

(Held On Fri	leld On Friday 05th April, 2024)		TIME: 9:00 AM to 12:00 NOON
	MATHEMATICS		TEST PAPER WITH SOLUTION
the $\frac{x-7}{4} = \frac{y-3}{3}$	SECTION-A e distance of the point of intersection of ines $\frac{x+6}{3} = \frac{y}{2} = \frac{z+1}{1}$ and $\frac{x+9}{2} = \frac{z-4}{2}$ from the point (7, 8, 9). Then	2.	Let a rectangle ABCD of sides 2 and 4 be inscribed in another rectangle PQRS such that the vertices of the rectangle ABCD lie on the sides of the rectangle PQRS. Let a and b be the sides of the rectangle PQRS when its area is maximum. Then $(a + b)^2$ is equal to :
$\frac{x-7}{4} = \frac{y-3}{3}$ $x = 4\mu + 7,$ $3\lambda - 6 = 4\mu$ $2\lambda = 3\mu + 9$	(2) 69 (4) 78 $=\frac{z+1}{1} = \lambda \qquad \dots(1)$ $y = 2\lambda, z = \lambda - 1$ $\frac{.9}{-2} = \frac{z-4}{2} = \mu \qquad \dots(2)$ $y = 3\mu + 9, z = 2\mu + 4$ $\mu + 7 \Rightarrow 3\lambda - 4\mu = 13 \qquad \dots(3) \times 2$ $P \Rightarrow 2\lambda - 3\mu = 9 \qquad \dots(4) \times 3$	Sol.	(a + b) is equal to : (1) 72 (2) 60 (3) 80 (4) 64 Ans. (1) R $4  ext{ 90-0}$ $4  ext{ 90-0}$ $2  ext{ 2}$ $2  ext{ cos}(90-0)$ $2  ext{ 2}$ $2  ext{ cos}(90-0)$
$\Rightarrow 3\lambda - 4(-3\lambda = 9)$ $\lambda = 3$ int. point ( $d^{2} = 16 + 4$	u = 27 $= -1$ $= -1$ $= -1$ $= -1$ $= 13$ $= 3, 6, 2); (7, 8, 9)$		Area = $(4\cos\theta + 2\sin\theta) (2\cos\theta + 4\sin\theta)$ = $8\cos^2\theta + 16\sin\theta\cos\theta + 4\sin\theta\cos\theta + 8\sin^2\theta$ JEE Main ( = $8 + 20\sin\theta\cos\theta$ = $8 + 10\sin2\theta$ Max Area = $8 + 10 = 18 (\sin2\theta = 1) \theta = 45^{\circ}$ $(a + b)^2 = (4\cos\theta + 2\sin\theta + 2\cos\theta + 4\sin\theta)^2$ = $(6\cos\theta + 6\sin\theta)^2$ = $36 (\sin\theta + \cos\theta)^2$ = $36 (\sqrt{2})^2$

= 72



4.



If y = y(x) is the solution of the differential

3. Let two straight lines drawn from the origin O intersect the line 3x + 4y = 12 at the points P and Q such that  $\triangle OPQ$  is an isosceles triangle and  $\angle POQ = 90^{\circ}$ . If  $l = OP^2 + PQ^2 + QO^2$ , then the greatest integer less than or equal to *l* is : (1) 44 (2) 48 (3) 46 (4) 42

Ans. (3)

н

.

Sol.  

$$Q(rcos(90+\theta), rsin(90+\theta) = (-rsin\theta, rcos\theta)$$
  
 $P(rcos\theta, rsin\theta)$   
 $O$ 

$$3x + 4y = 12$$

$$3(r\cos\theta) + 4(r\sin\theta) = 12$$

$$r(3\cos\theta + 4\sin\theta) = 12 \dots(1)$$

$$3(-r\sin\theta) + 4(r\cos\theta) = 12$$

$$r(-3\sin\theta + 4\cos\theta) = 12 \dots(2)$$

$$\left(\frac{12}{r}\right)^2 + \left(\frac{12}{r}\right)^2 = (3\cos\theta + 4\sin\theta)^2 + (-3\sin\theta + 4\cos\theta)$$

$$2\left(\frac{12}{r}\right)^2 = 9 + 16$$

$$\frac{2 \times 144}{r^2} = 25 \implies 288 = 25r^2$$

$$\implies \frac{288}{25} = r^2$$

$$\Rightarrow \sqrt{2}\left(\frac{12}{5}\right) = r$$

$$\ell = OP^2 + PQ^2 + QO^2$$

$$\ell = r^2 + r^2 + r^2(\cos\theta + \sin\theta)^2 + r^2(\sin\theta + \cos\theta)^2$$

 $= 2r^{2} + r^{2}(1 + \sin 2\theta + 1 - 2\sin 2\theta)$ 

 $=4\left(\frac{288}{25}\right)=\frac{1152}{25}=46.08$ 

equation 
$$\frac{dy}{dx} + 2y = \sin(2x), y(0) = \frac{3}{4}$$
, then  
 $y\left(\frac{\pi}{8}\right)$  is equal to :  
(1)  $e^{-\pi/8}$  (2)  $e^{-\pi/4}$   
(3)  $e^{\pi/4}$  (4)  $e^{\pi/8}$   
Ans. (2)  
Sol.  $\frac{dy}{dx} + 2y = \sin 2x, y(0) = \frac{3}{4}$   
I.F =  $e^{\int 2dx} = e^{2x}$   
 $y.e^{2x} = \int e^{2x} \sin 2x \, dx$   
 $y.e^{2x} = \frac{e^{2x}(2\sin 2x - 2\cos 2x)}{4 + 4} + C$   
 $x = 0, y = \frac{3}{4} \Rightarrow \frac{3}{4} \cdot 1 = \frac{1(0 - 2)}{8} + C$   
 $\frac{3}{4} = -\frac{1}{4} + C$   
 $1 = C$   
 $y = \frac{2\sin 2x - 2\cos 2x}{8} + 1 \cdot e^{-2x}$   
 $x = \frac{\pi}{8}, y = \frac{1}{8} \left(2\sin \frac{\pi}{4} - 2\cos \frac{\pi}{4}\right) + e^{-2\left(\frac{\pi}{8}\right)}$   
 $y = 0 + e^{-\frac{\pi}{4}}$ 

5. For the function

$$f(x) = \sin x + 3x - \frac{2}{\pi} (x^2 + x), \text{ where } x \in \begin{bmatrix} 0, \frac{1}{2} \end{bmatrix}, \text{ Main 0}$$

consider the following two statements :

(I) f is increasing in  $\left(0, \frac{\pi}{2}\right)$ .

(II) f' is decreasing in 
$$\left(0, \frac{\pi}{2}\right)$$
.

Between the above two statements,

- (1) only (I) is true.
- (2) only (II) is true.
- (3) neither (I) nor (II) is true.
- (4) both (I) and (II) are true.

 $=2r^{2}+2r^{2}$ 

 $=4r^{2}$ 

 $[\ell] = 46$ 



Ans. (4) **Sol.**  $f(x) = \sin x + 3x - \frac{2}{\pi} (x^2 + x) \quad x \in \left[0, \frac{\pi}{2}\right]$  $f'(x) = \cos x + 3 - \frac{2}{\pi} (2x + 1) > 0 \quad f(x) \uparrow$  $f'(x) = -\sin x + 0 - \frac{\pi}{2}(2)$  $=-\sin x-\frac{4}{\pi}<0$  f'(x)  $\downarrow$  $0 < x < \frac{\pi}{2}$  $\Rightarrow -\frac{2}{\pi} \left( \begin{array}{c} 0 < 2x < \pi \\ +1 & +1 \end{array} \right)$  $-\frac{2}{\pi} > \frac{-2}{\pi} (2x+1) > -\frac{2}{\pi} (\pi+1)$  $3 - \frac{2}{\pi} > 3 - \frac{2}{\pi}(2x+1) > 3 - \frac{2}{\pi}(\pi+1)$ If the system of equations 6.  $11x + y + \lambda z = -5$ 2x + 3y + 5z = 3 $8x - 19y - 39z = \mu$ has infinitely many solutions, then  $\lambda^4 - \mu$  is equal to: (2) 45 (4) 51 (1) 49(3) 47Ans. (3) **Sol.**  $11x + y + \lambda z = -5$ r-2024 Paper<sub>2x</sub>Shifty 2 5z = 3 $8x - 19y - 39z = \mu$ for infinite sol.  $\mathbf{D} = \begin{vmatrix} 11 & 1 & \lambda \\ 2 & 3 & 5 \end{vmatrix} = \mathbf{0}$ 8 -19 -39  $\Rightarrow 11(-117+95) - 1(-78-40) + \lambda(-38-24)$  $\Rightarrow 11(-22) + 118 - \lambda(62) = 0$  $\Rightarrow 62\lambda = 118 - 242$  $\Rightarrow \lambda = \frac{-124}{62} = -2$ 

$$D_{1} = \begin{vmatrix} -5 & 1 & -2 \\ 3 & 3 & 5 \\ \mu & -19 & -39 \end{vmatrix} = 0$$
  

$$\Rightarrow -5(-117 + 95) - 1(-117 - 5\mu) - 2(-57 - 3\mu) = 0$$
  

$$\Rightarrow -5(-22) + 117 + 5\mu + 114 + 6\mu = 0$$
  

$$\Rightarrow 11\mu = -110 - 231 = -341$$
  

$$\Rightarrow \mu = -31$$
  

$$\lambda^{4} - \mu = (-2)^{4} - (-31) = 16 + 31 = 47$$
  
7. Let A = {1, 3, 7, 9, 11} and B = {2, 4, 5, 7, 8, 10, 12}. Then the total number of one-one maps  
f: A  $\rightarrow$  B, such that f(1) + f(3) = 14, is :  
(1) 180 (2) 120  
(3) 480 (4) 240  
Ans. (4)  
Sol.  

$$(5) (7) - (7)$$





$$\lim_{x \to 0} = \frac{-\beta + x(3 + \alpha) + \frac{9\beta x^2}{\underline{|2|}} + \left(\frac{-27}{\underline{|3|}} - \frac{\alpha}{\underline{|3|}}\right) x^3 \dots}{x^3} = f(0)$$

for exist

$$\beta = 0, 3 + \alpha = 0, -\frac{27}{\underline{3}} - \frac{\alpha}{\underline{3}} = f(0)$$
$$\alpha = -3, -\frac{27}{6} - \frac{(-3)}{6} = f(0)$$
$$f(0) = \frac{-27 + 3}{6} = -4$$

