.  
Ans. (1600)  
Sol.  $(x - 7)^{2} + (y - 4)^{2}$ 

$$y = \sqrt{8x - x^{2} - 12}$$

P(7,4)  

$$m = 9$$

$$M = 41$$

$$M^{2} - m^{2} = 41^{2} - 9^{2} = 1600$$
29. Let a line perpendicular to the line  $2x - y = 10$   
touch the parabola  $y^{2} = 4(x - 9)$  at the point P. The  
distance of the point P from the centre of the circle  

$$x^{2} + y^{2} - 14x - 8y + 56 = 0 \text{ is } \underline{\qquad}.$$
Ans. (10)  
Sol.  $y^{2} = 4(x - 9)$   
slope of tangent  $= \frac{-1}{2}$   
Point of contact  $P\left(9 + \frac{1}{\left(-\frac{1}{2}\right)^{2}}, \frac{2 \times 1}{-\frac{1}{2}}\right)$   
P(13, -4)  
center of circle C(7, 4)  
distance  $CP = \sqrt{(13 - 7)^{2} + (-4 - 4)^{2}}$   
 $= 10$   
30. The number of real solutions of the equation  
 $x |x + 5| + 2|x + 7| - 2 = 0 \text{ is } \underline{\qquad}.$   
Ans. (3)  
30. The number of real solutions of the equation  
 $x |x + 5| + 2|x + 7| - 2 = 0 \text{ is } \underline{\qquad}.$   
Allen Ans. (3)  
Sol. Case I :  $x \ge -5$   
 $x^{2} + 5x + 2x + 12 = 0$   
 $x^{2} + 7x + 12 = 0$   
 $x = -3, -4$   
Case II :  $-7 < x < -5$   
 $-x^{2} - 5x + 2x + 14 - 2 = 0$ 

 $y^2 = -(x-4)^2 + 16 - 12$ 

 $(x-4)^2 + y^2 = 4$ 

28.

values of





$$-x^{2} - 3x + 12 = 0$$

$$x = \frac{-3 \pm \sqrt{9 + 48}}{2}$$

$$= \frac{-3 \pm \sqrt{57}}{2}$$

$$x = \frac{-3 - \sqrt{57}}{2}, \frac{-3 + \sqrt{57}}{2} \text{ (rejected)}$$

Case III :  $x \le -7$  $-x^2 - 5x - 2x - 14 - 2 = 0$  $x^2 + 7x + 16 = 0$ D = 49 - 64 < 0No solutions

No. of solutions = 3





# PHYSICS

# **SECTION-A**

31. Given below are two statements :

> Statement I : When the white light passed through a prism, the red light bends lesser than yellow and violet.

> **Statement II :** The refractive indices are different for different wavelengths in dispersive medium. In the light of the above statements, choose the correct answer from the options given below :

(1) Both Statement I and Statement II are true.

- (2) Statement I is true but Statement II is false.
- (3) Both Statement I and Statement II are false.
- (4) Statement I is false but Statement II is true.

## Ans. (1)

**Sol.** As  $\lambda_{red} > \lambda_{vellow} > \lambda_{violet}$ 

Light ray with longer wavelength bends less.

32. Which of the following statement is not true about stopping potential  $(V_0)$ ?

(1) It depends on the nature of emitter material.

(2) It depends upon frequency of the incident light.

(3) It increases with increase in intensity of the incident light.

(4) It is 1/e times the maximum kinetic energy of electrons emitted.

# Ans. (3)

**Sol.**  $KE_{max} = hv - \phi_0 = eV$ 

The angular momentum of an electron in a 33. hydrogen atom is proportional to : (Where r is the radius of orbit of electron)

(1) 
$$\sqrt{r}$$
 (2)  $\frac{1}{r}$   
(3) r (4)  $\frac{1}{\sqrt{r}}$ 

Ans. (1)

# TEST PAPER WITH SOLUTION

Sol. 
$$F_{C} = \frac{mv}{r}$$
$$\frac{Kq_{1}q_{2}}{r^{2}} = \frac{mv^{2}}{r}$$
$$mv^{2}r^{2} = Kq_{1}q_{2}r$$
$$\frac{L^{2}}{m} = Kq_{1}q_{2}r$$
$$L \propto \sqrt{r}$$

2

A galvanometer of resistance 100  $\Omega$  when 34. connected in series with 400  $\Omega$  measures a voltage of upto 10 V. The value of resistance required to convert the galvanometer into ammeter to read upto 10 A is  $x \times 10^{-2} \Omega$ . The value of x is :

Ans. (3)

Sol. 
$$i_g = \frac{10}{400+100} = 20 \times 10^{-3} \text{ A}$$
  
For ammeter  
Let shunt resistance = S  
 $i_g R = (i - i_g) S$   
 $20 \times 10^{-3} \times 100 = 10 \text{ S}$   
 $S = 20 \times 10^{-2} \Omega$   
35. The vehicles carrying inflamm

The vehicles carrying inflammable fluids usually 35. have metallic chains touching the ground :

> (1) To conduct excess charge due to air friction to ground and prevent sparking.

(2) To alert other vehicles.

(3) To protect tyres from catching dirt from ground.

(4) It is a custom.

Ans. (1)

Static charge is developed due to air friction. This Sol. can result in combustion. So, metallic chains is used to discharge excess charge.



If n is the number density and d is the diameter of 36. the molecule, then the average distance covered by a molecule between two successive collisions (i.e. mean free path) is represented by :

(1) 
$$\frac{1}{\sqrt{2n\pi d^2}}$$
 (2)  $\sqrt{2}n\pi d^2$   
(3)  $\frac{1}{\sqrt{2}n\pi d^2}$  (4)  $\frac{1}{\sqrt{2}n^2\pi^2 d^2}$ 

Ans. (3)

**Sol.** n = number of molecule per unit volume d = diameter of the molecule

$$\lambda = \frac{1}{\sqrt{2}\pi d^2 n}$$
 (By Theory)

A particle moves in x-y plane under the influence 37. of a force  $\vec{F}$  such that its linear momentum is  $\vec{P}(t) = \hat{i}\cos(kt) - \hat{j}\sin(kt)$ . If k is constant, the angle between  $\vec{F}$  and  $\vec{P}$  will be :