9. The integral 
$$\int_{0}^{\frac{1}{4}} \frac{136 \sin x}{3 \sin x + 5 \cos x} dx$$
 is equal to :

(1) 
$$3\pi - 50 \log_e 2 + 20 \log_e 5$$

(2) 
$$3\pi - 25 \log_e 2 + 10 \log_e 5$$

(3) 
$$3\pi - 10 \log_{e}(2\sqrt{2}) + 10 \log_{e} 5$$

(4)  $3\pi - 30 \log_e 2 + 20 \log_e 5$ 

#### Ans. (1)

Sol. 
$$I = \int_{0}^{\pi/4} \frac{136 \sin x}{3 \sin x + 5 \cos x} dx$$
  

$$136 \sin x = A(3 \sin x + 5 \cos x) + B(3 \cos x - 5 \sin x)$$
  

$$136 = 3A - 5B \qquad \dots(1)$$
  

$$0 = 5A + 3B \qquad \dots(2)$$
  

$$3B = -5A \Rightarrow B = -\frac{5}{3}A$$
  

$$3B = -5A \Rightarrow B = -\frac{5}{3}A$$
  

$$136 = 3A - 5\left(-\frac{5}{3}A\right)$$
  

$$136 = 3A + \frac{25}{3}A$$
  

$$136 = \frac{34A}{3}$$
  

$$\Rightarrow A = \frac{136 \times 3}{34} = 12$$

$$I = \int_{0}^{\pi/4} \frac{A(3\sin x + 5\cos x)}{3\sin x + 5\cos x} + \int_{0}^{\pi/4} \frac{B(3\cos x - 5\sin x)}{3\sin x + 5\cos x}$$
$$= A(x)_{0}^{\pi/4} + B\left[\ell n(3\sin x + 5\cos x)\right]_{0}^{\pi/4}$$
$$= 12\left(\frac{\pi}{4}\right) - 20\ell n\left(\frac{3}{\sqrt{2}} + \frac{5}{\sqrt{2}}\right) - \ell n(0+5)$$
$$= 3\pi - 20\ell n 4\sqrt{2} + 20\ell n 5$$
$$= 3\pi - 20 \times \frac{5}{2}\ell n 2 + 20\ell n 5$$
$$= 3\pi - 50\ell n 2 + 20\ell n 5$$

10. The coefficients a, b, c in the quadratic equation ax<sup>2</sup> + bx + c = 0 are chosen from the set {1, 2, 3, 4, 5, 6, 7, 8}. The probability of this equation having repeated roots is :

(1) 
$$\frac{3}{256}$$
  
(2)  $\frac{1}{128}$   
(3)  $\frac{1}{64}$   
(4)  $\frac{3}{128}$   
(4)  $\frac{3}{128}$   
(5) **Sol.**  $ax^2 + bx + c = 0$   
(4)  $\frac{3}{128}$   
(5)  $ax^2 + bx + c = 0$   
(5)  $a, b, c \in \{1, 2, 3, 4, 5, 6, 7, 8\}$   
Repeated roots  $D = 0$   
 $\Rightarrow b^2 - 4ac = 0 \Rightarrow b^2 = 4ac$   
Prob  $= \frac{8}{8 \times 8 \times 8} = \frac{1}{64}$   
 $\Rightarrow (a, b, c)$   
(1, 2, 1); (2, 4, 2); (1, 4, 4); (4, 4, 1); (3, 4)

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6, 3);

 $(2,\,8,\,8)\,;(8,\,8,\,2)\,;(4,\,8,\,4)$ 

8 case

 $B = \frac{-5}{3}(12) = -20$ 



- 11. Let A and B be two square matrices of order 3 such that |A| = 3 and |B| = 2. Then  $|A^T A(adj(2A))^{-1} (adj(4B))(adj(AB))^{-1}AA^T|$ is equal to : (1) 64(2) 81(3) 32(4) 108Ans. (1) **Sol.** |A| = 3, |B| = 2 $|A^{T}A(adj(2A))^{-1}(adj(4B))(adj(AB))^{-1}AA^{T}|$  $= 3 \times 3 \times |(\mathrm{adj}(2\mathrm{A})^{-1}| \times |\mathrm{adj}(4\mathrm{B})| \times |(\mathrm{adj}(\mathrm{A}\mathrm{B}))^{-1}| \times 3 \times 3$  $2^{12} \times 2^2 \qquad \frac{1}{|\operatorname{adj}(AB)|}$  $\frac{1}{|adj(2A)|}$  $=\frac{1}{|adjB \cdot adjA|}$  $=\frac{1}{2^6 |adjA|}$  $=\frac{1}{2^2 \cdot 3^2}$  $=\frac{1}{2^{6}\cdot 3^{2}}$  $=3^4 \cdot \frac{1}{2^6 \cdot 3^2} \cdot 2^{12} \cdot 2^2 \cdot \frac{1}{2^2 \cdot 3^2} = 64$
- 12. Let a circle C of radius 1 and closer to the origin be such that the lines passing through the point (3, 2) and parallel to the coordinate axes touch it. Then the shortest distance of the circle C from the point

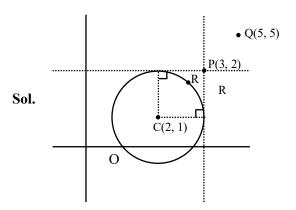
2) 5

(4) 4

(5, 5) is :

(1) 2√2 r-2024 Paper<sub>(3</sub>\$þjí<u>f</u>52

Ans. (4)



- Coordinates of the centre will be (2, 1) Equation of circle will be  $(x-2)^2 + (y-1)^2 = 1$   $QC = \sqrt{(5-2)^2 + (5-1)^2}$  QC = 5shortest distance = RQ = CQ - CR = 5 - 1= 4
- 13. Let the line 2x + 3y k = 0, k > 0, intersect the x-axis and y-axis at the points A and B, respectively. If the equation of the circle having the line segment AB as a diameter is  $x^2 + y^2 3x 2y = 0$  and the length of the latus rectum of the ellipse  $x^2 + 9y^2 = k^2$  is  $\frac{m}{n}$ , where m and n are coprime,

then 2m + n is equal to

Ans. (2)

**Sol.** Centre of the circle =  $\left(\frac{3}{2}, 1\right)$ 

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Equation of diameter = 2x + 3y - k = 0

$$2\left(\frac{3}{2}\right) + 3(1) - k = 0$$

 $\Rightarrow$  k = 6

Now, Equation of ellipse becomes

$$x^{2} + 9y^{2} = 36$$
$$\frac{x^{2}}{6^{2}} + \frac{y^{2}}{2^{2}} = 1$$

Give yourself an extra edge



length of LR 
$$=\frac{2b^2}{a} = \frac{2.2^2}{6} = \frac{8}{6} = \frac{4}{3} = \frac{m}{n}$$

 $\therefore 2m + n = 2(4) + 3 = 11$ 

14. Consider the following two statements :

Statement I : For any two non-zero complex numbers  $z_1, z_2$ 

$$(|z_1| + |z_2|) \left| \frac{z_1}{|z_1|} + \frac{z_2}{|z_2|} \right| \le 2(|z_1| + |z_2|)$$
 and

**Statement II :** If x, y, z are three distinct complex numbers and a, b, c are three positive real numbers

such that 
$$\frac{a}{|y-z|} = \frac{b}{|z-x|} = \frac{c}{|x-y|}$$
, then  
$$\frac{a^2}{y-z} + \frac{b^2}{z-x} + \frac{c^2}{x-y} = 1.$$

Between the above two statements,

(1) both Statement I and Statement II are incorrect.

(2) Statement I is incorrect but Statement II is correct.

(3) Statement I is correct but Statement II is incorrect.

(4) both Statement I and Statement II are correct.

Ans. (3)

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$$\left( \left| z_{1} \right| + \left| z_{2} \right| \right) \left| \frac{z_{1}}{\left| z_{1} \right|} + \frac{z_{2}}{\left| z_{2} \right|} \right|$$
Since  $\left| \frac{z_{1}}{\left| z_{1} \right|} + \frac{z_{2}}{\left| z_{2} \right|} \right| \le \left| \frac{z_{1}}{\left| z_{1} \right|} \right| + \left| \frac{z_{2}}{\left| z_{2} \right|} \right|$ 

$$\left| \frac{z_{1}}{\left| z_{1} \right|} + \frac{z_{2}}{\left| z_{2} \right|} \right| \le \frac{\left| z_{1} \right|}{\left| z_{1} \right|} + \frac{\left| z_{2} \right|}{\left| z_{2} \right|}$$

$$\left| \frac{z_{1}}{\left| z_{1} \right|} + \frac{z_{2}}{\left| z_{2} \right|} \right| \le 2$$

$$(|z_1| + |z_2|) \left( \left| \frac{z_1}{|z_1|} + \frac{z_2}{|z_2|} \right| \right) \le 2(|z_1| + |z_2|)$$

: statement I is correct

For Statement II :

$$\frac{a}{|y-z|} = \frac{b}{|z-x|} = \frac{c}{|x-y|}$$
$$\frac{a^2}{|y-z|^2} = \frac{b^2}{|z-x|^2} = \frac{c^2}{|x-y|^2} = \lambda$$
$$a^2 = \lambda(|y-z|^2) = \lambda(y-z)(\overline{y}-\overline{z})$$
$$b^2 = \lambda(z-x)(\overline{z}-\overline{x}) \text{ and } c^2 = \lambda(x-y)(\overline{x}-\overline{y})$$
$$\frac{a^2}{y-z} + \frac{b^2}{z-x} + \frac{c^2}{x-y} = \lambda(\overline{y}-\overline{z}+\overline{z}-\overline{x}+\overline{x}-\overline{y}) = 0$$

Statement II is false

**15.** Suppose 
$$\theta \in \left[0, \frac{\pi}{4}\right]$$
 is a solution of  $4\cos\theta - 3\sin\theta = 1$ .

Then  $\cos\theta$  is equal to :

(1) 
$$\frac{4}{(3\sqrt{6}-2)}$$
 (2)  $\frac{6-\sqrt{6}}{(3\sqrt{6}-2)}$   
(3)  $\frac{6+\sqrt{6}}{(3\sqrt{6}+2)}$  (4)  $\frac{4}{(3\sqrt{6}+2)}$ 

Ans. (1)

Sol. 
$$4\left(\frac{1-\tan^2\theta/2}{1+\tan^2\theta/2}\right) - 3\left(\frac{2\tan\frac{\theta}{2}}{1+\tan^2\frac{\theta}{2}}\right) = 1$$
$$\det \tan\frac{\theta}{2} = t$$
$$\frac{4-4t^2-6t}{1+t^2} = 1$$
$$4-4t^2-6t = 1+t^2$$

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 $\sqrt{100} - 1 = m \implies m = 9$ 

 $\frac{1}{1\cdot 2} + \frac{1}{2\cdot 3} + \dots \frac{1}{99\cdot 100} = n$ 

 $\frac{1}{1} - \frac{1}{2} + \frac{1}{2} - \frac{1}{3} \dots \frac{1}{99} - \frac{1}{100} = n$ 



Then

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$$\Rightarrow 5t^{2} + 6t - 3 = 0$$

$$\Rightarrow t = \frac{-6 \pm \sqrt{36} - 4(5)(-3)}{2(5)}$$

$$= \frac{-6 \pm 4\sqrt{6}}{10}$$

$$= \frac{-6 \pm 4\sqrt{6}}{10}$$

$$t = \frac{-3 \pm 2\sqrt{6}}{5}$$

$$\cos\theta = \frac{1 - t^{2}}{1 + t^{2}} = \frac{1 - \left(\frac{2\sqrt{6} - 3}{5}\right)^{2}}{1 + \left(\frac{24 + 9 - 12\sqrt{6}}{25}\right)}$$

$$= \frac{25 - 33 \pm 12\sqrt{6}}{25 \pm 33 - 12\sqrt{6}} = \frac{12\sqrt{6} - 8}{88 - 12\sqrt{6}} = \frac{6\sqrt{6} - 4}{29 - 6\sqrt{6}} \times \frac{29 + 6\sqrt{6}}{29 + 6\sqrt{6}}$$

$$= \frac{100 + 150\sqrt{6}}{625} = \frac{4 + 6\sqrt{6}}{25} \times \frac{4 - 6\sqrt{6}}{4 - 6\sqrt{6}}$$

$$= \frac{100 + 150\sqrt{6}}{25(4 - 6\sqrt{6})} = \frac{-8}{4 - 6\sqrt{6}} = \frac{4}{3\sqrt{6} - 2}$$
16. If  $\frac{1}{\sqrt{1} + \sqrt{2}} + \frac{1}{\sqrt{2} + \sqrt{3}} + \dots + \frac{1}{\sqrt{99} + \sqrt{100}} = m$  and  $\frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \dots + \frac{1}{99 \cdot 100} = n$ , then the point (m, n)  
wr-2024 Papertischiftlike line  
(1) 11(x - 1) - 100(y - 2) = 0  
(2) 11(x - 2) - 100(y - 1) = 0  
(3) 11(x - 1) - 100y = 0  
(4) 11x - 100y = 0
Ans. (4)  
Sol.  $\frac{1}{\sqrt{1} + \sqrt{2}} + \frac{1}{\sqrt{2} + \sqrt{3}} + \dots + \frac{1}{\sqrt{99} + \sqrt{100}} = m$ 

$$1 - \frac{1}{100} = n$$

$$\frac{99}{100} = n$$
(m, n) =  $\left(9, \frac{99}{100}\right)$ 

$$\Rightarrow 11(9) - 100 \left(\frac{99}{100}\right)$$

$$= 99 - 99 = 0$$
Ans. option (4) 11x - 100y = 0  
7. Let  $f(x) = x^5 + 2x^3 + 3x + 1$ ,  $x \in \mathbb{R}$ , and  $g(x)$  be a function such that  $g(f(x)) = x$  for all  $x \in \mathbb{R}$ . Then  
 $\frac{g(7)}{g'(7)}$  is equal to :  
(1) 7 (2) 42  
(3) 1 (4) 14  
Ans. (4)  
bl.  $f(x) = x^5 + 2x^3 + 3x + 1$   
 $f'(x) = 5x^4 + 6x^2 + 3$   
 $f'(1) = 5 + 6 + 3 = 14$   
 $g(f(x))f'(x) = 1$   
for  $f(x) = 7$   
 $\Rightarrow x^5 + 2x^3 + 3x + 1 = 7$   
 $\Rightarrow x = 1$   
 $g'(7) f'(1) = 1 \Rightarrow g'(7) = \frac{1}{f'(1)} = \frac{1}{14}$ 

 $\frac{\sqrt{1} - \sqrt{2}}{-1} + \frac{\sqrt{2} - \sqrt{3}}{-1} \dots \frac{\sqrt{99} - \sqrt{100}}{-1} = m$ 

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$$x = 1, f(x) = 7 \Rightarrow g(7) = 1$$

$$\frac{g(7)}{g'(7)} = \frac{1}{1/14} = 14$$
18. If A(1, -1, 2), B(5, 7, -6), C(3, 4, -10) and D(-1, -4, -2) are the vertices of a quadrilateral ABCD, then its area is :
(1)  $12\sqrt{29}$  (2)  $24\sqrt{29}$ 
(3)  $24\sqrt{7}$  (4)  $48\sqrt{7}$ 
Ans. (1)
Sol. A(1, -1, 2)
B(5, 7, -6)
C(3, 4, -10)
D(-1, -4, -2)
Area =  $\frac{1}{2} |\overline{AC} \times \overline{BD}| = \frac{1}{2} |(2\hat{i} + 5\hat{j} - 12\hat{k}) \times (6\hat{i} + 11\hat{j} - 4\hat{k})|$ 

$$= \frac{1}{2} |112\hat{i} - 64\hat{j} - 8\hat{k}|$$

$$= 4 \sqrt{196 + 64 + 1}$$

$$= 4\sqrt{261}$$

$$= 12\sqrt{29}$$
Arc2024 Paper The Vietable of  $\int_{-\pi}^{\pi} \frac{2y(1 + \sin y)}{1 + \cos^2 y} dy$  is :
(1)  $\pi^2$  (2)  $\frac{\pi^2}{2}$ 
(3)  $\frac{\pi}{2}$  (4)  $2\pi^2$ 

(Odd) (Even)  

$$= 0 + 2.2 \int_{0}^{\pi} y \left(\frac{\sin y}{1 + \cos^{2} y}\right) dy$$

$$I = 4 \int_{0}^{\pi} \frac{y \sin y}{1 + \cos^{2} y} dy$$

$$I = 4 \int_{0}^{\pi} \frac{\pi \sin y}{1 + \cos^{2} y} dy$$

$$2I = 4 \int_{0}^{\pi} \frac{\pi \sin y}{1 + \cos^{2} y} dy$$

$$I = 2\pi \int_{0}^{\pi} \frac{\sin y}{1 + \cos^{2} y} dy$$

$$I = 2\pi \left[ \left( -\frac{\pi}{4} \right) - \left( \frac{\pi}{4} \right) \right]$$

$$= -2\pi \left[ \left( -\frac{2\pi}{4} \right) - \left( \frac{\pi}{4} \right) \right]$$

$$= -2\pi \left[ \left( -\frac{2\pi}{4} \right) - \left( \frac{\pi}{4} \right) \right]$$
20. If the line  $\frac{2 - x}{3} = \frac{3y - 2}{4\lambda + 1} = 4 - z$  makes a right  
angle with the line  $\frac{x + 3}{3\mu} = \frac{1 - 2y}{6} = \frac{5 - z}{7}$ , then  
 $4\lambda + 9\mu$  is equal to : JEE Main Od  
(1) 13 (2) 4  
(3) 5 (4) 6  
Ans. (4)  
Sol.  $\frac{2 - x}{3} = \frac{3y - 2}{4\lambda + 1} = 4 - z$  ...(1)  
 $\frac{x - 2}{(-3)} = \frac{y - \frac{2}{3}}{\left(\frac{4\lambda + 1}{3}\right)} = \frac{z - 4}{(-1)}$ 

 $= \int_{-\pi}^{\pi} \frac{2y}{1 + \cos^2 y} \, dy + \int_{-\pi}^{\pi} \frac{2y \sin y}{1 + \cos^2 y} \, dy$ 

Ans. (1)

**Sol.**  $\int_{-\pi}^{\pi} \frac{2y(1+\sin y)}{1+\cos^2 y} dy$ 



$$\frac{x+3}{3\mu} = \frac{1-2y}{6} = \frac{5-z}{7} \qquad \dots (2)$$
  
$$\frac{x+3}{3\mu} = \frac{y-\frac{1}{2}}{(-3)} = \frac{z-5}{(-7)}$$
  
Right angle  $\Rightarrow (-3)(3\mu) + \left(\frac{4\lambda+1}{3}\right)(-3) + (-1)(-7) = 0$   
$$-9\mu - 4\lambda - 1 + 7 = 0$$
  
$$4\lambda + 9\mu = 6$$

### **SECTION-B**

21. From a lot of 10 items, which include 3 defective items, a sample of 5 items is drawn at random. Let the random variable X denote the number of defective items in the sample. If the variance of X is  $\sigma^2$ , then  $96\sigma^2$  is equal to\_\_\_\_\_.