(1) 
$$\frac{\pi}{2}$$
 (2)  $\frac{\pi}{6}$   
(3)  $\frac{\pi}{4}$  (4)  $\frac{\pi}{3}$ 

Ans. (1)

Sol. 
$$\vec{P} = \cos(kt)\hat{i} - \sin(kt)\hat{j}$$
;  $|\vec{P}| = 1$   
 $\therefore \vec{P} = m\vec{v}$ 

$$\therefore \hat{P} = \hat{v}$$

$$\Rightarrow \hat{v} = \cos(kt)\hat{i} - \sin(kt)\hat{j}$$

$$\hat{a} = \frac{-k\sin(kt)\hat{i} - k\cos(kt)\hat{j}}{k}$$

$$\Rightarrow \hat{a} = -\sin kt\hat{i} - \cos kt\hat{j}$$

$$\because \hat{F} = \hat{a} = -\sin kt\hat{i} - \cos kt\hat{j}$$

$$\cos \theta = \frac{\hat{F}\cdot\hat{P}}{|\hat{F}||\hat{P}|} = -\frac{\sin kt\cos t + \sin kt\cos t}{1 \times 1} = 0$$

$$\Rightarrow \theta = \frac{\pi}{2}$$

- The electrostatic force  $(\vec{F}_1)$  and magnetic force 38.  $(\vec{F}_2)$  acting on a charge q moving with velocity v can be written : (1)  $\vec{F}_1 = q\vec{V}.\vec{E}, \vec{F}_2 = q(\vec{B}.\vec{V})$ (2)  $\vec{F}_1 = q\vec{B}, \vec{F}_2 = q(\vec{B} \times \vec{V})$ (3)  $\vec{F}_1 = q\vec{E}$ ,  $\vec{F}_2 = q(\vec{V} \times \vec{B})$ (4)  $\vec{F}_1 = q\vec{E}$ ,  $\vec{F}_2 = q(\vec{B} \times \vec{V})$
- Ans. (3)
- **Sol.**  $\vec{F}_1 = q\vec{E}$ (Theory)  $\vec{F}_2 = q(\vec{V} \times \vec{B})$
- 39. A man carrying a monkey on his shoulder does cycling smoothly on a circular track of radius 9m and completes 120 revolutions in 3 minutes. The magnitude of centripetal acceleration of monkey is  $(in m/s^2)$ :

(1) zero  
(2) 
$$16 \pi^2 \text{ ms}^{-2}$$
  
(3)  $4\pi^2 \text{ ms}^{-2}$   
(4)  $57600 \pi^2 \text{ ms}^{-2}$ 

$$t^2 \text{ ms}^{-2}$$
 (4) 57600  $\pi^2 \text{ ms}^{-2}$ 

Ans. (2)

Sol. Given : 
$$R = 9m$$
,

$$\omega = \frac{120 \text{ revolution in 3 min}}{3 \text{ min.}} = \frac{120 \times 2\pi \text{ rad}}{3 \times 60 \text{ sec}} = \frac{4\pi}{3} \text{ rad / s}$$

$$a_{\text{centripetal}} = \omega^2 R = \left(\frac{4\pi}{3}\right)^2 \times 9 = 16\pi^2 \text{ m/s}^2$$

**40.** A series LCR circuit is subjected to an AC signal of 200 V, 50 Hz. If the voltage across the inductor (L = 10 mH) is 31.4 V, then the current in this circuit is : (1) 68 A (2) 63 A

Ans. (3)

**Sol.** Voltage across inductor  $V_L = IX_L$ 

31.4 = I[Lω]  
31.4 = I[L(2
$$\pi$$
f)]  
31.4 = I[10 × 10<sup>-3</sup>(2 × 3.14) × 50  
⇒ I = 10 A



41. What is the dimensional formula of  $ab^{-1}$  in the equation  $\left(P + \frac{a}{V^2}\right)(V - b) = RT$ , where letters

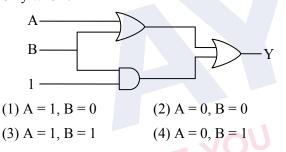
have their usual meaning.

(1) 
$$[M^0L^3T^{-2}]$$
 (2)  $[ML^2T^{-2}]$   
(3)  $[M^{-1}L^5T^3]$  (4)  $[M^6L^7T^4]$ 

Ans. (2)

Sol. :: 
$$[V] = [b]$$
  
:: Dimension of  $b = [L^3]$   
&  $[P] = \left[\frac{a}{V^2}\right]$   
[ $a$ ] =  $[PV^2] = [ML^{-1}T^{-2}][L^6]$   
Dimension of  $a = [ML^5T^{-2}]$   
::  $ab^{-1} = \frac{[ML^5T^{-2}]}{[L^3]} = [ML^2T^{-2}]$ 

**42.** The output (Y) of logic circuit given below is 0 only when :



Ans. (2) Sol.

> OR gate  $0 A \xrightarrow{0} 0$   $0 B \xrightarrow{0} 0$   $1 \xrightarrow{0} 0$   $1 \xrightarrow{0} 0$  0 R gate0 R gate

**43.** A body is moving unidirectionally under the influence of a constant power source. Its displacement in time t is proportional to :

(1) 
$$t^2$$
 (2)  $t^{2/3}$ 

(3)  $t^{3/2}$  (4) t

Ans. (3)

Sol. 
$$P = costant \Rightarrow FV = constant$$
  
 $\Rightarrow m \frac{dV}{dt} V = constant$   
 $\int_{0}^{V} V dV = (C) \int_{0}^{t} dt$   
 $\left(\frac{V^{2}}{2}\right) = Ct$   
 $V \propto t^{1/2}$   
 $\frac{ds}{dt} \propto t^{1/2}$   
 $\int_{0}^{S} ds = K \int_{0}^{t} t^{1/2} dt$   
 $S = K \times \frac{2}{3} t^{3/2}$   
 $S \propto t^{3/2}$ 

 $\therefore$  displacement is proportional to (t)<sup>3/2</sup>

44. Match List-I with List-II :-

	List-I		List-II
	EM-Wave	5	Wavelength
	EADY	•	Range
(A)	Infra-red	(I)	$< 10^{-3} \text{ nm}$
(B)	Ultraviolet	(II)	400 nm to 1 nm
(C)	X-rays	(III)	1 mm to 700 nm
(D)	Gamma rays	(IV)	$1 \text{ nm to } 10^{-3} \text{ nm}$

Choose the correct answer from the options given below :

(1) (A)-(II), (B)-(I), (C)-(IV), (D)-(III) (2) (A)-(III), (B)-(II), (C)-(IV), (D)-(I)

- (3) (A)-(IV), (B)-(III), (C)-(II), (D)-(I)
- (4) (A)-(I), (B)-(III), (C)-(II), (D)-(IV)

# Ans. (2)

Sol. Infrared is the least energetic thus having biggest wavelength ( $\lambda$ ) & gamma rays are most energetic thus having smallest wavelength ( $\lambda$ ).