Ans. (56)

**Sol.** X = denotes number of defective

Х	0	1	2	3	
P(x)	$\frac{7}{15}$	$\frac{5}{12}$	$\frac{5}{12}$	$\frac{1}{12}$	
$x_1^2$	0	1	4	9	
$P_i x_1^2$	0	$\frac{5}{12}$	$\frac{20}{12}$	$\frac{9}{12}$	
$p_i x_i$	0	$\frac{5}{12}$	$\frac{10}{12}$	$\frac{3}{12}$	

vr-2024 Paper ዞ Shẵṭṭ Ձ<sub>i</sub> =  $\frac{18}{12}$ 

$$\Sigma p_i x_1^2 = \frac{34}{12}$$

$$\sigma^2 = \Sigma p_i x_1^2 - (\mu)^2$$

$$= \frac{34}{12} - \left(\frac{18}{12}\right)^2 = \frac{17}{6} - \frac{9}{4}$$

$$\frac{34 - 27}{12} = \frac{7}{12}$$

$$96\sigma^2 = 96 \times \frac{7}{12} = 56$$

22. If the constant term in the expansion of  

$$(1 + 2x - 3x^3) \left(\frac{3}{2}x^2 - \frac{1}{3x}\right)^9$$
 is p, then 108p is equal  
to

Sol. 
$$(1+2x-3x^3)\left(\frac{3}{2}x^2-\frac{1}{3x}\right)^9$$
  
General term m $\left(\frac{3}{2}x^2-\frac{1}{3x}\right)^9$   
 $= {}^9C_r \cdot \frac{3^{9-2r}}{2^{9-r}}(-1)^r \cdot x^{18-3r}$   
Put r = 6 to get coeff. of  $x^0 = {}^9C_6 \cdot \frac{1}{6^3} \cdot x^0 = \frac{7}{18}x^0$ 

Put r = 7 to get coeff. of  $x^{-3} = {}^{9}C_{r} \cdot \frac{3^{-5}}{2^{2}} (-1)^{7} \cdot x^{-3}$ 

$$= -{}^{9}C_{7} \cdot \frac{1}{3^{5} \cdot 2^{2}} \cdot x^{-3} = \frac{-1}{27}x^{-3}$$
$$\left(1 + 2x - 3x^{3}\right) \left(\frac{7}{18}x^{0} - \frac{1}{27}x^{-3}\right)$$
$$\frac{7}{18} + \frac{3}{27} = \frac{7}{18} + \frac{1}{9} = \frac{7 + 2}{18} = \frac{9}{18} = \frac{1}{2}$$
$$\therefore 108 \cdot \frac{1}{2} = 54$$

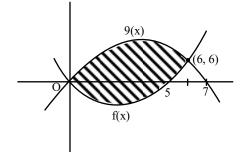
23. The area of the region enclosed by the parabolas

JEE Main 04

$$y = x^2 - 5x$$
 and  $y = 7x - x^2$  is \_\_\_\_\_  
Ans. (72)

NTA Ans. (198)

**Sol.**  $y = x^2 - 5x$  and  $y = 7x - x^2$ 





24.

a sum 16 on



$$\int_{0}^{6} (g(x) - f(x)) dx$$

$$\int_{0}^{6} ((7x - x^{2}) - (x^{2} - 5x)) dx$$

$$\int_{0}^{6} (12x - 2x^{2}) dx = \left[12\frac{x^{2}}{2} - \frac{2x^{3}}{3}\right]_{0}^{6}$$

$$\Rightarrow 6(6)^{2} - \frac{2}{3}(6)^{3}$$

$$= 216 - 144 = 72 \text{ unit}^{2}$$
The number of ways of getting throwing a dice four times is \_\_\_\_\_\_  
Ans. (125)

Sol. 
$$(x^{1} + x^{2} .... + x^{6})^{4}$$
  
 $x^{4} \cdot \left(\frac{1-x^{6}}{1-x}\right)^{4}$   
 $x^{4} \cdot (1-x^{6})^{4} \cdot (1-x)^{-4}$   
 $x^{4} [1-4x^{6} + 6x^{12} ....] [(1-x)^{-4}]$   
 $(x^{4} - 4x^{10} + 6x^{16} ....) (1-x)^{-4}$   
 $(x^{4} - 4x^{10} + 6x^{16}) (1 + {}^{15}C_{12}x^{12} + {}^{9}C_{6}x^{6} ....)$   
 $({}^{15}C_{12} - 4 \cdot {}^{9}C_{6} + 6)x^{16}$   
 $({}^{15}C_{3} - 4 \cdot {}^{9}C_{6} + 6)$   
 $= 35 \times 13 - 6 \times 8 \times 7 + 6$   
or-2024 Paper - Shift 2  
 $= 455 - 336 + 6$ 

= 125

25. If  $S = \{a \in R : |2a - 1| = 3[a]+2\{a\}\}$ , where [t] denotes the greatest integer less than or equal to t and  $\{t\}$  represents the fractional part of t, then  $72\sum_{a \in S} a$  is equal to \_\_\_\_\_.

Ans. (18)

Sol.  $|2a - 1| = 3[a] + 2\{a\}$ |2a - 1| = [a] + 2a

Case-1: 
$$a > \frac{1}{2}$$
  
 $2a - 1 = [a] + 2a$   
 $[a] = -1 \quad \therefore a \in [-1, 0)$  Reject  
Case-2:  $a < \frac{1}{2}$   
 $-2a + 1 = [a] + 2a$   
 $a = I + f$   
 $-2(I + f) + 1 = I + 2I + 2f$   
 $I = 0, f = \frac{1}{4} \quad \therefore a = \frac{1}{4}$   
Hence  $a = \frac{1}{4}$   
 $72\sum_{a \in S} a = 72 \times \frac{1}{4} = 18$   
Let f be a differentiable function

26. Let f be a differentiable function in the interval (0,  $\infty$ ) such that f(l) = 1 and  $\lim_{t \to x} \frac{t^2 f(x) - x^2 f(t)}{t - x} = 1$ 

for each x > 0. Then 2 f(2) + 3 f(3) is equal to

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Ans. (24)  
Sol. 
$$\lim_{t \to x} \frac{t^2 f(x) - x^2 f(t)}{t - x} = 1$$

$$\lim_{t \to x} \frac{2t f(x) - x^2 f'(x)}{1} = 1$$

$$2x f(x) - x2f'(x) = 1$$

$$\frac{dy}{dx} - \frac{2}{x} \cdot y = \frac{-1}{x^2}$$
I.f.  $= e^{\int -\frac{2}{x} dx} = \frac{1}{x^2}$ 

$$\therefore \frac{y}{x^2} = \int -\frac{1}{x^4} dx + C$$

$$\frac{y}{x^2} = \frac{1}{3x^3} + C$$
Put  $f(1) = 1$ 

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$$C = \frac{2}{3}$$

$$y = \frac{1}{3x} + \frac{2x^{2}}{3}$$

$$y = \frac{2x^{3} + 1}{3x}$$

$$f(2) = \frac{17}{6}$$

$$f(3) = \frac{55}{9}$$

$$2f(2) + 3f(3) = \frac{17}{3} + \frac{55}{3} = \frac{72}{3} = 24$$
27. Let  $a_{1}, a_{2}, a_{3}, ...$  be in an arithmetic progression of positive terms.  
Let  $A_{k} = a_{1}^{2} - a_{2}^{2} + a_{3}^{2} - a_{4}^{2} + ... + a_{2k-1}^{2} - a_{2k}^{2}$ .  
If  $A_{3} = -153$ ,  $A_{5} = -435$  and  $a_{1}^{2} + a_{2}^{2} + a_{3}^{2} = 66$ , then  $a_{17} - A_{7}$  is equal to \_\_\_\_\_\_.  
Ans. (910)  
Sol.  $d \rightarrow$  common diff.  
 $A_{k} = -kd[2a + (2k - 1)d]$   
 $A_{3} = -153$   
 $\Rightarrow 153 = 13d[2a + 5d]$  ...(1)  
 $A_{5} = -435$   
 $r-2024$  Paper - Shift 2  
 $87 = d[2a + 9d]$   
(2) - (1)  
 $36 = 4d^{2}$   
 $d = 3, a = 1$   
 $a_{17} - A_{7} = 49 - [-7.3[2 + 39]] = 910$   
28. Let  $\vec{a} = \hat{i} - 3\hat{j} + 7\hat{k}$ ,  $\vec{b} = 2\hat{i} - \hat{j} + \hat{k}$  and  $\vec{c}$  be a vector such that  $(\vec{a} + 2\vec{b}) \times \vec{c} = 3(\vec{c} \times \vec{a})$ . If  
 $\vec{a} \cdot \vec{c} = 130$ , then  $\vec{b} \cdot \vec{c}$  is equal to \_\_\_\_\_\_.

Sol. 
$$(\dot{a} + 2\ddot{b}) \times \ddot{c} = 3(\ddot{c} \times \ddot{a})$$
  
 $(2\ddot{b} + 4\ddot{a}) \times \ddot{c} = 0$   
 $\vec{c} = \lambda(4\vec{a} + 2\ddot{b}) = \lambda(8\hat{i} - 14\hat{j} + 30\hat{k})$   
 $\vec{a} \cdot \ddot{c} = 130$   
 $8\lambda + 42\lambda + 210\lambda = 130$   
 $\lambda = \frac{1}{2}$   
 $\vec{c} = 4\hat{i} - 7\hat{j} + 15\hat{k}$   
 $\vec{b} \cdot \vec{c} = 8 + 7 + 15 = 30$   
29. The number of distinct real roots of the equation  
 $|x| |x + 2| - 5|x + 1| - 1 = 0$  is \_\_\_\_\_\_.  
Ans. (3)  
 $\vec{c} = 3 \pm \sqrt{9 + 24} = 3 \pm \sqrt{33}$   
 $x = 3 \pm \sqrt{9 + 24} = 3 \pm \sqrt{33} - 2$   
One positive root  
 $Case - 2$   
 $-1 \le x < 0$   
 $x^2 - 2x - 5x - 5 - 1 = 0$   
 $x^2 + 7x + 6 = 0$   
 $(x + 6) (x + 1) = 0$   
 $x = -1$   
one root in range  
 $Case - 3$   
 $-2 \le x < -1$   
 $x^2 - 2x + 5x + 5 - 1 = 0$   
 $x^2 - 3x - 4 = 0$   
 $(x - 4) (x + 1) = 0$ 

be a





No root in range

$$x < -2$$
  

$$x^{2} + 7x + 4 = 0$$
  

$$x = \frac{-7 \pm \sqrt{49 - 16}}{2} = \frac{7 \pm \sqrt{33}}{2}$$

one root in range

Total number of distinct roots are 3

Suppose AB is a focal chord of the parabola 30.  $y^2 = 12x$  of length l and slope  $m < \sqrt{3}$ . If the distance of the chord AB from the origin is d, then  $ld^2$  is equal to \_\_\_\_\_.

Sol.

$$\ell = 4a \operatorname{cosec}^{2}\theta$$

$$\ell = 12 \times \frac{9}{d^{2}}$$

$$\ell d^{2} = 108$$

$$\ell d^{2} = 108$$

 $\ell = 4a \operatorname{cosec}^2 \theta$ 

$$\ell = 12 \times \frac{9}{d^2}$$
$$\ell d^2 = 108$$

r-2024 Paper - Shift 2

JEE Main 04



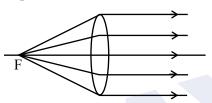
# PHYSICS



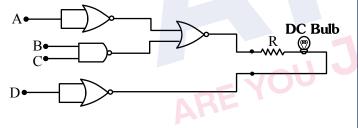
- **31.** Light emerges out of a convex lens when a source of light kept at its focus. The shape of wavefront of the light is:
  - (1) Both spherical and cylindrical
  - (2) Cylindrical
  - (3) Spherical
  - (4) Plane

## Ans. (4)

- Sol. Light emerges parallel
  - ∴ planor wavefront



**32.** Following gates section is connected in a complete suitable circuit.



- r-2024 PaperE Striftigh of the following combination, bulb will glow (ON):
  - (1) A = 0, B = 1, C = 1, D = 1(2) A = 1, B = 0, C = 0, D = 0(3) A = 0, B = 0, C = 0, D = 1

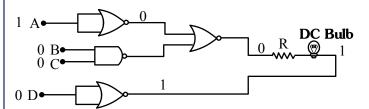
(4) 
$$A = 1, B = 1, C = 1, D = 0$$

## Ans. (2)

**Sol.** Bulb will glow if bulb have potential drop on it. One end of bulb must be at high (1) and other must be at low (0).

Option (2) satisfy this condition

### TEST PAPER WITH SOLUTION



- **33.** If G be the gravitational constant and u be the energy density then which of the following quantity have the dimension as that the  $\sqrt{uG}$ :
  - (1) Pressure gradient per unit mass
  - (2) Force per unit mass
  - (3) Gravitational potential
  - (4) Energy per unit mass

Sol.  $[uG] = [(M^1L^{-1}T^{-2}) (M^{-1}L^3T^{-2})]$  $[uG] = [M^0L^2T^{-4}]$ 

 $[\sqrt{uG}] = [L^1T^{-2}]$ 

Option (2) is correct

34. Given below are two statements :

**Statement-I**: When a capillary tube is dipped into a liquid, the liquid neither rises nor falls in the capillary. The contact angle may be  $0^{\circ}$ .

**Statement-II**: The contact angle between a solid and a liquid is a property of the material of the solid and liquid as well :

In the light of above statement, choose the **corFEEt**Main 04 answer from the options given below.

(1) Statement-I is false but Statement-II is true.

- (2) Both Statement-I and Statement-II are true.
- (3) Both Statement-I and Statement-II are false.
- (4) Statement-I is true and Statement-II is false.

## Ans. (1)

Sol. Capillary rise

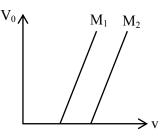
$$h = \frac{2T\cos\theta}{\rho gr};$$

If  $\theta = 0^{\circ}$  then rise is non-zero

- : Statement-1 is incorrect.
- Option(1) is correct



**35.** Given below are two statements:



**Statement-I:** Figure shows the variation of stopping potential with frequency (v) for the two photosensitive materials  $M_1$  and  $M_2$ . The slope gives value of  $\frac{h}{e}$ , where h is Planck's constant, e is

the charge of electron.

**Statement-II:**  $M_2$  will emit photoelectrons of greater kinetic energy for the incident radiation having same frequency.

In the light of the above statements, choose the most appropriate answer from the options given below.

(1) **Statement-I** is correct and **Statement-II** is incorrect.

(2) Statement-I is incorrect but Statement-II is correct.

(3) Both **Statement-I** and **Statement-II** are incorrect.

r-2024 Paper(45hiftoith Statement-I and Statement-II are correct.

Ans. (1)

**Sol.**  $eV_0 = hv - \phi$ 

$$V_0 = \frac{h}{e}v - \frac{\phi}{e}$$

 $M_2$  material has higher work function, so statement-(II) is incorrect.

Option (1) is correct.

36. The angle between vector  $\vec{Q}$  and the resultant of  $(2\vec{Q}+2\vec{P})$  and  $(2\vec{Q}-2\vec{P})$  is: (1) 0°

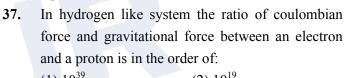
(2) 
$$\tan^{-1} \frac{(2\vec{Q} - 2\vec{P})}{2\vec{Q} + 2\vec{P}}$$
  
(3)  $\tan^{-1} \left(\frac{P}{Q}\right)$   
(4)  $\tan^{-1} \left(\frac{2Q}{P}\right)$ 

Ans. (1)

Sol. 
$$\vec{R} = (2\vec{Q} + 2\vec{P}) + (2\vec{Q} - 2\vec{P})$$
  
 $\vec{R} = 4\vec{Q}$ 

Angle between  $\vec{Q}$  and  $\vec{R}$  is zero

Option (1) is correct



(1) 
$$10^{39}$$
 (2)  $10^{19}$   
(3)  $10^{29}$  (4)  $10^{36}$ 

Sol. 
$$F_e = \frac{kQ_1Q_2}{r^2} = \frac{9 \times 10^9 \times 1.6 \times 10^{-19} \times 1.6 \times 10^{-19}}{r^2}$$
  
 $F_g = \frac{Gm_1m_2}{r^2} = \frac{6.67 \times 10^{-11} \times 9.1 \times 10^{-31} \times 1.6 \times 10^{-27}}{r^2}$   
 $\frac{F_e}{F_g} \approx 0.23 \times 10^{40} \approx 2.3 \times 10^{39}$  JEE Main 04

Option (1)

38. In a co-axial straight cable, the central conductor and the outer conductor carry equal currents in opposite directions. The magnetic field is zero.
(1) inside the outer conductor
(2) in between the two conductors

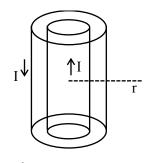
- (3) outside the cable
- (4) inside the inner conductor

Ans. (3)



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Sol.

 $\oint \vec{B}.d\vec{\ell} = \mu_0 i_{\text{enc}} = 0$ 

 $\therefore$  B = 0 outside the cable

**39.** An electron rotates in a circle around a nucleus having positive charge Ze. Correct relation between total energy (E) of electron to its potential energy (U) is:

(1) 
$$E = 2U$$
 (2)  $2E = 3U$   
(3)  $E = U$  (4)  $2E = U$ 

Ans. (4)

Sol. 
$$F = \frac{k(Ze)(e)}{r^2} = \frac{mv^2}{r}$$
$$KE = \frac{1}{2}mv^2 = \frac{1}{2}\frac{K(Ze)(e)}{r}$$
$$PE = -\frac{K(Ze)(e)}{r}$$
$$TE = \frac{K(Ze)(e)}{2r} - \frac{K(Ze)(e)}{r} = \frac{-K(Ze)(e)}{2r}$$
$$TE = \frac{PE}{2}$$
$$2TE = PE$$
Option (4)

40. If the collision frequency of hydrogen molecules in a closed chamber at 27°C is Z, then the collision frequency of the same system at 127° C is :

(1) 
$$\frac{\sqrt{3}}{2}Z$$
 (2)  $\frac{4}{3}Z$   
(3)  $\frac{2}{\sqrt{3}}Z$  (4)  $\frac{3}{4}Z$ 

Ans. (3)

Sol. Assuming mean free path constant.

$$f \propto v \propto \sqrt{T}$$

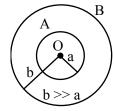
$$\frac{f_1}{f_2} = \sqrt{\frac{T_1}{T_2}} = \sqrt{\frac{300}{400}}$$

$$f_2 = \sqrt{\frac{4}{3}} = f_1 = \frac{2}{\sqrt{3}}Z$$

**41.** Ratio of radius of gyration of a hollow sphere to that of a solid cylinder of equal mass, for moment of Inertia about their diameter axis AB as shown in

04

**42.** Two conducting circular loops A and B are placed in the same plane with their centres coinciding as shown in figure. The mutual inductance between them is:





(1) 
$$\frac{\mu_0 \pi a^2}{2b}$$
 (2)  $\frac{\mu_0}{2\pi} \cdot \frac{b^2}{a}$   
(3)  $\frac{\mu_0 \pi b^2}{2a}$  (4)  $\frac{\mu_0}{2\pi} \cdot \frac{a^2}{b}$ 

Ans. (1)

**Sol.**  $\phi = Mi = BA$ 

$$\Rightarrow Mi = \frac{\mu_0 i}{2b} \pi a^2$$
$$\therefore M = \frac{\mu_0 \pi a^2}{2b}$$

Match list-I with list-II: 43.

	List-I		List-II
(A)	Kinetic energy of planet	(I)	GMm
			а
(B)	Gravitation Potential	(II)	GMm
	energy of Sun-planet		2a
	system.		
(C)	Total mechanical energy	(III)	Gm
	of planet		r
(D)	Escape energy at the	(IV)	GMm
	surface of planet for unit		2a
	mass object		

(Where a = radius of planet orbit, r = radius of planet, M = mass of Sun, m = mass of planet) Choose the correct answer from the options given below:

(1)(A) - II, (B) - I, (C) - IV, (D) - IIIr-2024 Paper(2) htt -2 III, (B) - IV, (C) - I, (D) - II (3)(A) - I, (B) - IV, (C) - II, (D) - III

$$(4) (A) - I, (B) - II, (C) - III, (D) - IV$$

Ans. (1)

Sol. 
$$KE = \frac{1}{2}mv^2 = \frac{GMm}{2a}$$
  
 $PE = -2KE$   
 $TE = -KE$ 

A wooden block of mass 5kg rests on soft **44**. horizontal floor. When an iron cylinder of mass 25 kg is placed on the top of the block, the floor yields and the block and the cylinder together go down with an acceleration of  $0.1 \text{ ms}^{-2}$ . The action force of the system on the floor is equal to:

(3) 291 N

Ans. (3)

Sol.