**45.** During an adiabatic process, if the pressure of a gas is found to be proportional to the cube of its absolute temperature, then the ratio of  $\frac{C_P}{C_{VP}}$  for the

gas is :

(1)  $\frac{5}{3}$  (2)  $\frac{9}{7}$ (3)  $\frac{3}{2}$  (4)  $\frac{7}{5}$ 

Ans. (3)

Sol.  $P \propto T^3$   $PT^{-3} = constant$   $\therefore \frac{PV}{T} = nR = constant$  from ideal gas equation (P)  $(PV)^{-3} = constant$   $P^{-2} V^{-3} = constant$  ...(1)  $\therefore$  Process equation for adiabatic process is  $PV^y = constant$  ...(2) Comparing equation (1) and (2)  $\frac{C_P}{2} = v - \frac{3}{2}$ 

$$C_V = 2$$

46. Match List-I with List-II :

	List-I			List-II
(A)	A force	that	(I)	Bulk modulus
	restores	an		
	elastic body	of		
	unit area to	its		VOV
	original state	N	RE	
(B)	Two equal	and	(II)	Young's modulus
	opposite fo	rces		
	parallel	to		
	opposite face	s		
(C)	Forces		(III)	Stress
	perpendicular	ſ		
	everywhere	to		
	the surface	per		
	unit area s	ame		
	everywhere			
(D)	Two equal	and	(IV)	Shear modulus
	opposite fo	rces		
	perpendicular	to		
	opposite face	s		

Choose the correct answer from the options given below :

below : (1) (A)-(II), (B)-(IV), (C)-(I), (D)-(III) (2) (A)-(IV), (B)-(II), (C)-(III), (D)-(I) (3) (A)-(III), (B)-(IV), (C)-(I), (D)-(IV) (4) (A)-(III), (B)-(I), (C)-(II), (D)-(IV) Ans. (3) Sol. (A) stress =  $\frac{F_{restoring}}{A}$ If A = 1 Stress = F<sub>restoring</sub> (A)-(III) (B) (B) (C) (C) Volumetric stress

> (C)-(I) (D)  $\leftarrow$   $\rightarrow$   $\Rightarrow$  Longitudinal stress

(D)-(II)

47. A vernier callipers has 20 divisions on the vernier scale, which coincides with 19<sup>th</sup> division on the main scale. The least count of the instrument is 0.1 mm. One main scale division is equal to \_\_\_\_mm.

$$\begin{array}{cccc}
(1) 1 & (2) 0.5 \\
(3) 2 & (4) 5
\end{array}$$

Ans. (3)

Sol. 20 VSD = 19 MSD  

$$1VSD = \frac{19}{20}$$
 MSD  
L.C. = 1 MSD - 1 VSD  
 $0.1 \text{ mm} = 1\text{MSD} - \frac{19}{20}$  MSD  
 $0.1 = \frac{1}{20}$  MSD  
 $1 \text{ MSD} = 2\text{mm}$ 



- **48.** A heavy box of mass 50 kg is moving on a horizontal surface. If co-efficient of kinetic friction between the box and horizontal surface is 0.3 then force of kinetic friction is :
  - (1) 14.7 N
  - (2) 147 N
  - (3) 1.47 N
  - (4) 1470 N

Ans. (2)

#### Sol.

$$\mu_k = 0.3 \qquad 50 \text{kg} \longrightarrow \text{V}$$

 $F_k = \mu_k N = 0.3 \times 50 \times 9.8 = 147 N$ 

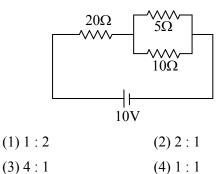
**49.** A satellite revolving around a planet in stationary orbit has time period 6 hours. The mass of planet is one-fourth the mass of earth. The radius orbit of planet is : (Given = Radius of geo-stationary orbit for earth is  $4.2 \times 10^4$  km)

ARE YOU

- (1)  $1.4 \times 10^4$  km
- (2)  $8.4 \times 10^4$  km
- (3)  $1.68 \times 10^5$  km
- (4)  $1.05 \times 10^4$  km

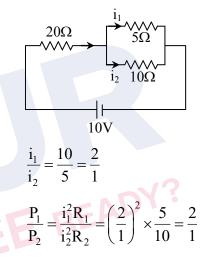
Sol. 
$$T = \frac{2\pi r^{3/2}}{\sqrt{GM}}$$
  
 $\frac{T_1}{T_2} = \left(\frac{r_1}{r_2}\right)^{3/2} \left(\frac{M_2}{M_1}\right)^{1/2}$   
 $\frac{6}{24} = \frac{(r_1)^{3/2}}{(4.2 \times 10^4)^{3/2}} \left(\frac{M}{M/4}\right)^{1/2}$   
 $r_1 = 1.05 \times 10^4 \text{ km}$ 

**50.** The ratio of heat dissipated per second through the resistance 5  $\Omega$  and 10  $\Omega$  in the circuit given below is :



Ans. (2)

Sol.



#### **SECTION-B**

51. A solenoid of length 0.5 m has a radius of 1 cm and is made up of 'm' number of turns. It carries a current of 5A. If the magnitude of the magnetic field inside the solenoid is  $6.28 \times 10^{-3}$  T, then the value of m is :

Ans. (500)

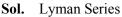
**Sol.** 
$$\mu_0 ni = B$$
  $n =$  number of turns per unit length

$$\mu_0 \left(\frac{m}{\ell}\right) \mathbf{i} = \mathbf{B}$$
$$m = \frac{\mathbf{B}.\ell}{\mu_0 \mathbf{i}} = \frac{6.28 \times 10^{-3} \times 0.5}{12.56 \times 10^{-7} \times 5}$$
$$m = 500$$



52. The shortest wavelength of the spectral lines in the Lyman series of hydrogen spectrum is 915 Å. The longest wavelength of spectral lines in the Balmer series will be \_\_\_\_\_\_ Å.