Taking g = 
$$9.8 \text{ m/s}^2$$
  
 $25 \text{ kg}$   $0.1 \text{ m/s}^2$   
 $N \uparrow \sqrt{30 \times 9.8} = 294$   
 $294 - \text{N} = 30 \times 0.1$   
 $\text{N} = 291$ 

45. A simple pendulum doing small oscillations at a place R height above earth surface has time period of  $T_1 = 4$  s.  $T_2$  would be it's time period if it is brought to a point which is at a height 2R from earth surface. Choose the correct relation [R =radius of Earth]:

(2)  $2T_1 = 3T_2$ 

(1) 
$$T_1 = T_2$$

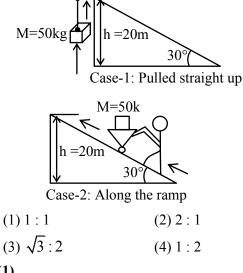
(3) 
$$3T_1 = 2T_2$$
 (4)  $2T_1 = T_2$ 

Ans. (3)

Sol. 
$$T_1 = 2\pi \sqrt{\frac{\ell}{GM}} (2R)^2$$
  
 $T_2 = 2\pi \sqrt{\frac{\ell}{GM}} (3R)^2$   
 $\therefore \frac{T_1}{T_2} = \frac{2}{3}$ 

JEE Main 04

46. A body of mass 50 kg is lifted to a height of 20 m from the ground in the two different ways as shown in the figures. The ratio of work done against the gravity in both the respective cases, will be:



### Ans. (1)

- **Sol.** Work done by gravity is independent of path. It depends only on vertical displacement so work done in both cases will be same. Option (1) is correct
- **47.** Time periods of oscillation of the same simple pendulum measured using four different measuring clocks were recorded as 4.62 s, 4.632 s, 4.6 s and 4.64 s. The arithmetic mean of these reading in correct significant figure is.

(1) 
$$4.623$$
 s (2)  $4.62$  s

(3) 4.6 s

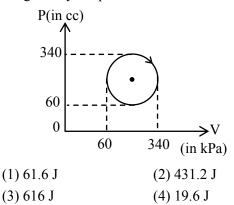
Ans. (3)

Sol. Sum of number by considering significant digit sum = 4.6 + 4.6 + 4.6 + 4.6 = 18.4

(4) 5 s

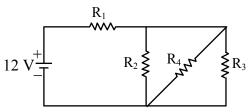
Arithmetic Mean =  $\frac{\text{sum}}{4} = \frac{18.4}{4} = 4.6$ r-2024 Paper - Shift 2

**48.** The heat absorbed by a system in going through the given cyclic process is :



## Ans. (1)

- Sol.  $\Delta U = 0$  (Cyclic process)  $\Delta Q = W = \text{area of P-V curve.}$   $= \pi \times (140 \times 10^3 \text{ Pa}) \times (140 \times 10^{-6} \text{ m}^3)$  $\Delta Q = 61.6 \text{ J}$
- **49.** In the given figure  $R_1 = 10\Omega$ ,  $R_2 = 8\Omega$ ,  $R_3 = 4\Omega$ and  $R_4 = 8\Omega$ . Battery is ideal with emf 12V. Equivalent resistant of the circuit and current supplied by battery are respectively.



(1) 12 $\Omega$ and 11.4 A	(2) 10.5 $\Omega$ and 1.14 A
(3) 10.5 $\Omega$ and 1 A	(4) 12 $\Omega$ and 1 A

Sol. Here 
$$R_2$$
,  $R_3$ ,  $R_4$  are in parallel

$$\frac{1}{R_{234}} = \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}$$

$$R_{234} = 2\Omega$$

$$R_{234} \text{ is in series with } R_1 \text{ so}$$

$$R_{eq} = R_{234} + R_1 = 2 + 10 = 12\Omega$$

$$i = \frac{12}{12} = 1 \text{ Amp}$$

50. An alternating voltage of amplitude 40 V and frequency 4 kHz is applied directly across the capacitor of 12  $\mu$ F. The maximum displacent Main 04 current between the plates of the capacitor is nearly:

Ans. (4)

Ans. (4)

**Sol.** Displacement current is same as conduction current in capacitor.

$$X_{\rm C} = \frac{1}{\omega {\rm C}} = \frac{1}{2\pi {\rm f}{\rm C}}$$
$$= \frac{1}{2\pi \times 4 \times 10^3 \times 12 \times 10^{-6}} = 3.317 {\rm \Omega}$$



$$I = \frac{V}{X_{\rm C}} = \frac{40}{3.317} = 12A$$

#### **SECTION-B**

51. In Young's double slit experiment, carried out with light of wavelength 5000Å, the distance between the slits is 0.3 mm and the screen is at 200 cm from the slits. The central maximum is at x = 0 cm. The value of x for third maxima is ...... mm.

#### Ans. (10)

Sol.  $\beta = \frac{\lambda D}{d} = \frac{5 \times 10^{-7} \times 2}{3 \times 10^{-4}} = \frac{10 \times 10^{-3}}{3} \text{ m}$ For 3<sup>rd</sup> maxima  $y_2 = 3\beta = 10 \times 10^{-3} \text{ m} =$ 

or 
$$3^{10}$$
 maxima  $y_3 = 3\beta = 10 \times 10^{-3}$  m = 10 mm

Ans. (5)

Sol. 
$$R = \frac{\rho \ell}{A} \Longrightarrow \frac{2 \times 10^{-6} \times \ell}{10^{-5}} = 1 \implies \ell = 5$$

 $mg = Bi\ell$ 

$$B = \frac{mg}{i\ell} = \frac{5}{2 \times 5} = 0.5 = 5 \times 10^{-1} \text{ Tesla}$$

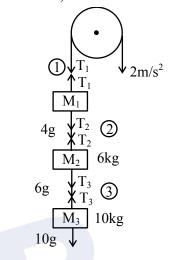
53. The electric field between the two parallel plates of a capacitor of 1.5  $\mu$ F capacitance drops to one third

**pr-2024 Paper** Of Shift Shift value in 6.6 μs when the plates are connected by a thin wire. The resistance of this wire is ......  $\Omega$ . (Given, log 3 = 1.1)

Ans. (4)

Sol. 
$$E = \frac{E_0}{3} \Longrightarrow V = \frac{V_0}{3}$$
$$\frac{V_0}{3} = V_0 e^{-\frac{t}{\tau}}$$
$$t = \tau \ell n 3$$
$$6.6 \times 10^{-6} = R (1.5 \times 10^{-6})(1.1)$$
$$R = \frac{6}{1.5} = 4\Omega$$

54. Three blocks  $M_1$ ,  $M_2$ ,  $M_3$  having masses 4 kg, 6 kg and 10 kg respectively are hanging from a smooth pully using rope 1, 2 and 3 as shown in figure. The tension in the rope 1,  $T_1$  when they are moving upward with acceleration of  $2ms^{-2}$  is ...... N (if  $g = 10 \text{ m/s}^2$ )



Ans. (240)

**Sol.** FBD of 
$$M_1$$

 $10 \text{ m/s}^2$ )

Ans. (600)



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Sol.  

$$T = mg$$

$$\sigma = \frac{T}{A} = \frac{mg}{A}$$

$$\frac{(\sigma A \ell)g}{A}$$
$$\Rightarrow \ell = \frac{\sigma}{\rho g} = \frac{1.2 \times 10^8 \times 3}{6 \times 10^4 \times 10} = 600$$

56. A body moves on a frictionless plane starting from rest. If  $S_n$  is distance moved between t = n - 1 and t = n and  $S_{n-1}$  is distance moved between t = n - 2and t = n - 1, then the ratio  $\frac{S_{n-1}}{S_n}$  is  $\left(1 - \frac{2}{x}\right)$  for n

= 10. The value of x is  $\dots$ 

Ans. (19)

Sol. 
$$S_n = \frac{1}{2}a(2n-1) = \frac{19a}{2}$$
  
 $S_{n-1} = \frac{1}{2}a(2n-3) = \frac{17a}{2}$   
 $\frac{S_{n-1}}{S} = \frac{17}{10} = 1 - \frac{2}{n} \Rightarrow x = 19$ 

r-2024 Paper - Shift 29

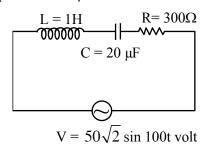
57. If three helium nuclei combine to form a carbon nucleus then the energy released in this reaction is  $\dots \times 10^{-2}$  MeV. (Given 1 u = 931 MeV/c<sup>2</sup>, atomic mass of helium = 4.002603 u)

Ans. (727)

$$3_2^4 \text{He} \longrightarrow {}_6^{12}\text{C} + \gamma \text{ rays}$$
  
Mass defect =  $\Delta m = (3m_{\text{He}} - m_{\text{C}})$   
=  $(3 \times 4.002603 - 12) = 0.007809 \text{ u}$   
Energy released  
= 931  $\Delta m$  MeV

 $= 7.27 \text{ MeV} = 727 \times 10^{-2} \text{ MeV}$ 

**58.** An ac source is connected in given series LCR circuit. The rms potential difference across the capacitor of 20  $\mu$ F is .....V.



## Ans. (50)

Sol.  $X_L = \omega L = 100 \times 1 = 100\Omega$ 

$$X_{\rm C} = \frac{1}{\omega {\rm C}} = \frac{1}{100 \times 20 \times 10^{-6}} = 500\Omega$$
  

$$Z = \sqrt{(X_{\rm L} - X_{\rm C})^2 + {\rm R}^2}$$
  

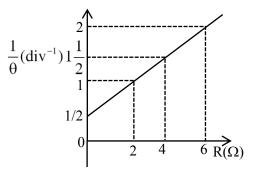
$$\sqrt{(100 - 500)^2 + 300^2}$$
  

$$Z = 500\Omega$$
  

$$i_{\rm rms} = \frac{V_{\rm rms}}{Z} = \frac{50}{500} = 0.1{\rm A}$$
  
rms voltage agrees oppositor

rms voltage across capacitor  $V_{rms} = X_C i_{rms}$ =500 × 0.1 = 50V

**59.** In the experiment to determine the galvanometer resistance by half-deflection method, the plot of  $\frac{1}{\Omega}$ 









Sol. 
$$i = K\theta$$
  

$$\frac{2}{G+R} = K\theta$$

$$\Rightarrow \frac{1}{\theta} = \frac{(G+R)K}{2} = R\left(\frac{K}{2}\right) + \frac{KG}{2}$$
Slope  $= \frac{K}{2} = \frac{1}{4} \Rightarrow K = 0.5 = 5 \times 10^{-1} A$ 

60. Three capacitors of capacitances 25  $\mu$ F, 30  $\mu$ F and 45  $\mu$ F are connected in parallel to a supply of 100 V. Energy stored in the above combination is E. When these capacitors are connected in series to the same supply, the stored energy is  $\frac{9}{x}$ E. The value of x is .....

### Ans. (86)

**Sol.** In parallel combination : Potential difference is same across all

Energy = 
$$\frac{1}{2}(C_1 + C_2 + C_3)V^2$$
  
=  $\frac{1}{2}(25 + 30 + 45) \times (100)^2 \times 10^{-6} = 0.5 = E$ 

In series combination: Charge is same on all.

$$\frac{1}{C_{equ}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} = \frac{1}{25} + \frac{1}{30} + \frac{1}{45}$$
$$\frac{1}{C_{equ}} = \frac{(18 + 15 + 10)}{450} = \frac{43}{450} \implies C_{equ} = \frac{450}{43}$$

r-2024 PaperEnding t ₹  $\frac{Q^2}{2C_1} + \frac{Q^2}{2C_2} + \frac{Q^2}{2C_3}$ 

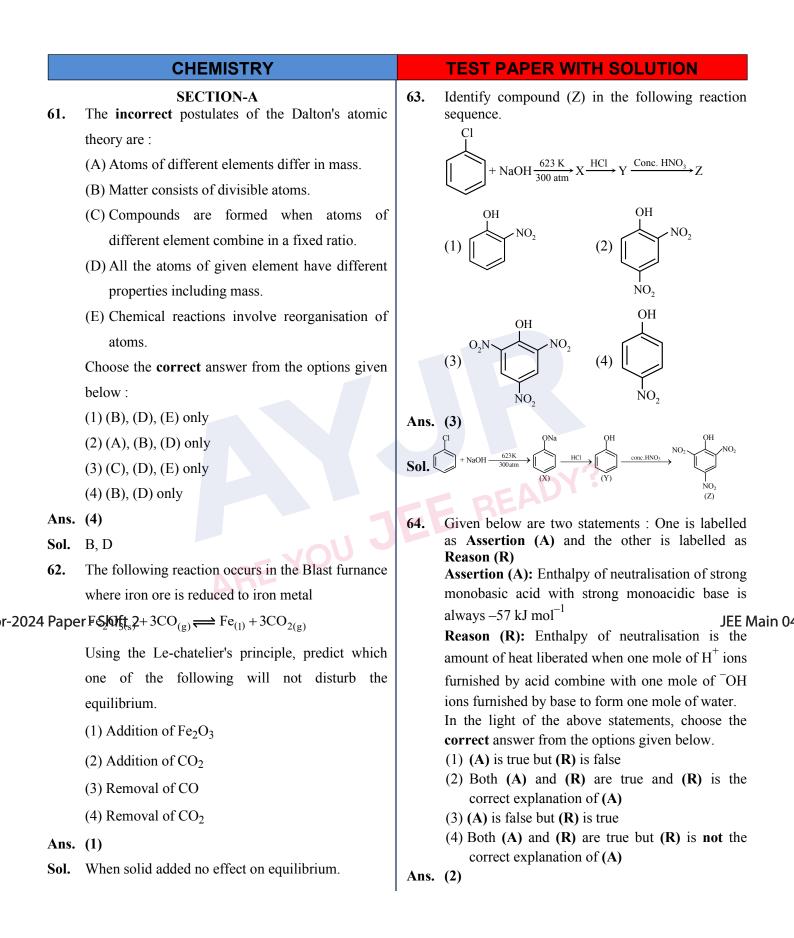
$$= \frac{Q^{2}}{2} \left[ \frac{1}{C_{1}} + \frac{1}{C_{2}} + \frac{1}{C_{3}} \right]$$
$$\frac{(V \times C_{equ})^{2}}{2} \times \frac{1}{C_{equ}} = \frac{V^{2}C_{equ}}{2}$$
$$\frac{(100)^{2}}{2} \times \frac{450}{43} \times 10^{-6}$$
$$\Rightarrow \frac{4.5}{86} = \frac{9}{x} E = \frac{9}{x} \times 0.5 \Rightarrow x = 86$$

JEE Main 04

EE READY?









- **Sol.** Enthalpy of neutralization of SA & SB is always -57 kJ / mol because strong monoacid gives one mole of H<sup>+</sup> and strong mono base gives one mole of OH<sup>-</sup> which form one mole of water.
- 65. The statement(s) that are **correct** about the species  $O^{2-}, F^{-}, Na^{+} and Mg^{2+}$ .
  - (A) All are isoelectronic
  - (B) All have the same nuclear charge
  - (C)  $O^{2-}$  has the largest ionic radii

(D)  $Mg^{2+}$  has the smallest ionic radii

Choose the most appropriate answer from the options given below :

- (1) (B), (C) and (D) only
- (2) (A), (B), (C) and (D)
- (3)(C) and (D) only
- (4) (A), (C) and (D) only
- Ans. (4)

Sol.

- $O^{-2}$  F<sup>-</sup> Na<sup>+</sup>  $Mg^{+2}$ (No. of  $e^{-}$ ) 10 10 10 (Ionic radius)  $O^{-2} > F^{-} > Na^{+} > Mg^{+2}$  $O^{-2} < F^{-} < Na^{+} < Mg^{+2}$ Zeff
- 66. For the compounds:
  - (A) H<sub>3</sub>C-CH<sub>2</sub>-O-CH<sub>2</sub>-CH<sub>2</sub>-CH<sub>3</sub>
  - (B) H<sub>3</sub>C-CH<sub>2</sub>-CH<sub>2</sub>-CH<sub>2</sub>-CH<sub>3</sub>

(C) 
$$CH_3-CH_2-C-CH_2-CH_3$$
  
(D)  $H_3C-CH-CH_2-CH_2-CH_3$   
OH

r-2024 Paper Flshift 2 asing order of boiling point is :

I ОН

Choose the correct answer from the options given below :

- (1) (A)  $\leq$  (B)  $\leq$  (C)  $\leq$  (D)
- (2) (B)  $\leq$  (A)  $\leq$  (C)  $\leq$  (D)
- (3) (D)  $\leq$  (C)  $\leq$  (A)  $\leq$  (B)
- (4) (B)  $\leq$  (A)  $\leq$  (D)  $\leq$  (C)

## Ans. (2)

Sol. Compounds having same number of carbon atoms follow the boiling point order as:

> (Boiling point)<sub>Hydrogen bonding</sub> >(Boiling point)<sub>high polarity</sub> > (Boiling point)<sub>low polarity</sub> > (Boiling point)<sub>non polar</sub>

**67.** Given below are two statements :

Statement I: In group 13, the stability of +1 oxidation state increases down the group.

Statement II: The atomic size of gallium is greater than that of aluminium.

In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) Statement I is incorrect but Statement II is correct
- (2) Both Statement I and Statement II are correct
- (3) Both Statement I and Statement II are incorrect
- (4) Statement I is correct but Statement II is incorrect

## Ans. (4)

Sol. Statement I : Number of d & f electrons, increases down the group and due to poor shielding of d & f e, stability of lower oxidation states increases down the group

> Statement II : The atomic size of aluminium is greater than that of gallium.

Number of  $\sigma$  and  $\pi$  bonds present in ethylene 68. molecule is respectively:

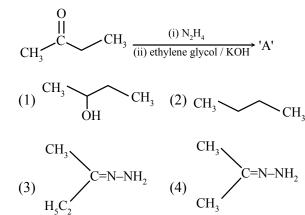
(4) 5 and 1

Ans. (4)

 $1\pi$  bond.

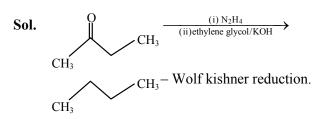
JEE Main 04

69. Identify 'A' in the following reaction :



Ans. (2)





- The reaction at cathode in the cells commonly used 70. in clocks involves.
  - (1) reduction of Mn from +4 to +3
  - (2) oxidation of Mn from +3 to +4
  - (3) reduction of Mn from + 7 to +2
  - (4) oxidation of Mn from + 2 to +7

Ans. (1)

- Sol. In the cathode reaction manganese (Mn) is reduced from the +4 oxidation state to the +3 state.
- Which one of the following complexes will exhibit 71. the least paramagnetic behaviour?

[Atomic number, 
$$Cr = 24$$
,  $Mn = 25$ ,  $Fe = 26$ ,  $Co = 27$ ]

(4)  $[Cr(H_2O)_6]^{2+}$ 

$$[Co(H_2O)_6]^{2+}$$
 (2)  $[Fe(H_2O)_6]^{2+}$ 

$$(3) [Mn(H_2O)_6]^{2+}$$

Ans. (1) Sol.

(1

	Number of unpaired e	$\mu = \sqrt{n(n+2)} \text{ B.M.}$
$[Co(H_2O)_6]^{2+}$	3	3.87
$\left[\mathrm{Fe}(\mathrm{H}_{2}\mathrm{O})_{6}\right]^{2+}$	4	4.89
$[Mn(H_2O)_6]^{2+}$	5	5.92
$[Cr(H_2O)_6]^{2+}$	4	4.89

Least paramagnetic behaviour =  $[Co(H_2O)_6]^{2+1}$ 

- 72. Given below are two statements : one is labelled
- as Assertion (A) and the other is labelled as  $r_{\bar{R}}$  Shift 2 Reason (R). r-2024 Pape

Assertion (A): Cis form of alkene is found to be more polar than the trans form

Reason (R): Dipole moment of trans isomer of 2-butene is zero.

In the light of the above statements, choose the correct answer from the options given below :

- (1) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)
- (2) (A) is true but (R) is false
- (3) Both (A) and (R) are true and (R) is the correct explanation of (A)
- (4) (A) is false but (R) is true

Ans. (3)

Sol. Dipole moment is a vector quantity and for compound net dipole moment is the vector sum of all dipoles hence dipole moment of cis form is greater than trans form.

$$\begin{array}{c} \mu:CH_{3} \\ H \\ Cis \\ (\mu > 0) \end{array} > \begin{array}{c} H \\ CH_{3} \\ CH_{3} \\ CH_{3} \\ (\mu = 0) \end{array} = \begin{array}{c} CH_{3} \\ H \\ CH_{3} \\ (\mu = 0) \end{array}$$

73. Given below are two statements :

> Statement I: Nitration of benzene involves the following step -

$$H - \bigcup_{\bullet}^{H} - NO_2 \longrightarrow H_2O + NO_2$$

Statement II: Use of Lewis base promotes the electrophilic substitution of benzene.