#### Ans. (6588)



$$h = L$$
Shortest,  $\frac{hc}{\lambda} = -13.6 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$ 

$$\lambda \downarrow E \uparrow ; \frac{hc}{\lambda_0} = -13.6(1)$$
Balmer Series :
$$n = 3$$

$$n = 2$$

$$\frac{hc}{\lambda_1} = -13.6 \left( \frac{1}{2^2} - \frac{1}{3^2} \right)$$

$$\frac{hc}{\lambda_1} = -13.6 \left( \frac{1}{4} - \frac{1}{9} \right)$$

$$\frac{hc}{\lambda_1} = -13.6 \left( \frac{5}{36} \right)$$

$$\Rightarrow \frac{-13.6\lambda_0}{\lambda_1} = -13.6 \times \frac{5}{36}$$

$$\lambda_1 = \frac{\lambda_0 \times 36}{5} = \frac{915 \times 36}{5} = 6588$$

53. In a single slit experiment, a parallel beam of green light of wavelength 550 nm passes through a slit of width 0.20 mm. The transmitted light is collected on a screen 100 cm away. The distance of first order minima from the central maximum will be  $x \times 10^{-5}$  m. The value of x is :

Ans. (275) Sol.

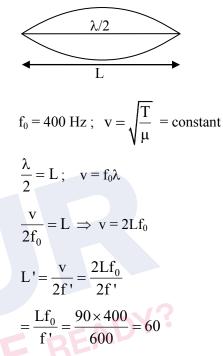
y  

$$\lambda = 550 \text{ nm} \\
d = 0.2 \text{ mm} \\
y = \frac{\lambda D}{d} = \frac{550 \times 10^{-9} \times 100 \times 10^{-2}}{0.2 \times 10^{-3}} = 275$$

54. A sonometer wire of resonating length 90 cm has a fundamental frequency of 400 Hz when kept under some tension. The resonating length of the wire with fundamental frequency of 600 Hz under same tension \_\_\_\_\_ cm.

Ans. (60)

Sol.



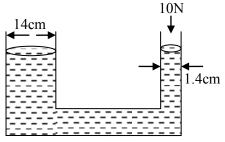
**55.** A hollow sphere is rolling on a plane surface about its axis of symmetry. The ratio of rotational kinetic

energy to its total kinetic energy is  $\frac{x}{5}$ . The value of x is \_\_\_\_\_.

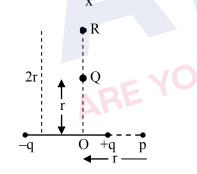
Ans. (2)

Sol. 
$$\frac{\frac{1}{2}I\omega^{2}}{\frac{1}{2}I\omega^{2} + \frac{1}{2}mv^{2}} = \frac{\left(\frac{1}{2}\right)\left(\frac{2}{3}mR^{2}\right)\omega^{2}}{\left(\frac{1}{2}\right)\left(\frac{2}{3}mR^{2}\right)\omega^{2} + \frac{1}{2}m(R\omega)^{2}}$$
$$= \frac{\frac{2}{3}}{\frac{2}{3}+1} = \frac{2}{5}$$
$$x = 2$$

**56.** A hydraulic press containing water has two arms with diameters as mentioned in the figure. A force of 10 N is applied on the surface of water in the thinner arm. The force required to be applied on the surface of water in the thicker arm to maintain equilibrium of water is \_\_\_\_\_ N.



- Sol.  $\frac{F_1}{A_1} = \frac{F_2}{A_2}$  $\frac{F_1}{\pi (7)^2} = \frac{10}{\pi \times (0.7)^2}$  $F_1 = 1000 \text{ N}$
- 57. The electric field at point p due to an electric dipole is E. The electric field at point R on equitorial line will be  $\frac{E}{x}$ . The value of x :



Ans. (16)

Sol.  $E_P = \frac{2KP}{r^3} = E$  $E_R = \frac{KP}{r^3} = \frac{E}{16}$ 

$$E_{R} = \frac{KP}{(2r)^{3}} = \frac{E}{16}$$
$$x = 16$$

58. The maximum height reached by a projectile is 64 m. If the initial velocity is halved, the new maximum height of the projectile is \_\_\_\_\_ m. Ans. (16)

Sol. 
$$H_{max} = \frac{u^2 \sin^2 \theta}{2g}$$
$$\frac{H_{1max}}{H_{2max}} = \frac{u_1^2}{u_2^2}$$
$$\frac{64}{H_{2max}} = \frac{u^2}{(u/2)^2}$$
$$H_{2max} = 16 \text{ m}$$

**59.** A wire of resistance  $20 \Omega$  is divided into 10 equal parts. A combination of two parts are connected in parallel and so on. Now resulting pairs of parallel combination are connected in series. The equivalent resistance of final combination is

$$\frac{1}{\text{Ans.}(5)}$$

Sol.

 $\frac{20\Omega}{\implies} \Rightarrow 10 \text{ equal part}$ 

Each part has resistance =  $2\Omega$ 

2 parts are connected in parallel so,  $R = 1\Omega$ 

Now, there will be 5 parts each of resistance  $1\Omega$ , they are connected in series.