In the light of the above statements, choose the most appropriate answer from the options given below :

- (1) Both Statement I and Statement II are incorrect
- (2) Statement I is correct but Statement II is incorrect
- (3) Both Statement I and Statement II are correct
- (4) Statement I is incorrect but Statement II is correct
- Ans. (2)
- JEE Main 04 In nitration of benzene concentrated H<sub>2</sub>SO<sub>4</sub> and Sol. HNO<sub>3</sub> is used as reagent which generates electrophile  $NO_2$  in following steps:

Lewis acids can promote the formation of electrophiles not Lewis base



- 74. The correct order of ligands arranged in increasing field strength. (1)  $Cl^- < OH < Br^- < CN^-$ (2)  $F^- < Br^- < I^- < NH_3$ (3)  $Br^{-} < F^{-} < H_2O < NH_3$ (4)  $H_2O < OH < CN < NH_3$ Ans. (3) **Sol.** Experimental order  $Br^- < F^- < H_2O < NH_3$ Which of the following gives a positive test with 75. ninhvdrin? (1) Cellulose (2) Starch (3) Polyvinyl chloride (4) Egg albumin Ans. (4) Sol. Ninhydrin test is a test of amino acids. Egg albumin contains protein which is a natural polymer of amino acids which will show positive ninhvdrin test 76. The metal that shows highest and maximum number of oxidation state is: (1) Fe (2) Mn (3) Ti (4) Co Ans. (2) Sol. Mn shows highest oxidation state  $(Mn^{+7})$  in 3d series metals. 77. Ail organic compound has 42.1% carbon, 6.4% hydrogen and remainder is oxygen. If its molecular weight is 342, then its molecular formula is :  $(1) C_{11}H_{18}O_{12}$  $(2) C_{12}H_{20}O_{12}$  $(3) C_{14}H_{20}O_{10}$  $C_{12}H_{22}O_{11}$ Ans. (4) Sol. only  $C_{12}H_{22}O_{11}$  has 42.1% carbon, 6.4% hydrogen & 51.5 percent oxygen. r-2024 Paper Shift 2 Given below are two statement : Statement I : Bromination of phenol in solvent with low polarity such as CHCl<sub>3</sub> or CS<sub>2</sub> requires Lewis acid catalyst. Statement II : The lewis acid catalyst polarises the bromine to generate  $Br^+$ . In the light of the above statements, choose the correct answer from the options given below : (1) Statement I is true but Statement II is false. (2) Both Statement I and Statement II are true (3) Both Statement I and Statement II are false. (4) Statement I is false but Statement II is true.
  - Ans. (4)

- **Sol.** Phenol is a highly activated compound which can undergo bromination directly with Bromine without any lewis acid.
- 79. Molar ionic conductivities of divalent cation and anion are 57 S cm<sup>2</sup> mol<sup>-1</sup> and 73 S cm<sup>2</sup> mol<sup>-1</sup> respectively. The molar conductivity of solution of an electrolyte with the above cation and anion will be ·

(1) 65 S  $\text{cm}^2 \text{mol}^{-1}$ (2) 130 S cm<sup>2</sup> mol<sup>-1</sup> (3) 187 S cm<sup>2</sup> mol<sup>-1</sup> (4) 260 S cm<sup>2</sup> mol<sup>-1</sup>

Ans. (2)

Sol. 
$$\Lambda_{\rm C}^{+2} = 57 \, {\rm S} \, {\rm cm}^2 \, {\rm mol}^{-1}$$
  
 $\Lambda_{\rm A}^{+2} = 73 \, {\rm S} \, {\rm cm}^2 \, {\rm mol}^{-1}$   
 $\Lambda_{\rm Solution} = \lambda_{\rm C}^{+2} + \Lambda_{\rm A}^{-2}$   
 $= 57 + 73 = 130$ 

80. The number of neutrons present in the more abundant isotope of boron is 'x'. Amorphous boron upon heating with air forms a product, in which the oxidation state of boron is 'y'. The value of x + y is ...

$$\begin{array}{c} (1) 4 \\ (3) 3 \\ (4) 9 \end{array}$$

More abundant isotope =  $B^{11}$ Sol. [Number of neutrons = 6]  $\mathbf{x} = 6$ 

 $B + O_2 \rightarrow B_2O_3$ 

Oxidation state of B in  $B_2O_3 = +3$ 

So, y = 3

Hence x + y = 9

**SECTION-B** 

JEE Main 04

The value of Rydberg constant (R<sub>H</sub>) is  $2.18 \times 10^{-18}$  J. 81. The velocity of electron having mass  $9.1 \times 10^{-31}$  kg in Bohr's first orbit of hydrogen atom = .....×10<sup>5</sup> ms<sup>-1</sup> (nearest integer)

Ans. (22)

Sol. 
$$V = 2.18 \times 10^6 \times \frac{Z}{n}$$
  
=  $21.8 \times 10^5 \times \frac{1}{1} \approx 22 \times 10^5$  (nearest)

 $82. \qquad \begin{pmatrix} \circ \\ \circ \\ \bullet \end{pmatrix}^{A}_{B}$ 

In a borax bead test under hot condition, a metal salt (one from the given) is heated at point B of the flame, resulted in green colour salt bead. The spin-only magnetic moment value of the salt is ......BM (Nearest integer)

[Given atomic number of Cu = 29, Ni = 28, Mn = 25, Fe = 26]

# Ans. (6)

**Sol.** Fe<sup>+3</sup> will give green coloured bead when heated at point B.

Number of unpaired  $e^-$  in  $Fe^{+3} = 5$  $\mu = 5.92$ 

Nearest integer = 6

83. The heat of combustion of solid benzoic acid at constant volume is -321.30 kJ at 27°C. The heat of combustion at constant pressure is (-321.30 - xR) kJ, the value of x is .....

Ans. (150)

Sol. 
$$C_6H_5COOH(S) + \frac{15}{2}O_2(g) \rightarrow 7CO_2(g) + 3H_2O(\ell)$$
  
 $\Delta H = \Delta U + \Delta n_BT$ 

$$= -321.30 - \frac{1}{2} \frac{R}{100} \times 300$$

= (-321.30 - 150R) kJr-2024 Paper - Shift 2 84 Consider the given che

84. Consider the given chemical reaction sequence :

$$\underbrace{\underbrace{\text{Conc. H}_2\text{SO}_4}}_{\text{Conc. H}_2\text{SO}_4} \text{Product A} \xrightarrow{\text{Conc. H}_3\text{NO}_3} \text{Product B}$$

Total sum of oxygen atoms in Product A and Product B are .....

Ans. (14)

**Sol.** Picric acid is prepared by treating phenol first with concentrated sulphuric acid which converts it to phenol-2,4-disulphonic acid and then with concentrated nitric acid to get 2, 4, 6 trinitrophenol.

Co : 27)

Ans. (5) Sol. Strong oxidising agent =  $Co^{+3}$ 

No. of unpaired  $e^-$  in  $Co^{+3}[3d^6] = 4$ Hence  $\mu = \sqrt{n(n+2)} = \sqrt{24}$  BM Nearest integer = 5

86. During Kinetic study of reaction  $2A + B \rightarrow C + D$ , the following results were obtained :

	A[M] B[M]		initial rate of	
			formation of D	
Ι	0.1	0.1	$6.0 \times 10^{-3}$	
ΙΙ	0.3	0.2	$7.2 \times 10^{-2}$	
Ш	0.3	0.4	$2.88 \times 10^{-1}$	
IV	0.4	0.1	$2.40 \times 10^{-2}$	

Based on above data, overall order of the reaction is .....

JEE Main 04

# Ans. (3)

Sol. 
$$r = K[A]^{x}[B]^{y}$$
  
(I)  $6 \times 10^{-3} = K[0.1]^{x}[0.1]^{y}$   
(IV)  $2.4 \times 10^{-2} = K[0.4]^{x}[0.1]^{y}$   
(IV)/(I)  
 $4 = (4)^{x}$   
 $x = 1$   
 $r = K[A]^{x}[B]^{y}$   
(III)  $2.88 \times 10^{-1} = K[0.3]^{x}[0.4]^{y}$   
(II)  $7.2 \times 10^{-2} = K[0.3]^{x}[0.2]^{y}$   
(III)/(II)  
 $4 = 2^{y}$   
 $y = 2$   
Overall order =  $x + y = 1 + 2 = 3$ 



87. An artificial cell is made by encapsulating 0.2 M glucose solution within a semipermeable membrane. The osmotic pressure developed when the artificial cell is placed within a 0.05 M solution of NaCl at 300 K is \_\_\_\_\_  $\times 10^{-1}$  bar. (Nearest Integer)

[Given :  $R = 0.083 L \text{ bar mol}^{-1} K^{-1}$ ]

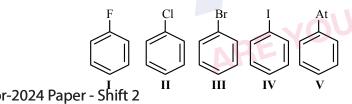
Assume complete dissociation of NaCl

### Ans. (25)

Sol.

0.2 M	0.05 M
Glucose N	JaCl Sol.

- NaCl  $\longrightarrow$  Na<sup>+</sup> + Cl<sup>-</sup> 0.05M 0.05M 0.05M Total C<sub>1</sub> = 0.05 + 0.05 = 0.1 M (NaCl) C<sub>2</sub> = 0.2 M (glucose)  $\pi = (C_2 - C_1) RT$ = (0.2 - 0.1) × 0.083 × 300 = 2.49 bar = 24.9 × 10<sup>-1</sup> bar
- **88.** The number of halobenzenes from the following that can be prepared by Sandmeyer's reaction is ......



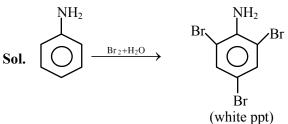
Ans. (2)

- **Sol.** In Sandmayer reaction only bromobenzene & chlorobenzene are prepared
- **89.** In the lewis dot structure for  $NO_2^{-}$ , total number of valence electrons around nitrogen is .....
- Ans. (8)
- Sol.

Number of valence  $e^-$  around N-atom = 8

- 90. 9.3 g of pure aniline is treated with bromine water at room temperature to give a white precipitate of the product 'P'. The mass of product 'P' obtained is 26.4 g. The percentage yield is ..........%.
- Ans. (80)

EE READ



93 g of aniline produces 330 g of 2, 4, 6tribromoaniline. Hence 9.3 g of aniline should produce 33g of 2, 4, 6-tribromoaniline. Hence percentage yield  $\frac{26.4 \times 100}{33} = 80\%$ 

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