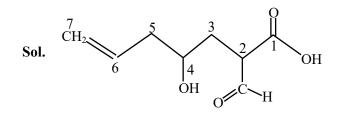
 $R_{eq} = 5R, R_{eq} = 5\Omega$ 

- 60. The current in an inductor is given by I = (3t + 8) where t is in second. The magnitude of induced emf produced in the inductor is 12 mV. The self-inductance of the inductor \_\_\_\_\_ mH.
- Ans. (4) Sol. I = 3t + 8 $\varepsilon = 12 \text{ mV}$  $|\varepsilon| = L \left| \frac{dI}{dt} \right|$  $12 = L \times 3$ L = 4 mH



	CHEMISTRY		TEST PAPER WITH SOLUTION
	SECTION-A		Fe <sup>+2</sup> ions undergoes hydrolysis, therefore while
61.	Match List - I with List - II.		preparing aqueous solution of ferrous sulphate and
	List - I List - II		ammonium sulphate in water dilute sulphuric acid
	(A) ICI (I) T -Shape		is added to prevent hydrolysis of ferrous sulphate.
	(B) ICI <sub>3</sub> (II) Square pyramidal	63.	Identify the major product in the following
	(C) CIF <sub>5</sub> (III) Pentagonal bipyramidal	00.	reaction.
	(D) $IF_7$ (IV) Linear		-
	Choose the <b>correct</b> answer from the options given		Br
	below:		$\begin{array}{c} & \overline{OH} \\ \hline CH_3 & \overline{C_2H_5OH} \\ \end{array} \\ \begin{array}{c} \overline{OH} \\ \hline C_2H_5OH \\ \end{array} \\ \begin{array}{c} \overline{OH} \\ \overline{OH} \\$
	(1) (A)–(I), (B)–(IV), C–(III), D–(II)		$C_2H_5OH$
	(2) (A)–(I), (B)–(III), C–(II), D–(IV)		
	(3) (A)–(IV), (B)–(I), C–(II), D–(III)		(1) CH <sub>2</sub>
	(4) (A)–(IV), (B)–(III), C–(II), D–(I)		
Ans.			Br
Sol.	A. I – Cl (iv) linear		(2)
			CH <sub>3</sub>
	B. $\bigcirc I = Cl$ (I) T-shape		
	Cl		CH
	F		(4) Ch <sub>3</sub>
	C. $F \downarrow F$ (II) Square pyramidal		
	F F	Ans.	(3)
	BEI	Sol.	CH <sub>3</sub> CH <sub>3</sub>
	F $F \downarrow F$		$ \begin{array}{c} & & \\ & & $
	D. $F$ (III) Pentagonal bipyramidal		
	F I I F	64.	The correct nomenclature for the following
62.	While preparing crystals of Mohr's salt, dil. $H_2SO_4$	U <b>7</b> .	compound is:
	is added to a mixture of ferrous sulphate and		0
	ammonium sulphate, before dissolving this mixture		
	in water, dil. $H_2SO_4$ is added here to:		✓ ↓ ↓ OH
	(1) prevent the hydrolysis of ferrous sulphate		OH O H
	<ul><li>(2) prevent the hydrolysis of ammonium sulphate</li></ul>		(1) 2-carboxy-4-hydroxyhept-6-enal
	<ul><li>(2) prevent the hydrorysis of annionant surplace</li><li>(3) make the medium strongly acidic</li></ul>		<ul><li>(2) 2-carboxy-4-hydroxyhept-7-enal</li><li>(3) 2-formyl-4-hydroxyhept-6-enoic acid</li></ul>
	<ul><li>(4) increase the rate of formation of crystals</li></ul>		(4) 2–formyl–4–hydroxyhept–7–enoic acid
A	•	Ans.	
Ans.	(1)		





2-formly-4-hydroxyhept-6-enoic acid

65. Given below are two statements : one is labelled as Assertion (A) and the other is labelled as Reason (R).
Assertion (A) : NH<sub>3</sub> and NF<sub>3</sub> molecule have pyramidal shape with a lone pair of electrons on nitrogen atom. The resultant dipole moment of NH<sub>3</sub> is greater than that of NF<sub>3</sub>.

**Reason (R) :** In  $NH_3$ , the orbital dipole due to lone pair is in the same direction as the resultant dipole moment of the N–H bonds. F is the most electronegative element.

In the light of the above statements, choose the **correct** answer from the options given below:

- (1) Both (A) and (R) are true and (R) is the correct explanation of (A)
- (2)(A) is false but (R) is true
- (3)(A) is true but (R) is false
- (4)Both (A) and (R) are true but (R) is NOT the correct explanation of (A)

Ans. (1)

Sol.  $F \stackrel{()}{=} K \stackrel{$ 

Resultant dipole moment =  $0.80 \times 10^{-30}$  Cm



Resultant dipole moment =  $4.90 \times 10^{-30}$  cm

**66.** Given below are two statements:

**Statement I** : On passing  $HCl_{(g)}$  through a saturated solution of  $BaCl_2$ , at room temperature white turbidity appears.

**Statement II :** When HCl gas is passed through a saturated solution of NaCl, sodium chloride is precipitated due to common ion effect.

In the light of the above statements, choose the **most appropriate** answer from the options given below:

- (1) Statement I is correct but Statement II is incorrect
- (2)Both Statement I and Statement II are incorrect
- (3) Statement I is incorrect but Statement II is correct
- (4) Both Statement I and Statement II are correct

Ans. (1)

- **Sol.** BaCl<sub>2</sub>, NaCl are soluble but on adding HCl(g) to BaCl<sub>2</sub>, NaCl solutions, Sodium or Barium chlorides may precipitate out, as a consequence of the law of mass action.
- 67. The metal atom present in the complex MABXL (where A, B, X and L are unidentate ligands and M is metal) involves sp<sup>3</sup> hybridization. The number of geometrical isomers exhibited by the complex is:
  - $\begin{array}{c} (1) \\ (3) \\ 2 \end{array} \begin{array}{c} (2) \\ (4) \\ (4) \\ (4) \\ 3 \end{array}$

Ans. (2)

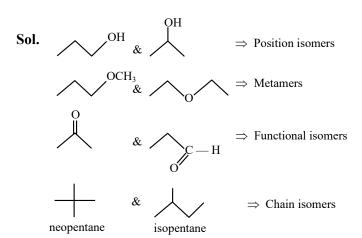
- **Sol.** Tetrahedral complex does not show geometrical isomerism.
- 68. Match List I with List II.

	List - I		List - II
	(Pair of Compounds)		(Isomerism)
(A)	n-propanol and	(I)	Metamerism
	Isopropanol		
(B)	Methoxypropane and	(II)	Chain Isomerism
	ethoxyethane		
(C)	Propanone and	(III)	Position
	propanal		Isomerism
(D)	Neopentane and	(IV)	Functional
	Isopentane		Isomerism
(1)(	(A)-(II), (B)-(I), (C)-(IV	/), (D	0)-(III)
(2) (	(A)-(III), (B)-(I), (C)-(I	I), (D	)–(IV)
(3) (	(A)-(I), (B)-(III), (C)-(I	V), (l	D)–(II)
(4) (	$A)_{-}(III) (B)_{-}(I) (C)_{-}(I)$	$\mathbf{v}$	D)_(II)

Ans. (4)





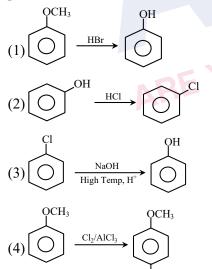


- The quantity of silver deposited when one coulomb 69. charge is passed through AgNO<sub>3</sub> solution:
  - (1) 0.1 g atom of silver
  - (2) 1 chemical equivalent of silver
  - (3) 1 g of silver
  - (4) 1 electrochemical equivalent of silver

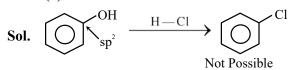
- W = ZItW = ZO
- O = W

$$Q = \frac{1}{Z}$$

- W = ZQ = (electrochemical equivalent)
- 70. Which one of the following reactions is NOT possible?



#### Ans. (2)



71. Given below are two statements : Statement I: The metallic radius of Na is 1.86 A° and the ionic radius of  $Na^+$  is lesser than 1.86 A°. Statement II : Ions are always smaller in size than the corresponding elements.

> In the light of the above statements, choose the correct answer from the options given below :

- (1) Statement I is correct but Statement II is false
- (2) Both Statement I and Statement II are true
- (3) Both Statement I and Statement II are false
- (4) Statement I is incorrect but Statement II is true

#### Ans. (1)

Sol.  $r_{Na} > r_{Na^+}$ 

> So, Statement (I) is correct but size of anions are greater than size of neutral atoms. So statement (II) is incorrect.

72. CH,CH,-OH (i) Jone's Reagent (ii) KMnO<sub>4</sub> (iii)NaOH, CaO,∆

> Consider the above reaction sequence and identify the major product P.

Ans. (1)

Sol. 
$$CH_3 - CH_2 - OH$$
  
 $KMnO_4$   
 $MaOH$   
 $CH_3 - C - OH$   
 $CH_3 - C - OH$   
 $CaI$   
 $CH_4 + Na_2CO$ 

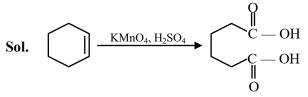
73. Consider the given chemical reaction :

$$\boxed{\frac{\text{KMnO}_4 - \text{H}_2\text{SO}_4}{\text{Heat}}} \text{Product "A"}$$

Product "A" is :

- (1) picric acid (2) oxalic acid (4) adipic acid (3) acetic acid

Ans. (4)





- 74. For the electro chemical cell  $M|M^{2+}||X|X^{2-}$ If  $E^{0}_{(M^{2+}/M)} = 0.46 \text{ V and } E^{0}_{(X/X^{2-})} = 0.34 \text{ V}.$ Which of the following is **correct** ?
  - (1)  $E_{cell} = -0.80 V$
  - (2)  $M + X \rightarrow M^2 + X^{2-}$  is a spontaneous reaction
  - (3)  $M^{2^+} + X^{2^-} \rightarrow M + X$  is a spontaneous reaction
  - (4)  $E_{cell} = 0.80 V$
- Ans. (3)
- **Sol.**  $M \mid M^{+2} \parallel X / X^{2-}$ 
  - $E_{cell}^{o} = E_{M/M^{+2}}^{o} + E_{X/X^{-2}}^{o}$ = -0.46 + 0.34 = -0.12V

As  $E_{cell}^{o}$  is negative so anode becomes cathode and cathode become anode. Spontaneous reaction will be  $M^{+2} + X^{2-} \longrightarrow M + X$ 

- **75.** The number of moles of methane required to produce  $11g \operatorname{CO}_2(g)$  after complete combustion is: (Given molar mass of methane in g mol<sup>-1</sup> : 16) (1) 0.75 (2) 0.25
  - (3) 0.35 (4) 0.5
- Ans. (2)

Sol. 
$$C_nH_{2n+2} + \frac{3n+1}{2}O_2 \longrightarrow nCO_2 + (n+1)H_2O$$
  
 $CH_4 + 2O_2 \longrightarrow CO_2 + 2H_2O$   
 $4gm$  11gm  
 $0.25$  mole 0.25 mole  $CO_2 + 2H_2O$ 

 $0.25 \text{ mole CH}_4$  gives  $0.25 \text{ mole (or 11gm) CO}_2$ ,

- 76. The number of complexes from the following with no electrons in the  $t_2$  orbital is \_\_\_\_\_. TiCl<sub>4</sub>, [MnO<sub>4</sub>]<sup>-</sup>, [FeO<sub>4</sub>]<sup>2-</sup>, [FeCl<sub>4</sub>]<sup>-</sup>, [CoCl<sub>4</sub>]<sup>2-</sup> (1) 3 (2) 1 (3) 4 (4) 2
- Ans. (1)

Sol. 
$$TiCl_4 \Rightarrow Ti^{+4}$$
  $e^0t_2^0$   
 $MnO_4^- \Rightarrow Mn^{+7}$   $e^0t_2^0$   
 $FeO_4^{2-} \Rightarrow Fe^{+6}$   $e^2t_2^0$   
 $FeCl_4^{2-} \Rightarrow Fe^{+2}$   $e^3t_2^3$   
 $CoCl_4^{2-} \Rightarrow Co^{+2}$   $e^4t_2^3$ 

77. The number of ions from the following that have the ability to liberate hydrogen from a dilute acid is .  $Ti^{2+}$ ,  $Cr^{2+}$  and  $V^{2+}$ 

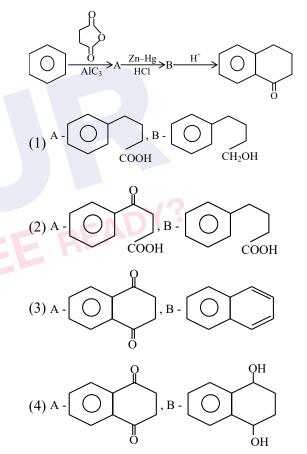
(3) 3 (4) 1

Ans. (3)

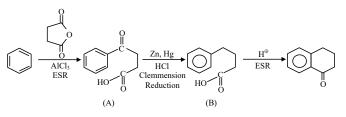
**Sol.** The ions  $Ti^{+2}$ ,  $V^{+2}$   $Cr^{+2}$  are strong reducing agents and will liberate hydrogen from a dilute acid, eg.

$$2Cr_{(aq.)}^{+2} + 2H_{(aq.)}^{+} \longrightarrow 2Cr_{(aq.)}^{+3} + H_2(g)$$

**78.** Identify A and B in the given chemical reaction sequence : -



Sol.





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- **79.** The correct statements from the following are :
  - (A) The decreasing order of atomic radii of group 13 elements is Tl > In > Ga > Al > B.
  - (B) Down the group 13 electronegativity decreases from top to bottom.
  - (C) Al dissolves in dil. HCl and liberate H<sub>2</sub> but conc. HNO<sub>3</sub> renders Al passive by forming a protective oxide layer on the surface.
  - (D) All elements of group 13 exhibits highly stable +1 oxidation state.
  - (E) Hybridisation of Al in  $[Al(H_2O)_6]^{3+}$  ion is  $sp^3d^2$ .

Choose the **correct** answer from the options given below :

- (1) (C) and (E) only
- (2) (A), (C) and (E) only
- (3) (A), (B), (C) and (E) only
- (4) (A) and (C) only
- Ans. (1)
- **Sol.** A. size order  $T\ell > In > Al > Ga > B$

B. Electronegativity order  $B > Al < Ga < In < T\ell$ 

D. B, Al are more stable in +3 oxidation state So, only C, E statements are correct.

- 80. Coagulation of egg, on heating is because of :
  - (1) Denaturation of protein occurs
  - (2) The secondary structure of protein remains unchanged
  - (3) Breaking of the peptide linkage in the primary structure of protein occurs
  - (4) Biological property of protein remains unchanged

# Ans. (1)

**Sol.** Coagulation of egg give primary structure of protein, which is known as denaturation of protein

## SECTION-B

81. Combustion of 1 mole of benzene is expressed at  $C_6H_6(1) + \frac{15}{2}O_2(g) \rightarrow CO_2(g) + 3H_2O(1).$ 

The standard enthalpy of combustion of 2 mol of benzene is - 'x' kJ.

(1) standard Enthalpy of formation of 1 mol of  $C_{6}H_{6}(1)$ , for the reaction

 $6C(\text{graphite}) + 3H_2(g) \rightarrow C_6H_6(1) \text{ is } 48.5 \text{ kJ mol}^{-1}.$ 

(2) Standard Enthalpy of formation of 1 mol of  $CO_2(g)$ , for the reaction

 $C(\text{graphite}) + O_{2(g)} \rightarrow CO_2(g) \text{ is } -393.5 \text{ kJ mol}^{-1}.$ 

(3) Standard and Enthalpy of formation of 1 mol of H<sub>2</sub>O(1), for the reaction

$$H_2(g) + \frac{1}{2}O_2(g) \rightarrow H_2O(1) \text{ is } -286 \text{ kJ mol}^{-1}.$$

#### Ans. (6535)

 $\mathbf{x} =$ 

Sol. 6C(graphite)+3H<sub>2</sub>(g)  $\rightarrow$  C<sub>6</sub>H<sub>6</sub>( $\ell$ );  $\Delta$ H = 48.5 kJ/mol

C(graphite)+O<sub>2</sub>(g) 
$$\rightarrow$$
 CO<sub>2</sub>(g);  $\Delta$ H = -393.5 kJ/mol

$$H_2^{(g)} + \frac{1}{2}(g) \longrightarrow H_2O(\ell)$$
;  $\Delta H = -286 \text{ kJ/mol}$ 

equation 
$$-(1) \times 1 + (2) \times 6 + (3) \times 3$$

- 48.5 -6 × 393.5 - 3 × 286

- = -3267.5 kJ for 1 mol
- = 6535 kJ for 2 mol

**Ans.** 6535 kJ

82. The fusion of chromite ore with sodium carbonate in the presence of air leads to the formation of products A and B along with the evolution of CO<sub>2</sub>. The sum of spin-only magnetic moment values of A and B is \_\_\_\_ B.M. (Nearest integer) (Given atomic number : C : 6, Na : 11, O : 8, Fe : 26, Cr : 24]

Sol. 
$$4\text{FeCr}_2\text{O}_4 + 8\text{Na}_2\text{CO}_3 + 7\text{O}_2 \rightarrow$$
  
 $8\text{Na}_2\text{CrO}_4 + 2\text{Fe}_2\text{O}_3 + 8\text{CO}_2$   
A B

Spin only magnetic moment

For Na<sub>2</sub>CrO<sub>4</sub> 
$$\mu_{\rm B} = 0$$
  
For Fe<sub>2</sub>O<sub>3</sub>  $\mu_{\rm B} = 5.9$   
sum = 5.9



83. X of enthanamine was subjected to reaction with  $NaNO_2/HCl$  followed by hydrolysis to liberate  $N_2$  and HCl. The HCl generated was completely neutralised by 0.2 moles of NaOH. X is \_\_\_\_\_ g.

- Sol.  $CH_3$ — $CH_2$ — $NH_2$ — $NH_2$ —HCl  $CH_3$ — $CH_2$ — $N_2Cl$ 0.2 mole MW of ethanamine = 45  $45 \times 0.2 = 9 \text{ gm}$   $CH_3$ — $CH_2$ — $OH + N_2 + HCl$ (g) 0.2 mole
- 84. In an atom, total number of electrons having quantum numbers n = 4,  $|m_i| = 1$  and  $m_s = -\frac{1}{2}$  is

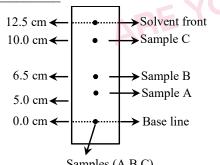
Ans. (6)

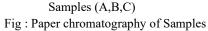
Sol. n = 4  $\ell$   $m_{\ell}$  0 0 1 -1, 0, +1 2 -2, -1, 0, +1, +2, +3So number of orbital associated with

 $n = 4, |m_{\ell}| = 1 \text{ are } 6$ 

Now each orbital contain one  $e^-$  with  $m_s = -\frac{1}{2}$ 

85. Using the given figure, the ratio of  $R_r$  values of sample A and sample C is  $x \times 10^{-2}$ . Value of x is





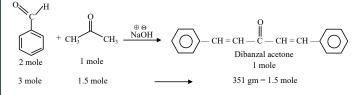
Ans. (50)

Sol. 
$$R_{f} \text{ of } A = \frac{5}{12.5}$$
  $R_{f} \text{ of } C = \frac{10}{12.5}$   
Ratio  $= \frac{R_{f(A)}}{R_{f(C)}} = \frac{1}{2} = 0.5 \text{ or } 50 \times 10^{-2}$ 

86. In the Claisen-Schmidt reaction to prepare 351 g of dibenzalacetone using 87 g of acetone, the amount of benzaldehyde required is \_\_\_\_\_\_g. (Nearest integer)

Ans. (318)

Sol. Claisen Schmidt reaction



mw of benzaldehyde = 
$$106$$

- $106 \times 3 = 318$  gm. Benzaldehyde is required to give 1.5 mole (or 351 gm) product
- **87.** Consider the following single step reaction in gas phase at constant temperature.
  - $2A_{\scriptscriptstyle (g)} + B_{\scriptscriptstyle (g)} \to C_{\scriptscriptstyle (g)}$

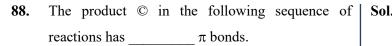
The initial rate of the reaction is recorded as  $r_1$  when the reaction starts with 1.5 atm pressure of A and 0.7 atm pressure of B. After some time, the rate  $r_2$  is recorded when the pressure of C becomes 0.5 atm. The ratio  $r_1 : r_2$  is \_\_\_\_\_ × 10<sup>-1</sup>. (Nearest integer)

Ans. (315)

**Sol.**  $2A(g) + B(g) \longrightarrow C(g)$ 

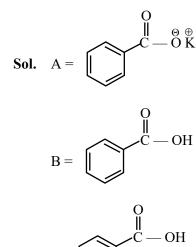
- $r_1 = 1.5 \text{ atm} = 0.7 \text{ atm}$
- r<sub>2</sub> 0.5 atm 0.2 atm 0.5 atm ∴ r = K [P<sub>A</sub>]<sup>2</sup>[P<sub>B</sub>] r<sub>1</sub> = K [1.5]<sup>2</sup>[0.7] r<sub>2</sub> = K [0.5]<sup>2</sup>[0.2]  $\frac{r_1}{r_2} = 9 \times \frac{7}{2} = 31.5 = 315 \times 10^{-1}$ Ans. 315





$$\underbrace{\frac{\text{KMnO}_{4}-\text{KOH}}{\Delta}}_{\text{KMnO}_{4}-\text{KOH}} \otimes \underbrace{\frac{\text{H}_{3}\text{O}^{+}}{\text{FeBr}_{3}}}_{\text{FeBr}_{3}} \otimes \underbrace{\frac{\text{Br}_{2}}{\text{FeBr}_{3}}}_{\text{FeBr}_{3}} \otimes \underbrace{\frac{\text{Br}_{2}}{\text{FeBr}_{4}}}_{\text{FeBr}_{3}} \otimes \underbrace{\frac{\text{Br}_{2}}}_{\text{FeBr}_{4}} \otimes \underbrace{\frac{\text{Br}_{2}}{\text{Fe$$

Ans. (4)





 $\pi$  bonds = 4

C =

89. Considering acetic acid dissociates in water, its dissociation constant is  $6.25 \times 10^{-5}$ . If 5 mL of acetic acid is dissolved in 1 litre water, the solution will freeze at  $-x \times 10^{-2}$  °C, provided pure water freezes at 0 °C.

x = \_\_\_\_\_. (Nearest integer)

Given :  $(K_r)_{water} = 1.86 \text{ K kg mol}^{-1}$ . density of acetic acid is 1.2 g mol<sup>-1</sup>

> molar mass of water =  $18 \text{ g mol}^{-1}$ . molar mass of acetic acid =  $60 \text{ g mol}^{-1}$ . density of water =  $1 \text{ g cm}^{-3}$

Acetic acid dissociates as

$$CH_3COOH \rightleftharpoons CH_3COO^{\Theta} + H^{\oplus}$$

Ans. (19)

Mass of CH<sub>3</sub>COOH = V × d  
= 5 ml × 1.2 g/ml  
= 6 gm  

$$n_{CH_3COOH} = \frac{6}{60} = 0.1 \text{ mol}$$
  
 $m_{CH_3COOH} \approx M_{CH_3COOH} = \frac{0.1}{1} = 0.1 \text{ M}$   
CH<sub>3</sub>COOH  $\implies$  CH<sub>3</sub>COO<sup>-</sup> + H<sup>+</sup>  
C  
C - C $\alpha$  C $\alpha$  C $\alpha$   
 $K_a = \frac{C\alpha^2}{1-\alpha}$   
 $1 - \alpha \approx 1 \Rightarrow K_a = C\alpha^2$   
 $\alpha = \sqrt{\frac{Ka}{C}} = \sqrt{\frac{6.25 \times 10^{-5}}{0.1}} = 25 \times 10^{-3}$   
V.f. (i) = 1 +  $\alpha$ (n - 1) = 1 +  $\alpha$ (2 - 1) = 1 +  $\alpha$   
= 1 + 25 × 10<sup>-3</sup> = 1.025  
 $\Delta T_r = iK_r m$   
= (1.025)(1.86)(0.1)  
= 0.19  
= 19 × 10<sup>-2</sup>  
Number of compounds from the following  $\gamma$ 

90. Number of compounds from the following with zero dipole moment is \_\_\_\_\_\_.
HF, H<sub>2</sub>, H<sub>2</sub>S, CO<sub>2</sub>, NH<sub>3</sub>, BF<sub>3</sub>, CH<sub>4</sub>, CHCl<sub>3</sub>, SiF<sub>4</sub>, H<sub>2</sub>O, BeF<sub>2</sub>

Ans. (6)

**Sol.**  $H_2$ ,  $CO_2$ ,  $BF_3$ ,  $CH_4$ ,  $SiF_4$ ,  $BeF_2$ 

are symm. molecule so dipole moment is zero